



# Development and Applications of Josephson Arbitrary Waveform Synthesizers

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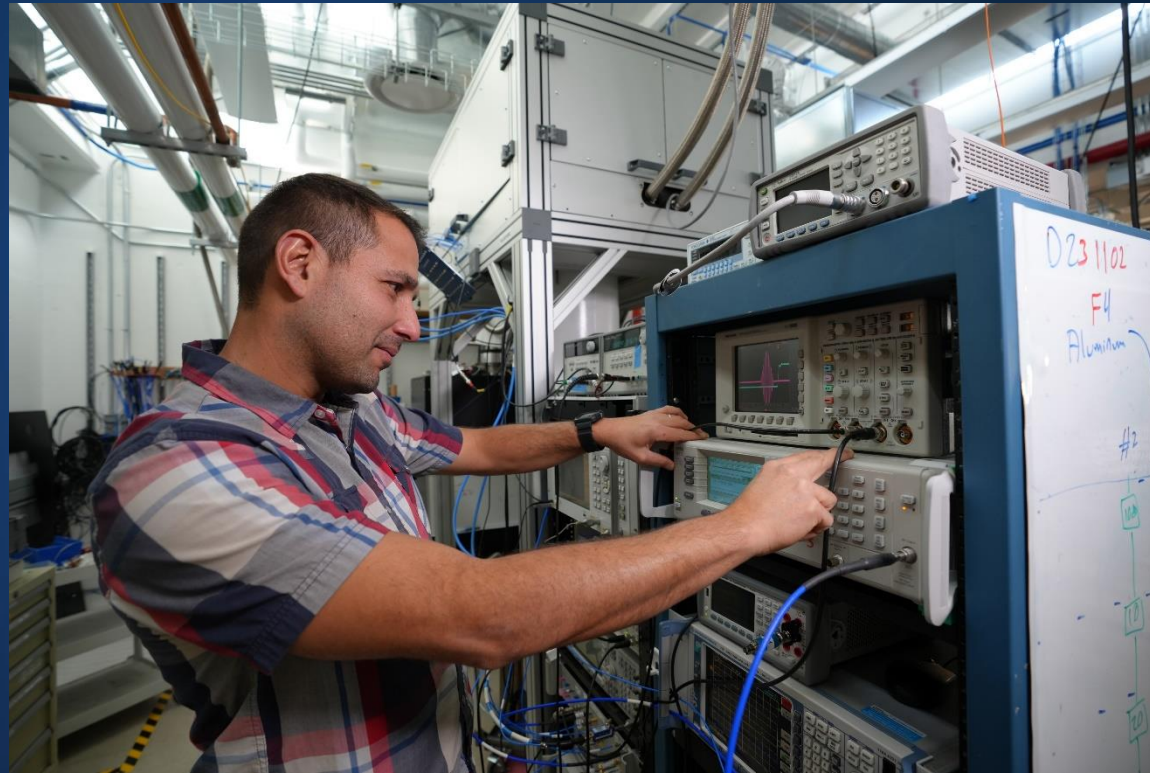


# Superconductive Electronics Group





# Superconductive Electronics Group Research



- DC, AC & RF quantum-based Josephson Voltage Standards (JVS)
- Independent test & measurement of industry energy-efficient superconducting devices
- Develop precision measurements and scalable control circuits for quantum computing

# Outline

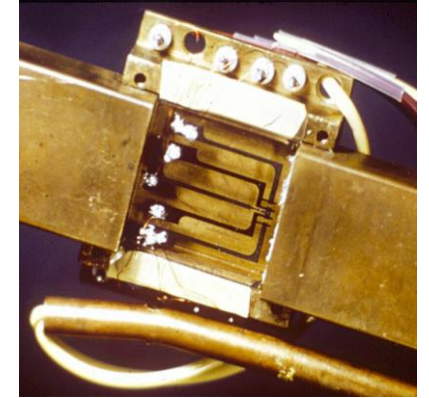
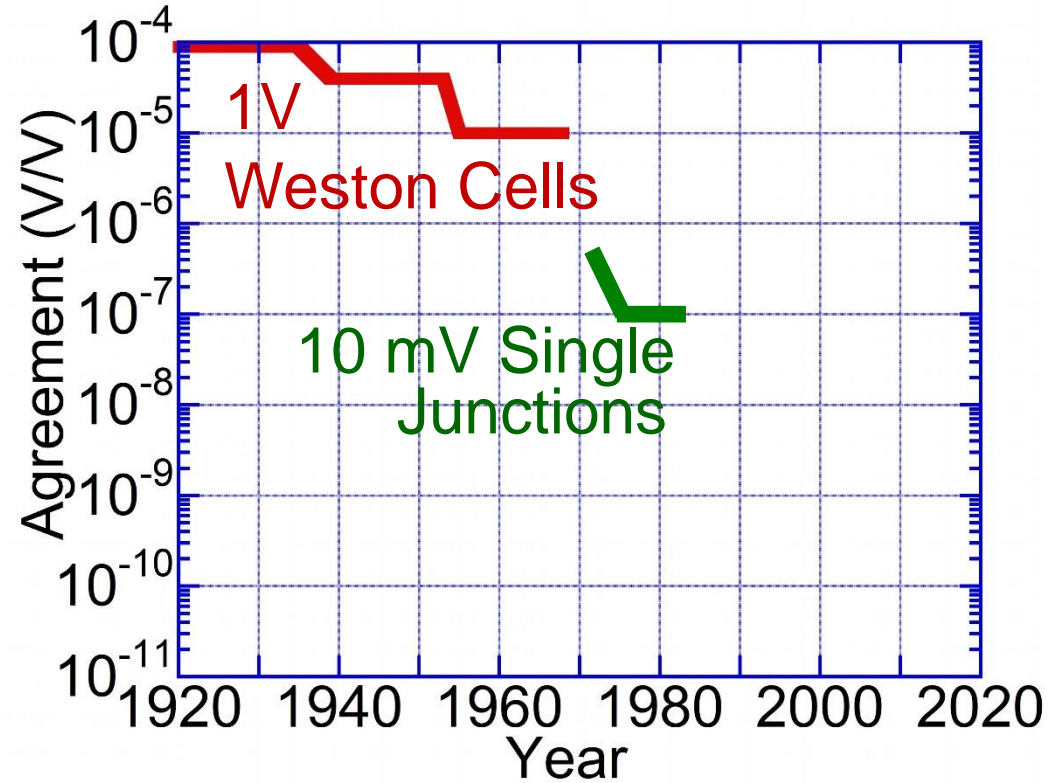
- Josephson Voltage Standard History
  - Junction Development
  - Packaging and system evolution
- Josephson Arbitrary Waveform Synthesizer = **JAWS**
  - Applications
  - Operation
  - Circuit Development
- Making it practically useful for Metrologists
  - Reaching practical voltages above 1 V
  - Pulse generator development
  - Cryogenic integration & System Development
- Extending to Megahertz and Gigahertz Frequencies
  - **VHF JAWS** for power calibration
  - **RF JAWS** for linearity and precise synthesis of arbitrary waveforms



# DC Voltage Artifact Standards Replaced by Josephson Standards



Electrochemical Battery  
CdHg Weston Cell  
Vary in time & with  
environmental  
conditions



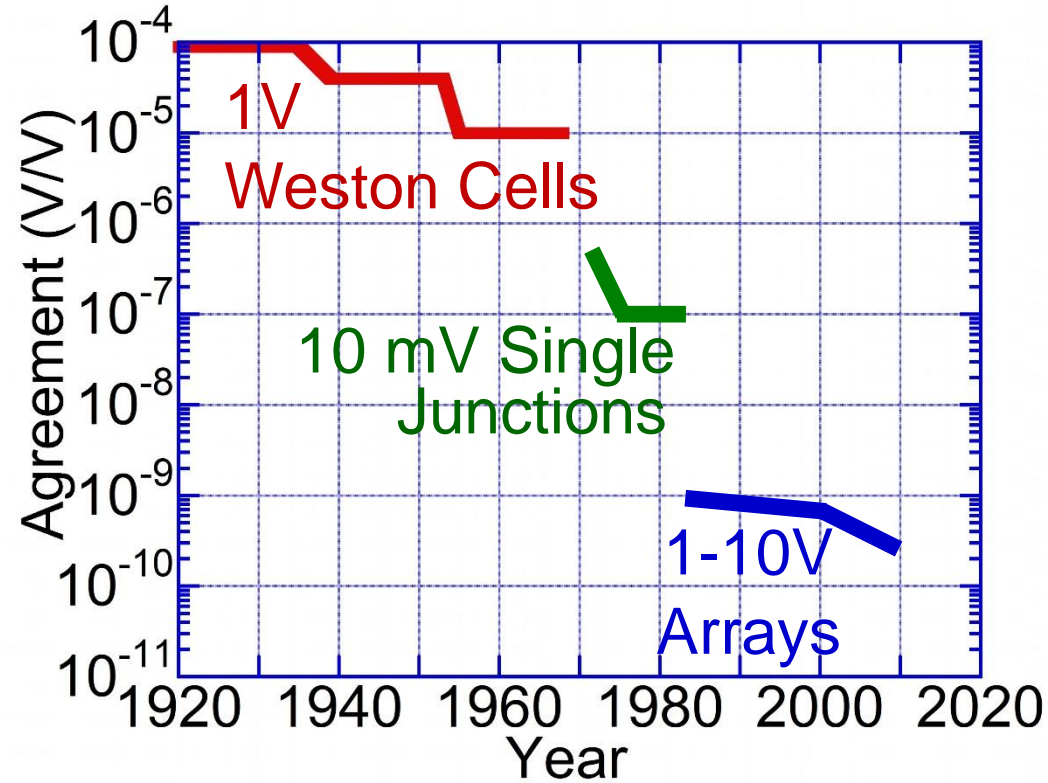
Single Josephson  
Junctions

Intrinsically accurate  
& based on  
quantum effects

# DC Voltage Artifact Standards Replaced by Josephson Standards



Electrochemical Battery  
CdHg Weston Cell  
Vary in time & with  
environmental  
conditions



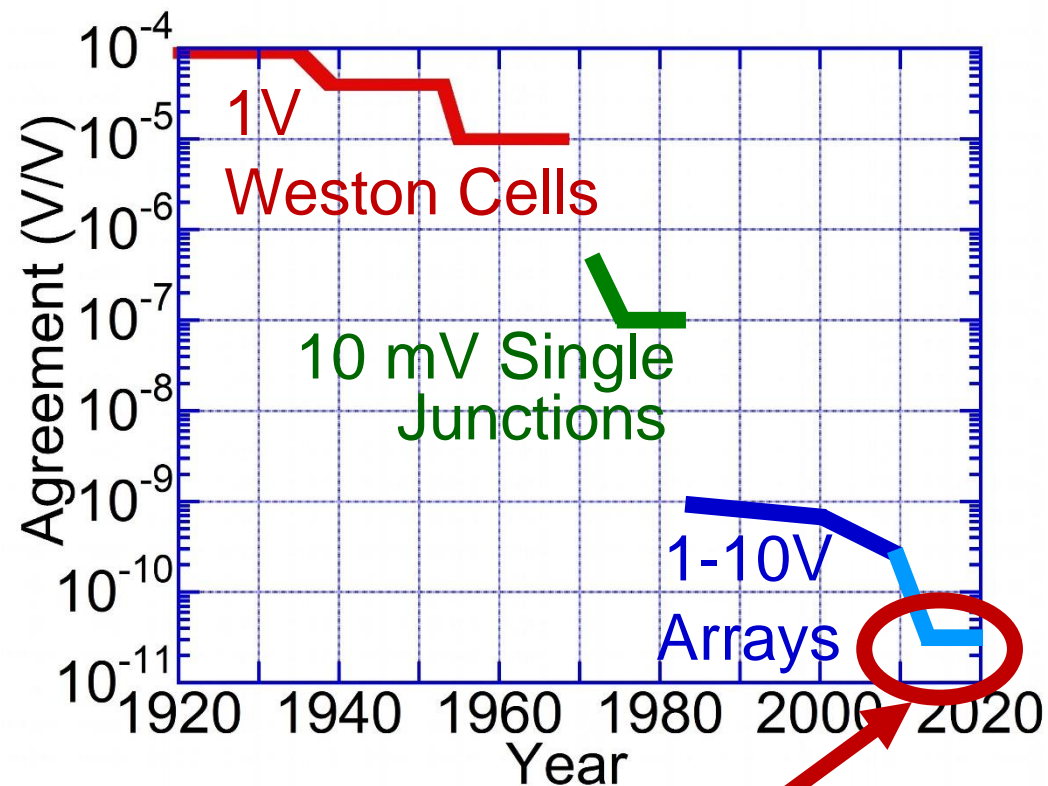
Conventional JVS  
Intrinsically accurate  
& based on  
quantum effects



# DC Voltage Artifact Standards Replaced by Josephson Standards



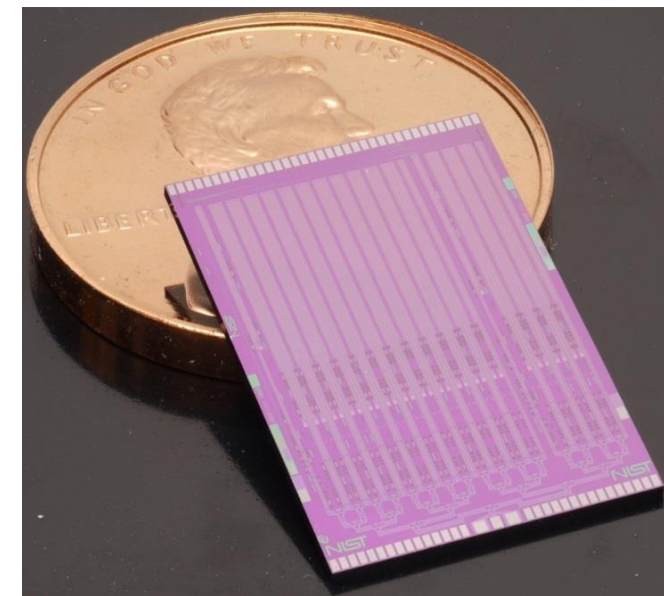
Electrochemical Battery  
CdHg Weston Cell  
Vary in time & with  
environmental  
conditions



**PJVS DC to DC**

**comparison:  $3 \times 10^{-11}$**

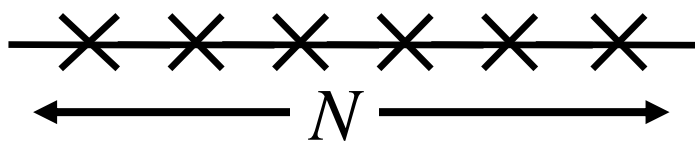
A Rüfenacht, et al., Metrologia vol. 55,  
no. 5, pp. S152–S173, July 6, 2018



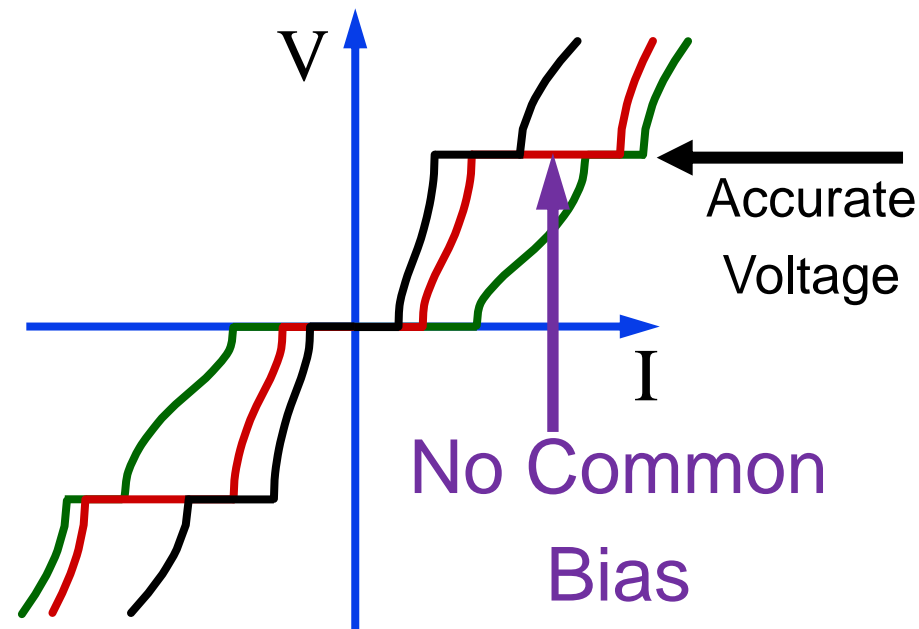
Programmable JVS  
Intrinsically accurate  
& based on  
quantum effects

# Practical Voltages Require Series Arrays

- $h/2e$  is SMALL  $\approx 2 \mu\text{V}/\text{GHz}$ 
  - 20 GHz produces  $\approx 40 \mu\text{V}$  steps
- 10 V is the desired output voltage
  - Large series arrays are required



$$V_{n,N} = \frac{h}{2e} nNf$$

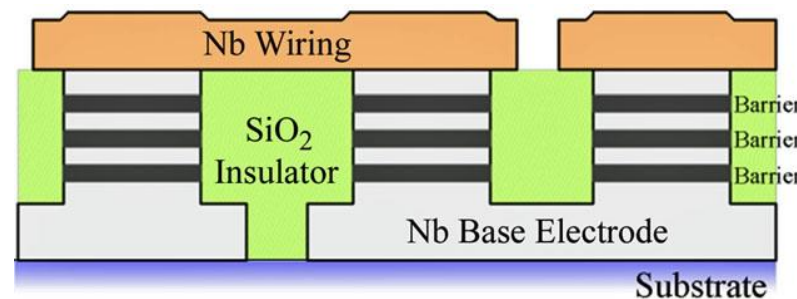
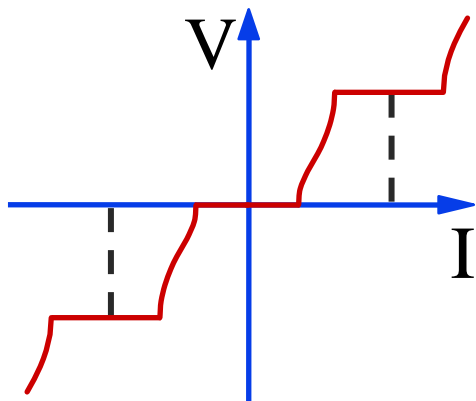


- Common bias requires
  - Uniform junctions
  - Uniform microwave power

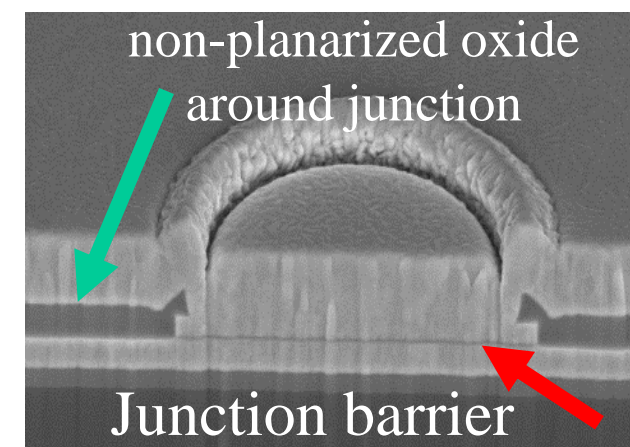
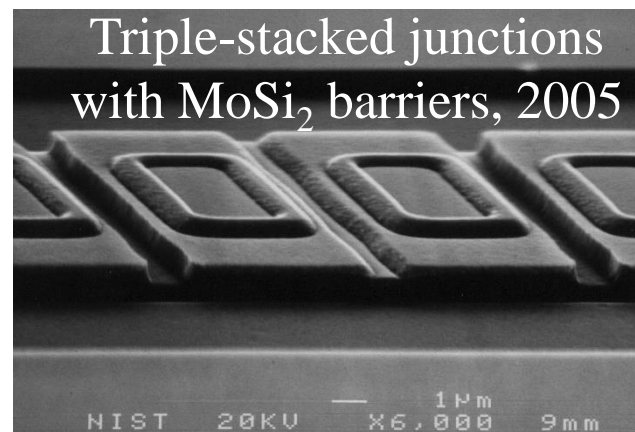
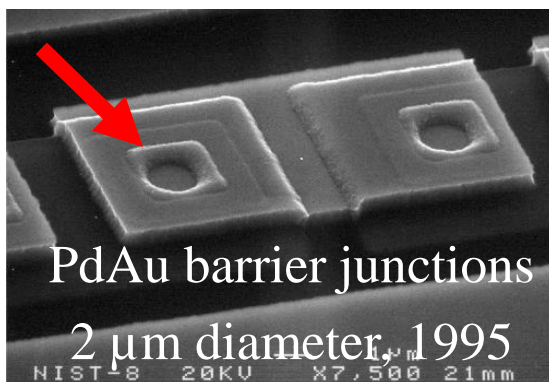
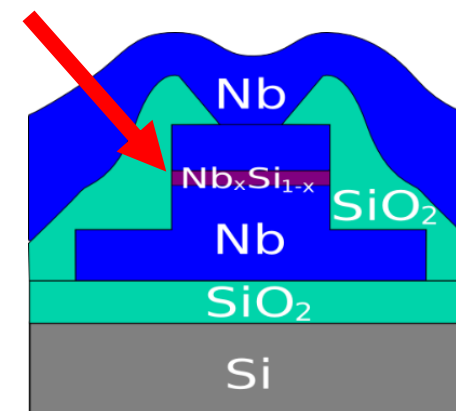
Practical voltages require  
long arrays of uniform junctions  
& excellent microwave designs



# Damped-Junction Development



$\text{Nb}_x\text{Si}_{1-x}$  Barriers



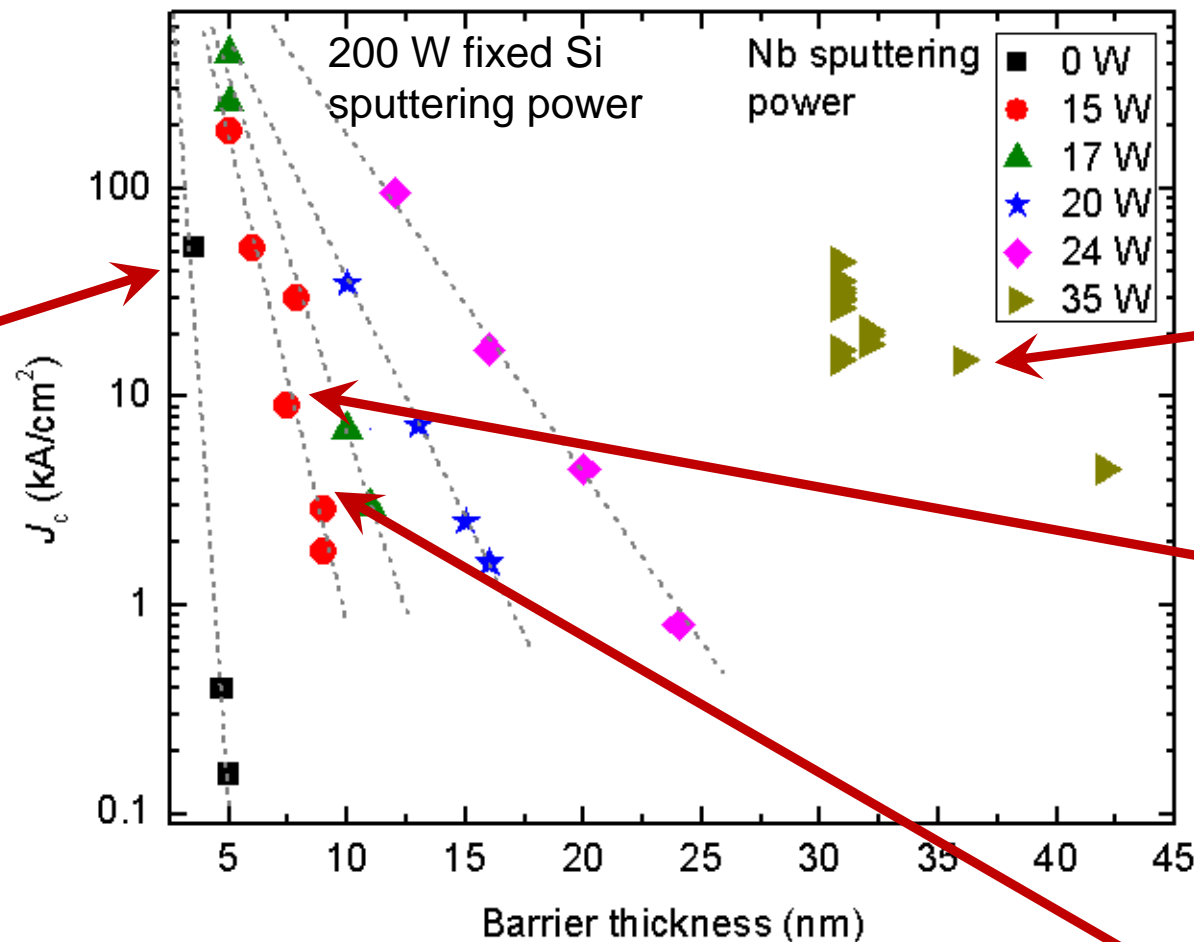
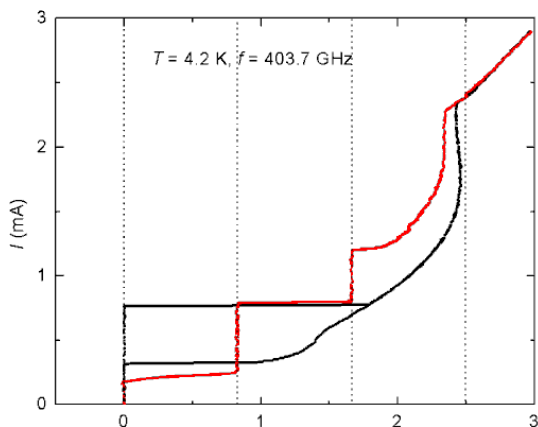
# Tunable $\text{Nb}_x\text{-Si}_{1-x}$ Barriers for Many Applications

400 GHz FIR optically driven JJ

9 W Nb power,  $d = 4.6$  nm

$I_c R_n = 1$  mV

$J_c = 13$  kA/cm<sup>2</sup>



15-20 GHz pulse-ACJVS & PJVS

$x = 0.15$ ,  $d = 35$  nm

$\rho_{4.2K} = 1$  m $\Omega$  cm

$I_c R_n = 30$   $\mu$ V

$J_c = 11$  kA/cm<sup>2</sup>

170 GHz Digital circuits

15-16 W Nb power,  $d = 10$  nm

$I_c R_n = 100$ -130  $\mu$ V

$J_c = 5.5$  kA/cm<sup>2</sup>

70 GHz NIST/PTB 10V PJVS

$x = 0.08$ ,  $d = 11$  nm

$\rho_{4.2K} = 700$  m $\Omega$  cm

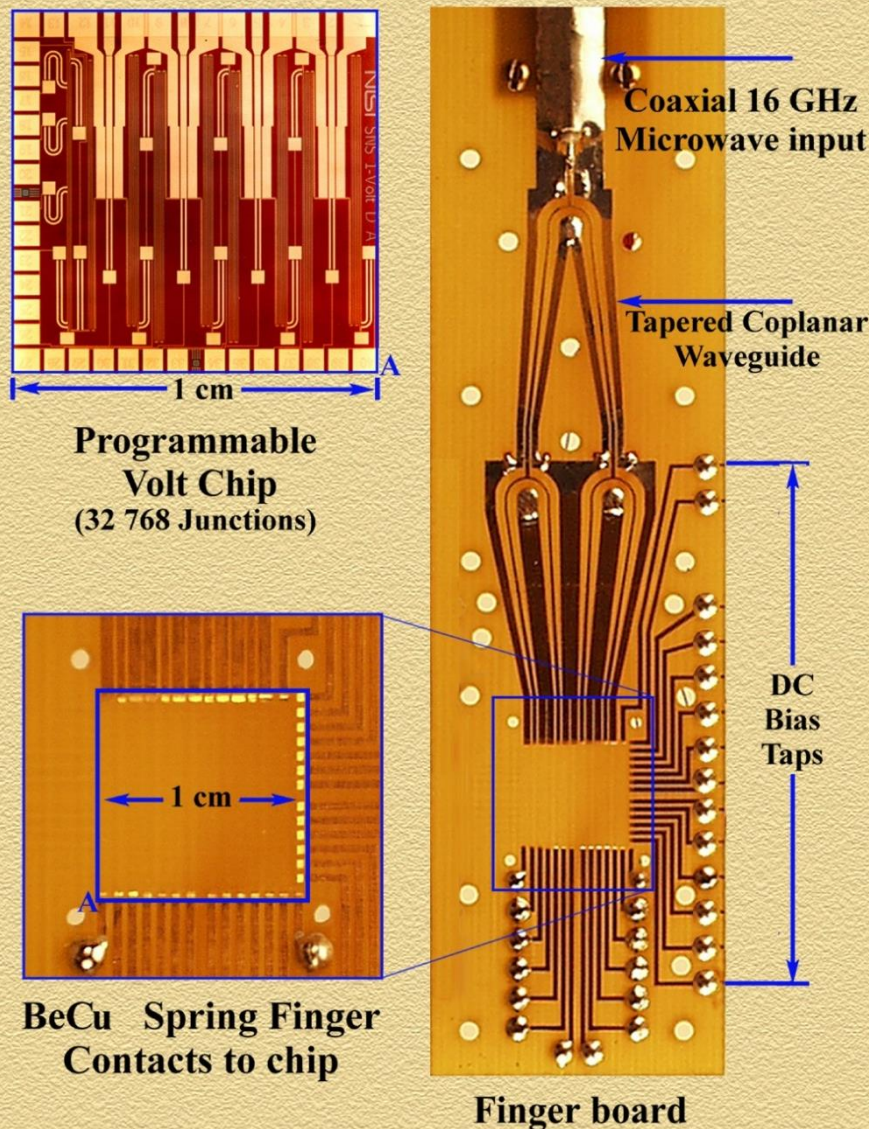
$I_c R_n = 150$   $\mu$ V

$J_c = 2.5$  kA/cm<sup>2</sup>

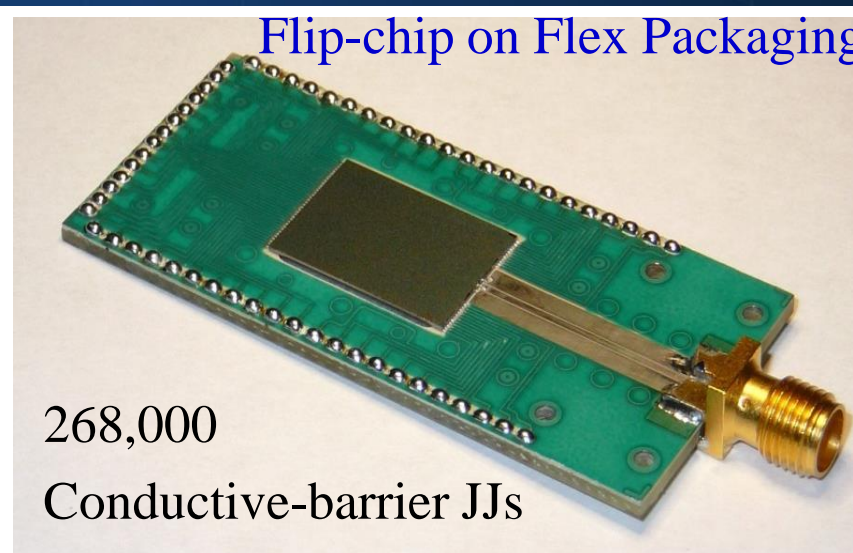


# Packaging of Josephson Voltage Standards

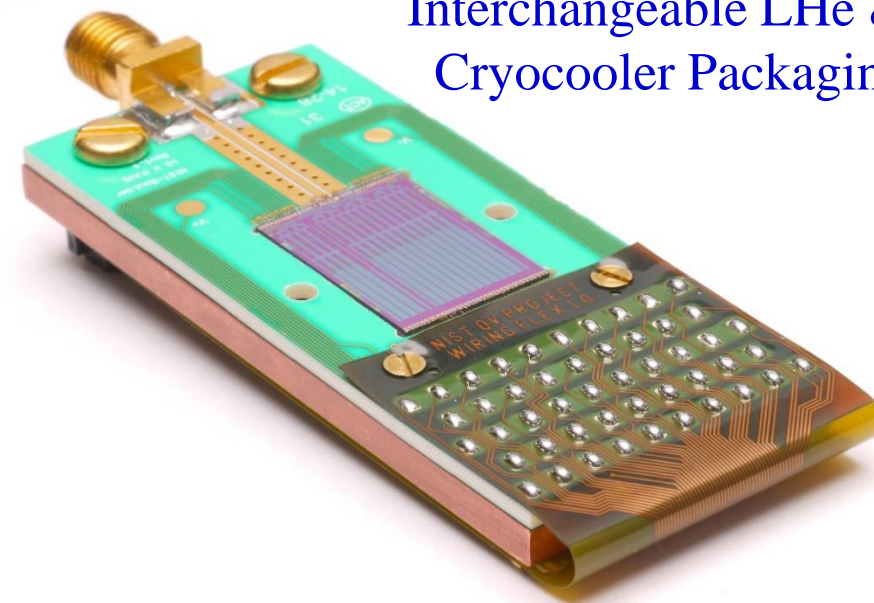
## Microwave and DC Bias Circuit



## Flip-chip on Flex Packaging



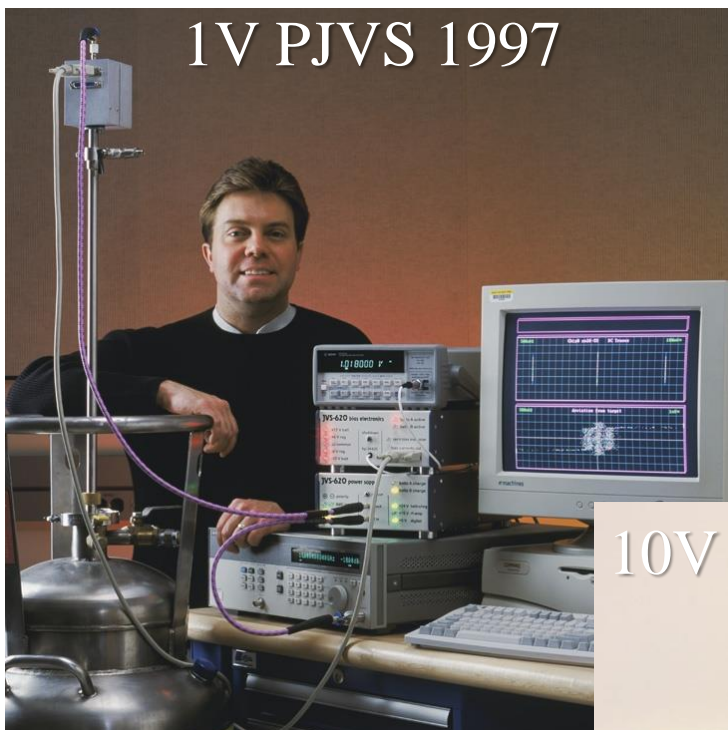
## Interchangeable LHe & Cryocooler Packaging





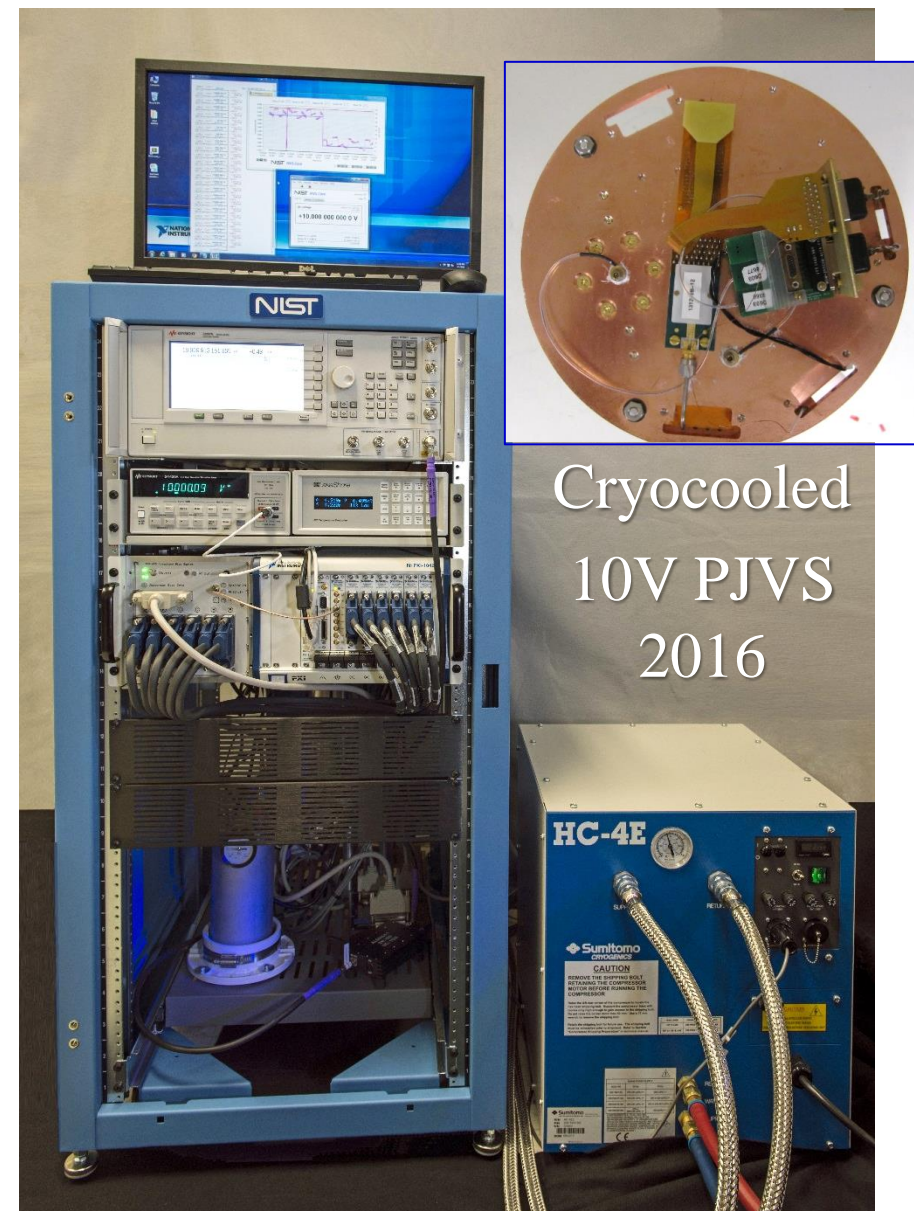
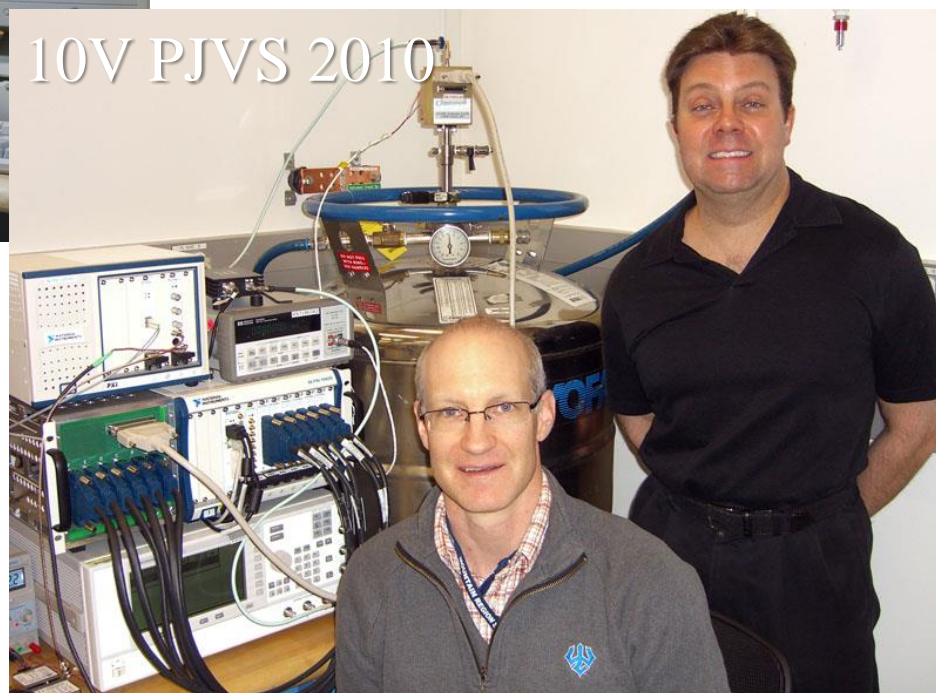
# PJVS System Development

1V PJVS 1997



- Goal: COTS Parts
- Full automation
  - Quantum Operation
  - Applications
- No Liquid Helium

10V PJVS 2010



Cryocooled  
10V PJVS  
2016



The prices listed below are for the individual instrument and do not include costs related to the final measurement calibration performed before delivery or post-delivery installation and training. The related Calibration Service ID for the SRI is [68000S](#). To obtain a quote for the instrument and calibration services, please contact Sales and Customer Service by phone at 301-975-2200 or email at [srminfo@nist.gov](mailto:srminfo@nist.gov).

6000e	Cryo-cooled 10V PJVS, with water-cooled compressor	\$332,900
6000h	Cryo-cooled 10V PJVS, with water-cooled compressor, without synthesizer	\$329,100
6000i	Cryo-cooled 10V PJVS, with air-cooled compressor	\$338,000
6000l	Cryo-cooled 10V PJVS, with air-cooled compressor, without synthesizer	\$334,100
6000m	Cryopackaged 10V PJVS chip	\$56,900
6000n	Cryopackaged 2V PJVS chip	\$29,900
6000f	Cryo-cooled 10V PJVS, with water-cooled compressor (US GSA Authorized)	Superseded by SRI 6000e
6000j	Cryo-cooled 10V PJVS, with air-cooled compressor (US GSA Authorized)	Superseded by SRI 6000i
6000o	Upgrade existing NIST-installed Liquid-helium-cooled PJVS to Cryocooler with water-cooled compressor	Superseded by 6000h
6000p	Upgrade existing NIST-installed Liquid-helium-cooled PJVS to Cryocooler with air-cooled compressor	Superseded by 6000i

## SRI 6000 Series Programmable Josephson Voltage Standard (PJVS)

Technical Contact: [Paul Dresselhaus](#)

The Programmable Josephson voltage standard (PJVS) is an instrument that generates stable, quantum-accurate, direct-current (DC) voltages that are programmable over the range from -10 volts to +10 volts. The quantum accuracy of these voltages is derived from the Josephson Effect such that every superconducting Josephson junction in the PJVS circuit produces a voltage precisely proportional to the frequency of the applied microwave bias signal.

The PJVS with its quantum accurate dc voltages can serve as a primary voltage standard with accuracy of parts in  $10^{10}$  (determined through intercomparison with another quantum voltage standard) or as a stable, programmable source for precision measurements, metrology experiments or calibrations. For example, the PJVS can be used to calibrate Zener references (typically parts in  $10^7$  depending on the measurement instruments and Zener noise) as well as the amplitude-dependent gain and linearity of digital voltage meters.

The PJVS is also capable of generating stepwise-approximated waveforms or sine waves with a rise time between voltage steps that is less than 2 microseconds. The AC voltage of the stepwise waveforms do not have quantum accuracy because the transitions between the steps are bias dependent. A differential-sampling measurement technique with an integrating sampling digital voltmeter is used with the step-wise waveforms to calibrate the ac voltage of commercial voltage calibration sources at frequencies up to a few hundred hertz with a typical measurement uncertainty of parts in  $10^7$ , depending on the phase and amplitude stability of the source.





# Josephson Arbitrary Waveform Synthesizer JAWS for Audio Frequency AC Voltage Calibrations



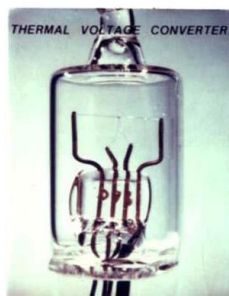
- N E Flowers-Jacobs, et al., “Development and Applications of a Four-Volt Josephson Arbitrary Waveform Synthesizer,” Proceedings of the 2019 ISEC, 28 July-1 Aug. 2019, Riverside, CA, USA
- N E Flowers-Jacobs, et al., “Calibration of an AC Voltage Source Using a Josephson Arbitrary Waveform Synthesizer at 4 V,” 32<sup>st</sup> CPEM 2020 Digest, Aug. 24 - 28, 2020, Denver, CO.



# AC Voltage & RF Standards and Instruments

## Audio Frequency Thermal Converters

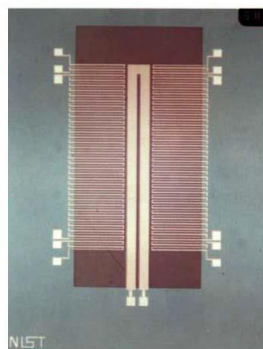
Thermal Converter



1 cm

Few ppm

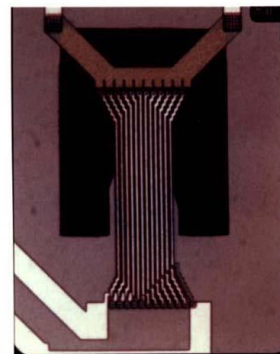
Multijunction Thermal Converter



2 mm

Sub ppm

CMOS Compatible Thermal Converter

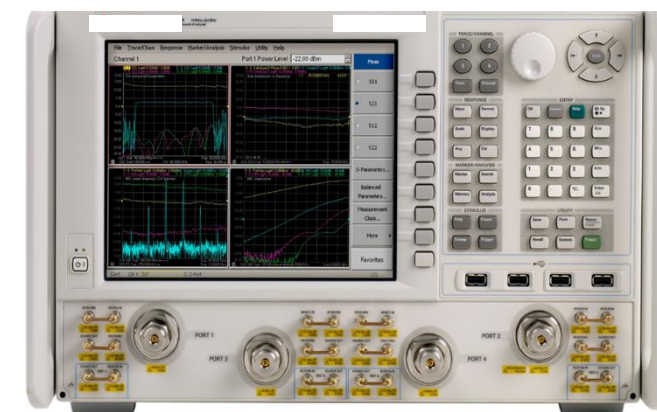


200  $\mu$ m

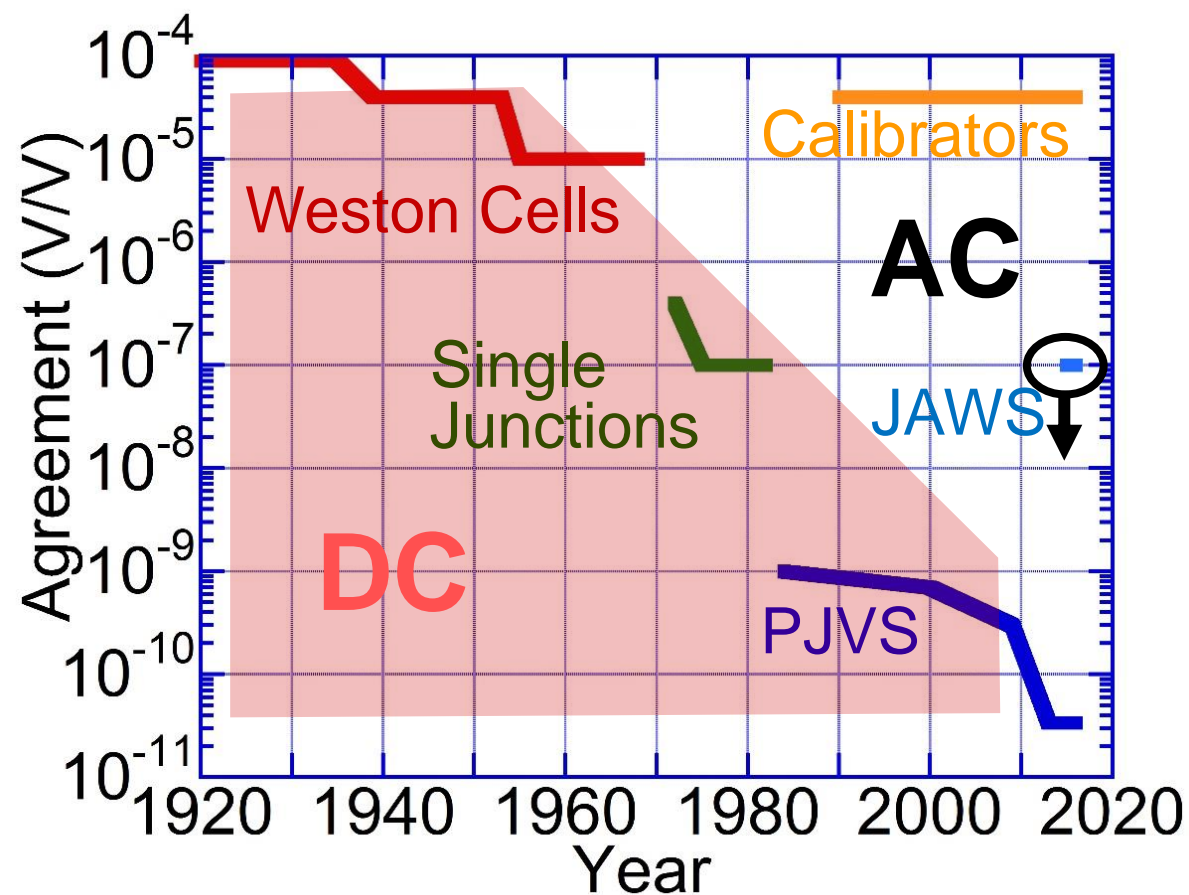
Few Tens of ppm



## RF Power Meters, Analyzers & Amplifiers



# Complement Voltage Calibrators with JAWS Sources



Statistical uncertainty below  $10^{-7}$  for 1 V JAWS intercomparison

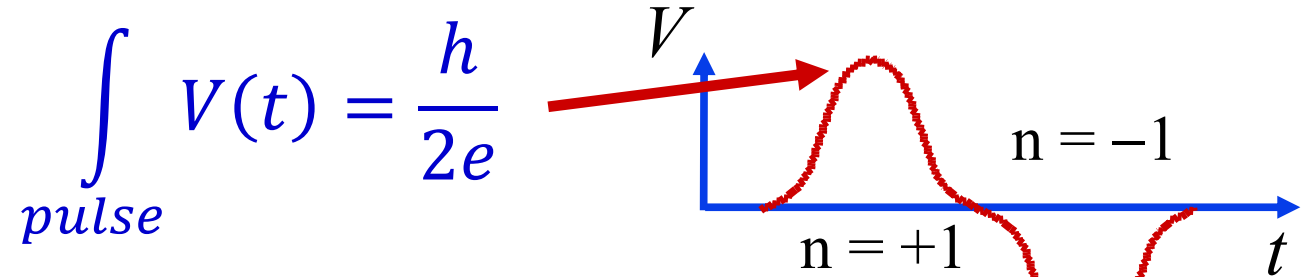


# Josephson Arbitrary Waveform Synthesizer

Co-invented in 1995 by NIST & Westinghouse researchers, H. Worsham, J.X. Przybysz, S. Benz, and C. Hamilton

- Synthesized voltage SOURCE

- Pulse-driven AC Josephson Voltage Standard
- Josephson DAC
- Perfectly quantized JJ pulse areas

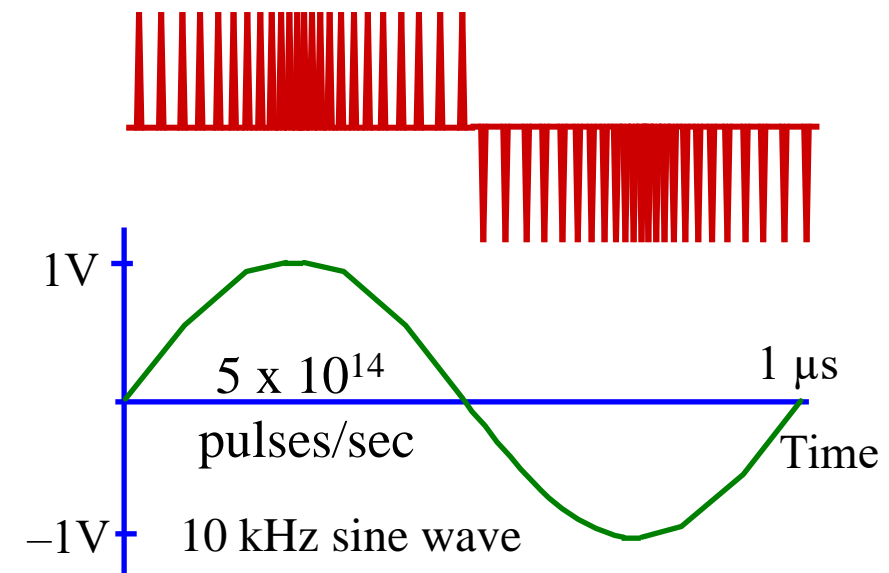


- Directly control every JJ pulse

- Digital signal provided by high-speed bitstream generator (or AWG)

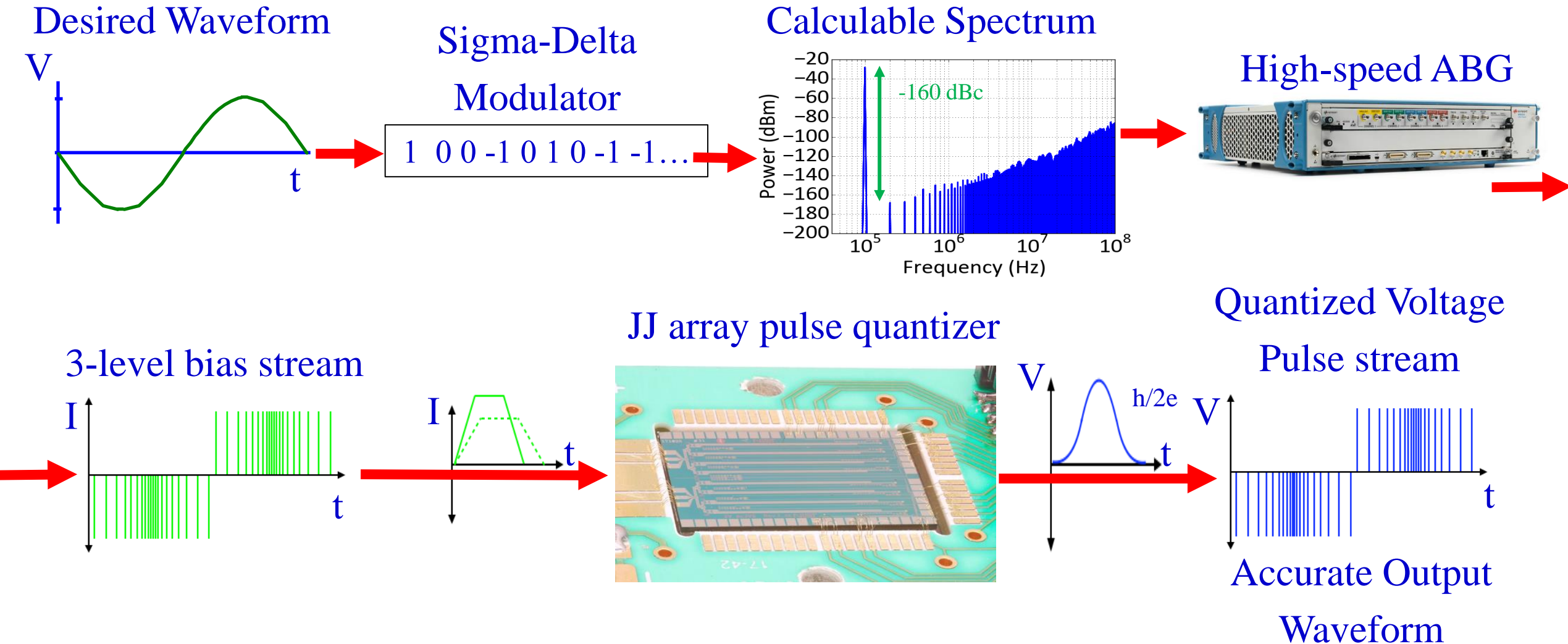
- Arbitrary waveform synthesis

- Timing, placement and polarity of pulses precisely determines the voltage waveform
- Accuracy ensured



# Quantized Pulses Enable Accurate Waveform Synthesis

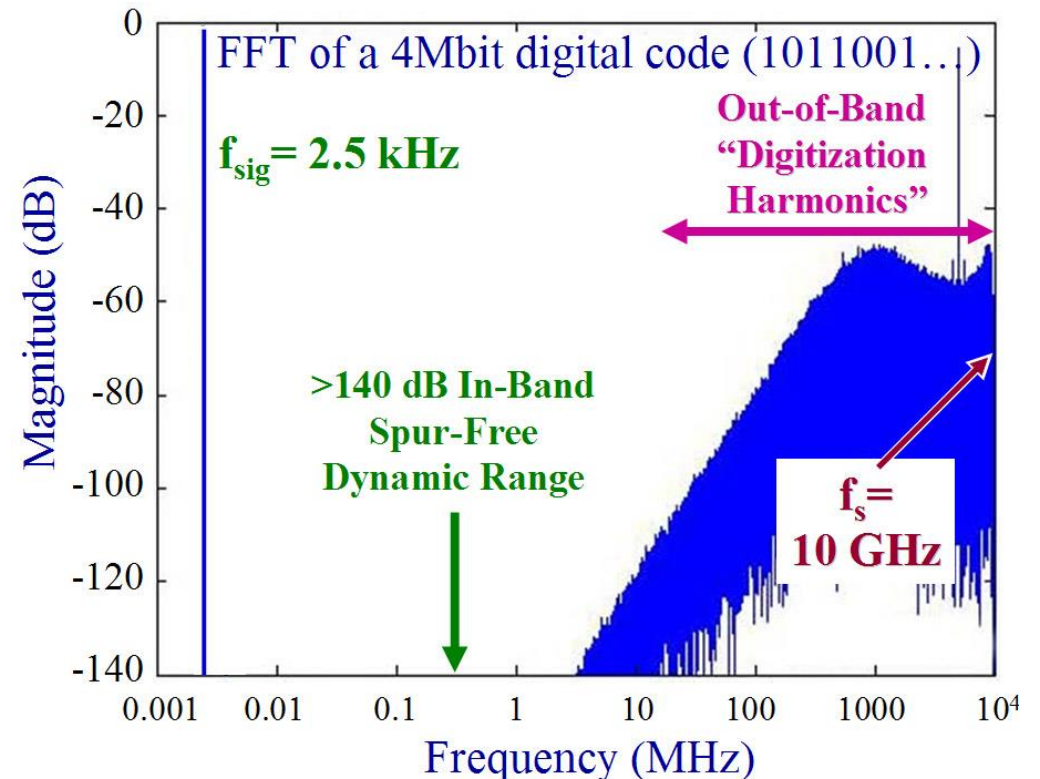
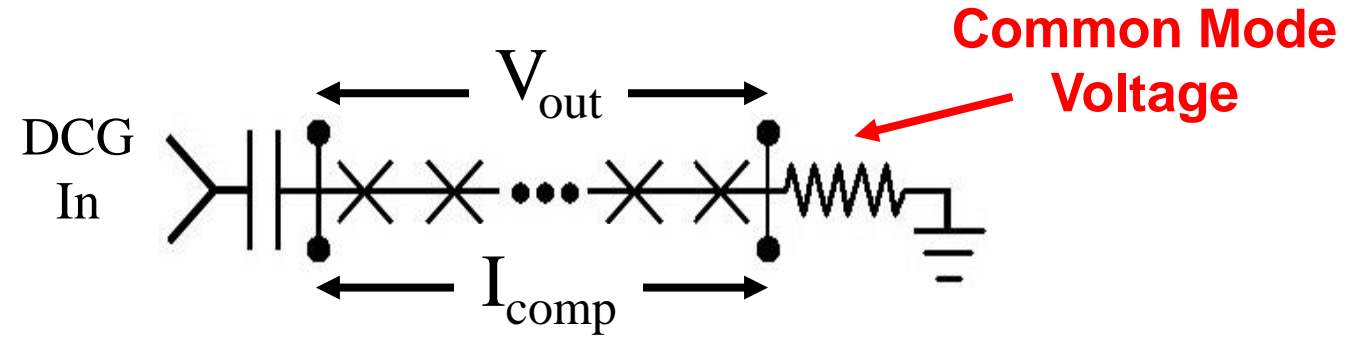
## Josephson Arbitrary Waveform Synthesizer (JAWS)





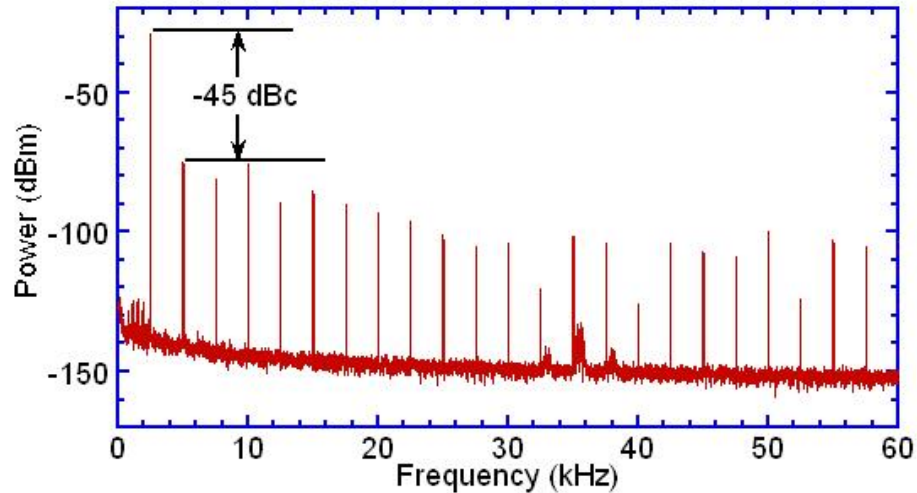
# JAWS Circuit Challenges

- Junction dissipation limits array length
- ABG drive has a signal at the same synthesized frequency
  - 50  $\Omega$  microwave termination
  - Output voltage is NOT referenced to ground
  - Multiple arrays cannot be connected in series
  - Inductance between the JJs creates error signals
- Solution: AC coupled bias
  - DC Blocking capacitors
  - Compensation current  $I_{\text{comp}}$
  - Zero-compensation pulses biasing

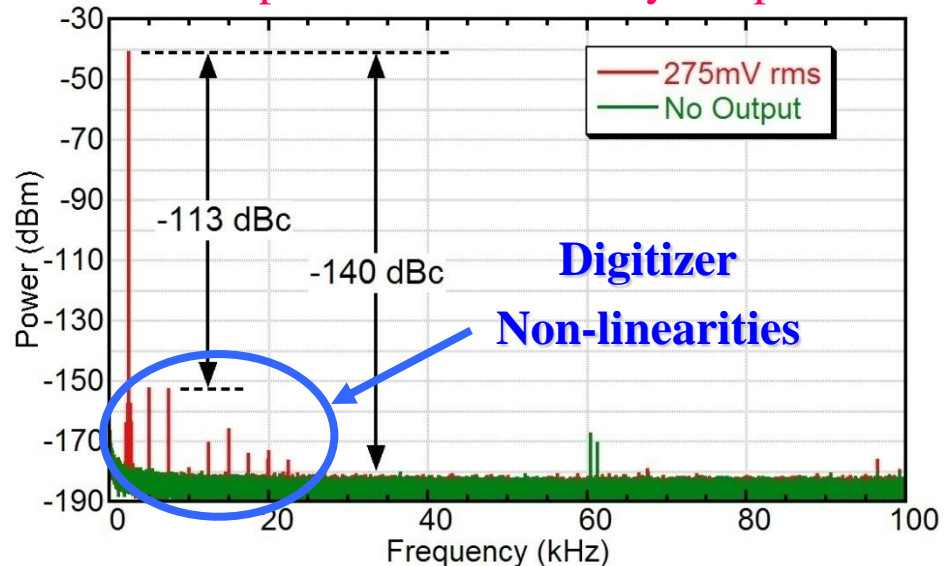


# Bitstream Generator Limitations

## Semiconductor Code Generator Output



## Josephson Junction Array Output



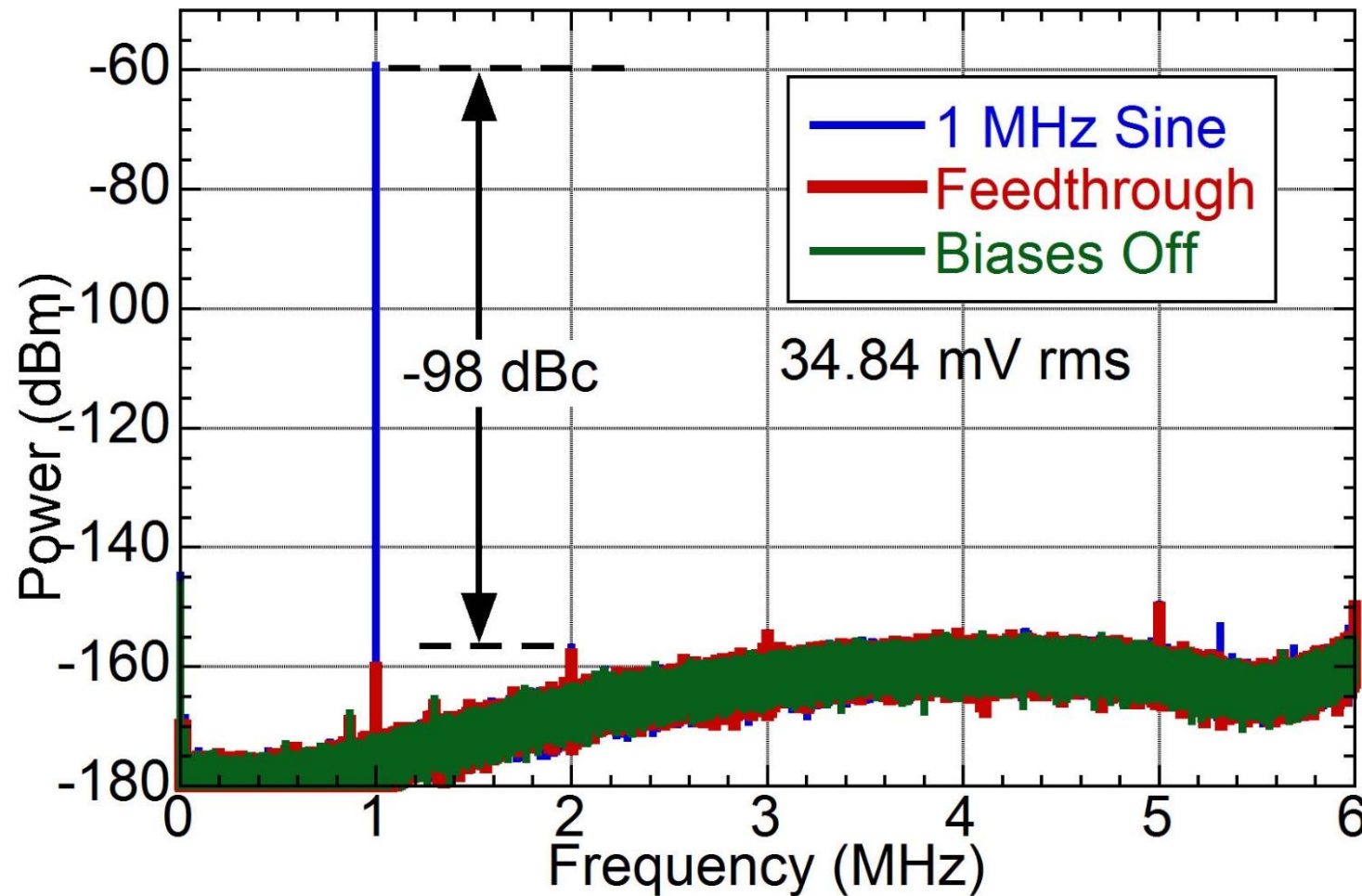
- Sine Wave Synthesis
  - 2.5 kHz tone
  - 4,000,000 bit code length
  - 2-level output, NOT 3-level
  - 15 GHz sine, 10 GHz clock
- Semiconductor code generator (ABG)
  - **-45 dBc** Harmonic distortion
- 2 ac-coupled arrays in series
  - 10,240 junctions
  - 275 mV rms voltage
  - **-140 dBc** Harmonic distortion (to measured noise)

Perfect quantization produces intrinsically accurate waveforms



# 1 V RMS Voltage & Feedthrough Error

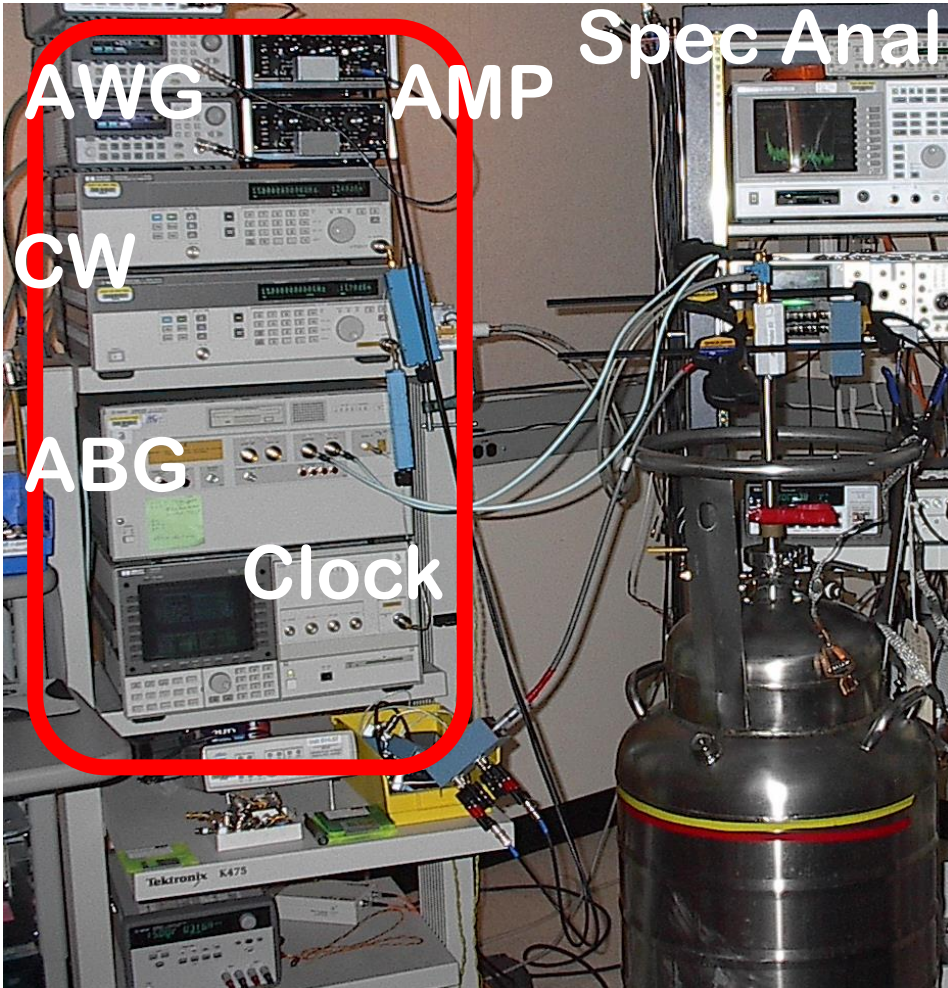
1 MHz sinewave, 1 mA margins, 1 array



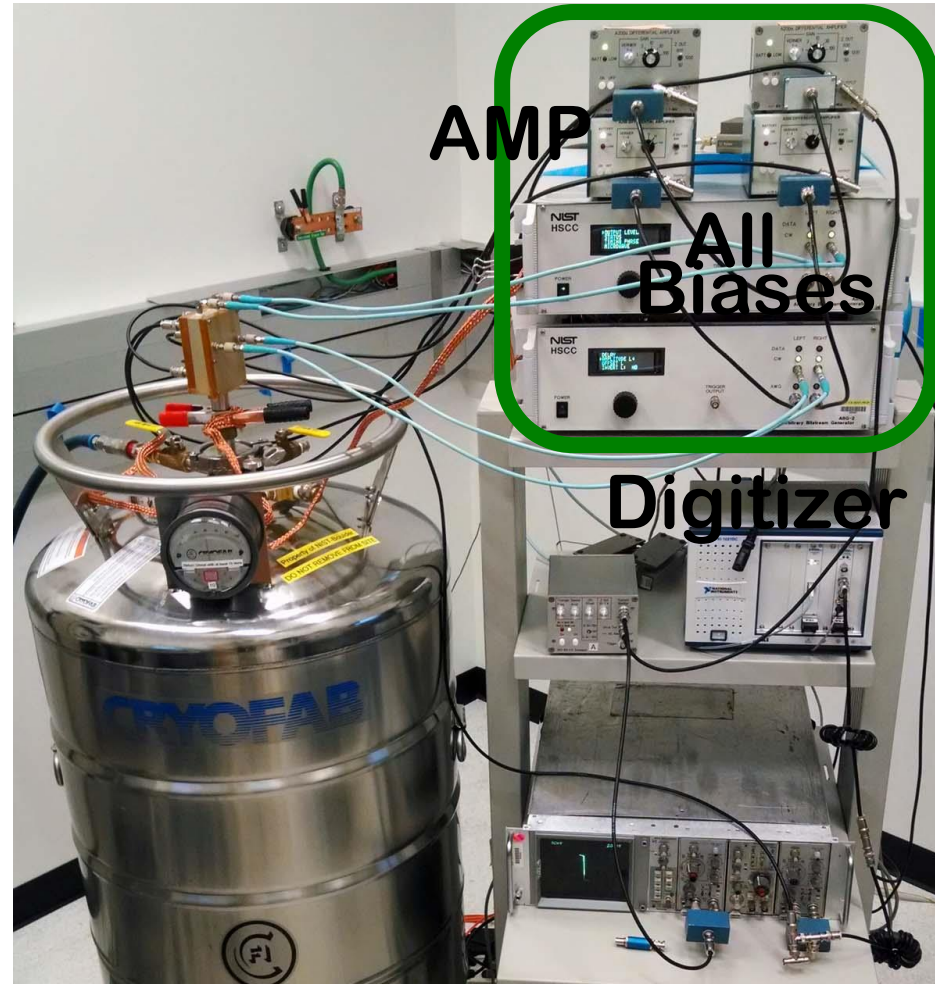


# Compare JAWS Systems

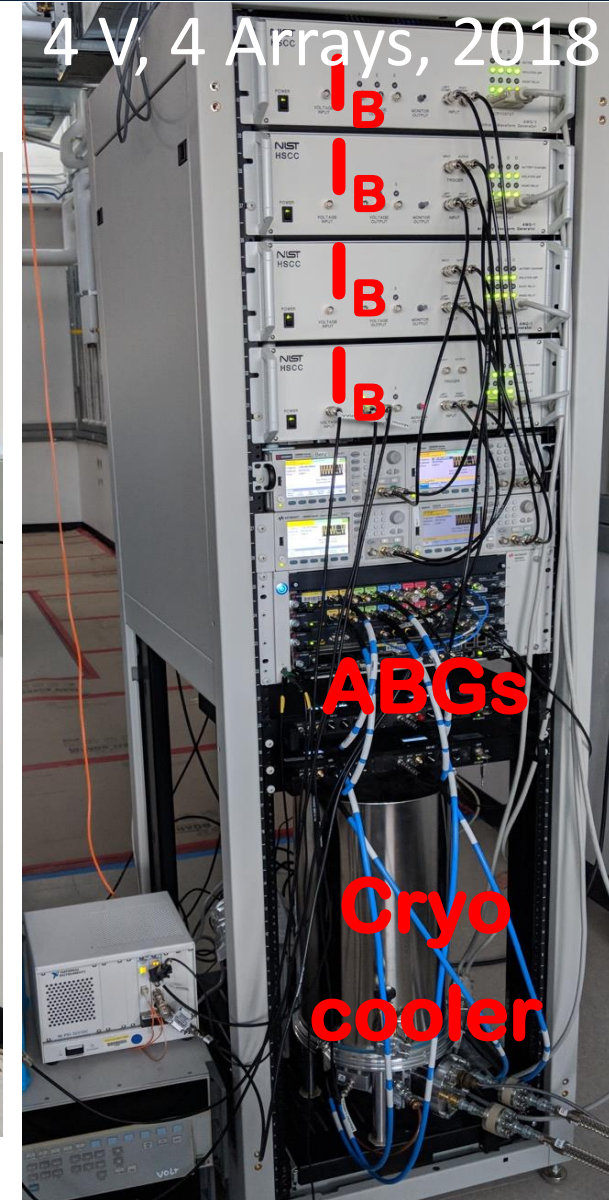
100 mV, 2 Arrays, 2006



1 V, 4 Arrays, 2014



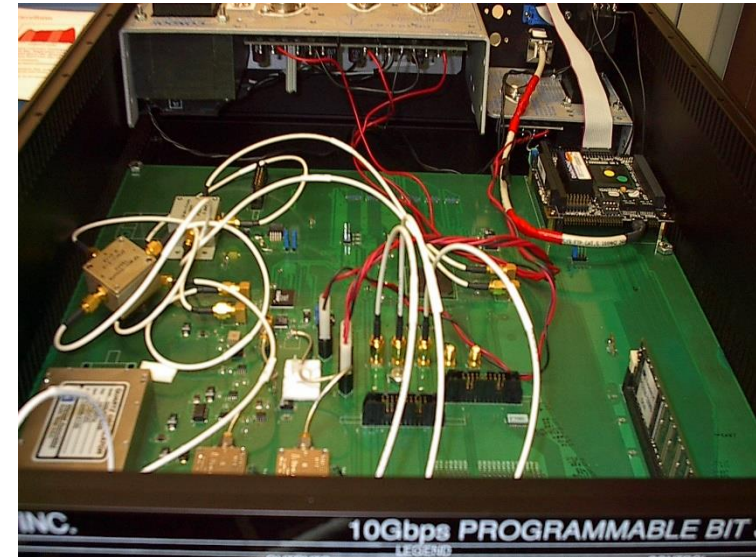
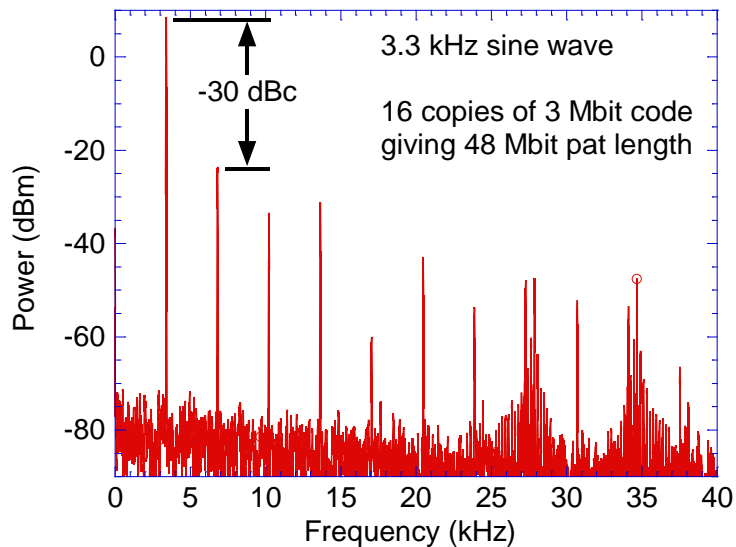
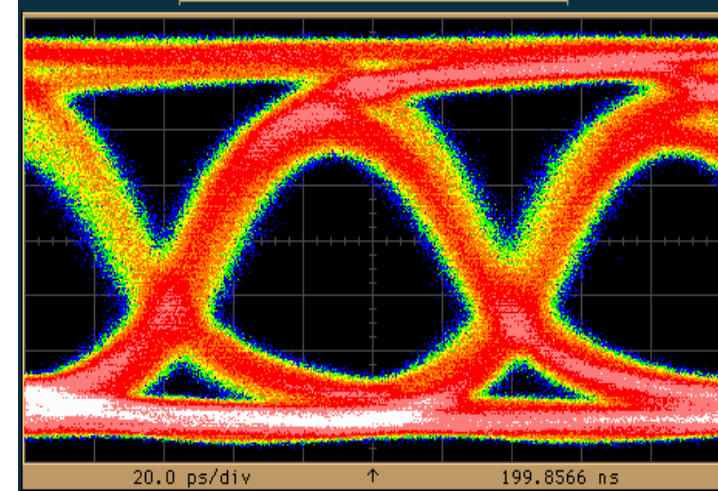
4 V, 4 Arrays, 2018



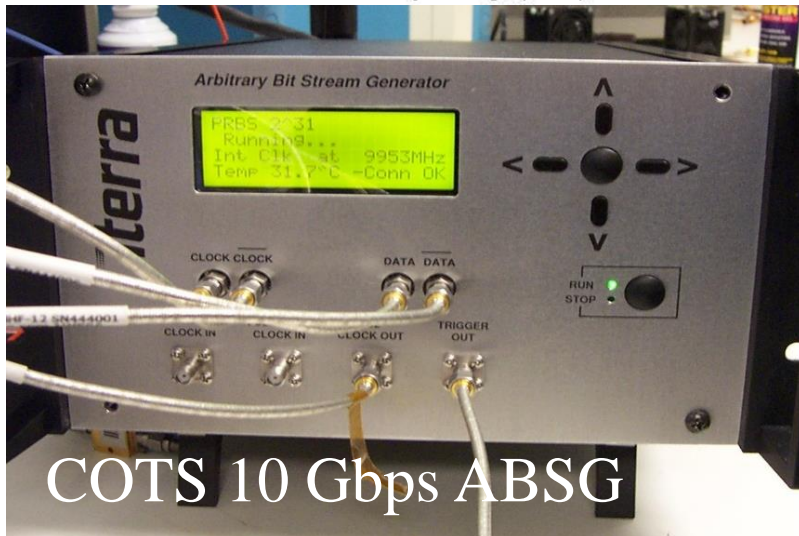
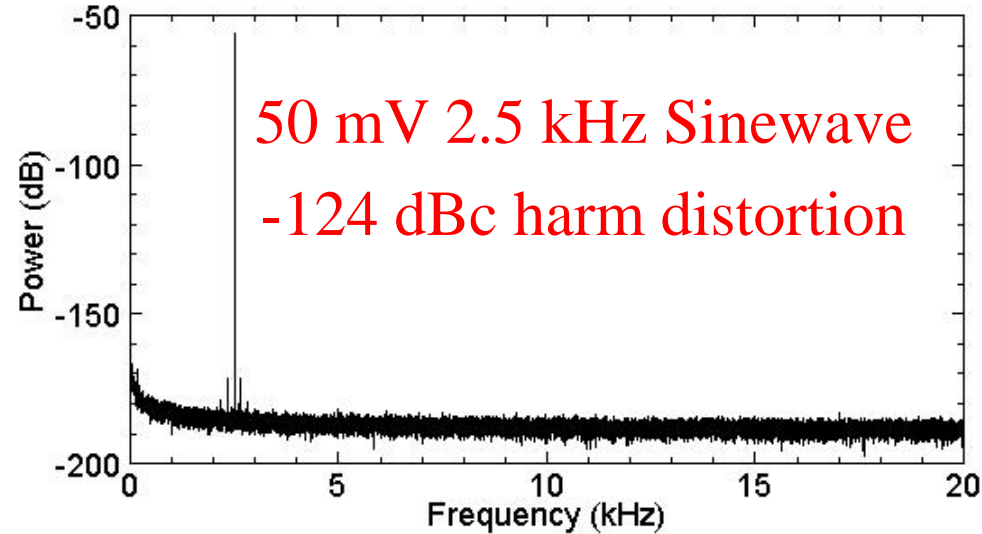


# Advanced Arbitrary Bitstream Generator

- 1000X more memory
  - 1 to 8 Gbit
- Software generation/selection of multiple patterns
- 10X cheaper
  - ~\$40K
- Collaboration with Tao of Digital Inc.



# 2006 ONR Report: Quantum-accurate Waveform Synthesis



With 1 Hz frequency resolution

- NIST is developing more accurate and stable waveform synthesizers.
- Unprecedented and unmatched accuracy and performance are possible only with the quantum properties of superconducting devices.
- Such performance is essential for ac voltage metrology (NIST) and for transmission of high-performance rf and microwave radar and communications (Navy).
- NIST co-invented the pulse-driven Josephson DAC 10 years ago and has spent the intervening period improving the relevant technologies to make it practical.
- This successful program is a direct result of ONR support, namely a COTS 10 Gbps arbitrary bitstream generator that drives the superconducting circuits with high speed pulses and superconducting stacked Josephson junctions to increase the output voltage and operating bandwidth. The complete system technology has become practical in 2005.
- Present systems will directly benefit ac and dc metrology needs of the Navy and have demonstrated quantum-accurate state-of-the-art performance for ac synthesis. Future systems at rf frequencies will improve Navy communications and advanced signal processing.



# HSCC Bipolar 28.8 Gbps ABG

Developed for NIST by High Speed Circuit Consultants

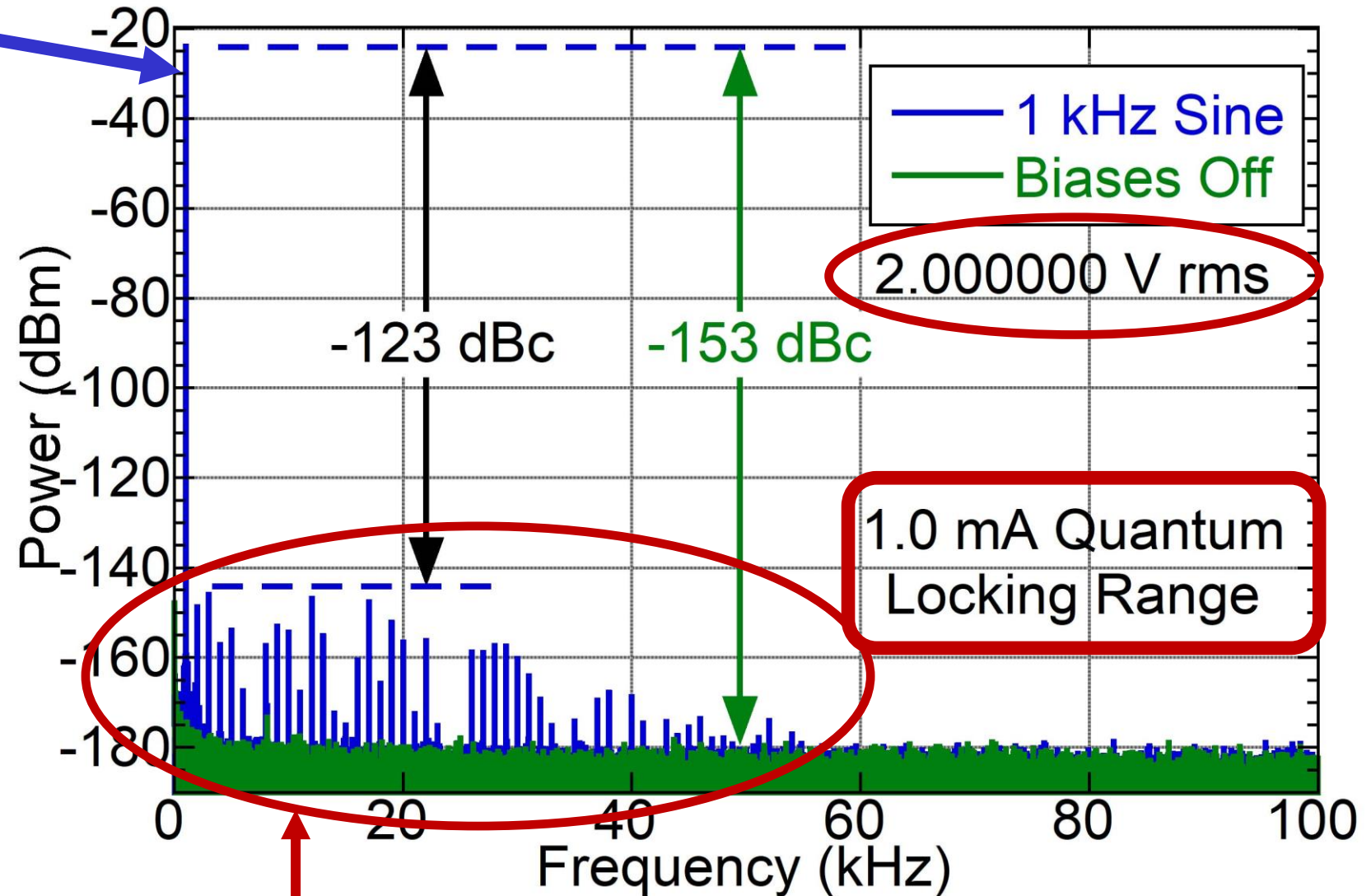
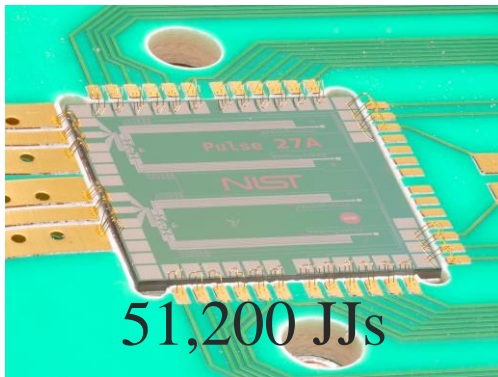
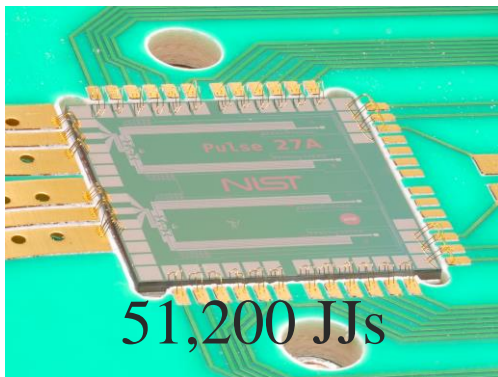


- Advantages of custom ABG
  - 28.8 Gbps is ~3X faster Bipolar Voltage Levels
  - Large 30 Gbit memory size gives 1Hz resolution
  - Integrates all 6 biases for both arrays into one unit
  - One internal 14.4 GHz CW for Quantization
  - Biases remain phase-locked and synchronized



# Josephson Arbitrary Waveform Synthesizer-JAWS

1 kHz 2 V rms Sinewave



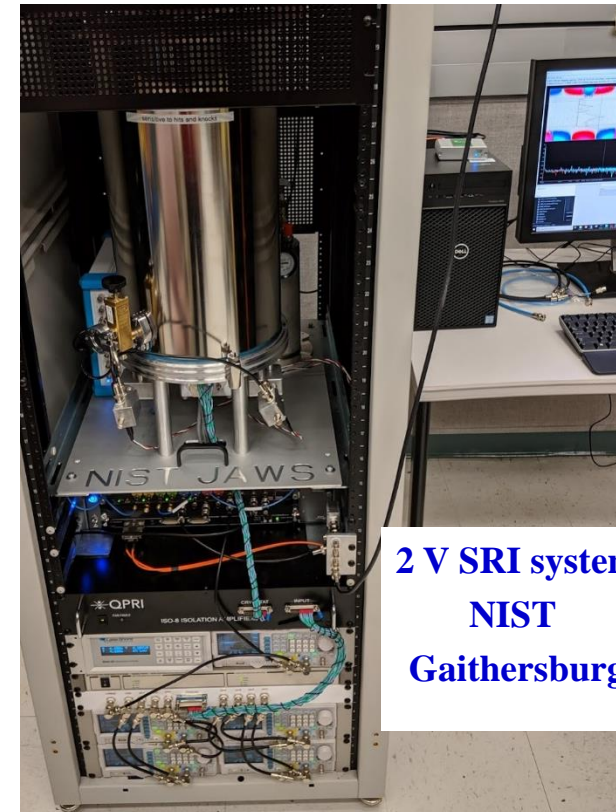
Nathan Flowers-Jacobs et al., IEEE  
Trans. Appl. Supercond., Feb. 2016



# Commercially Available ABG

## Keysight M8195A:

- 8-bit, 64 GSa/s arbitrary bitstream generator
- Operating at 14.4 Gpulses/s
- Integrated finite impulse response (FIR) filter
- Large number of tuning parameters - every sample!



**2 V SRI system  
NIST  
Gaithersburg**

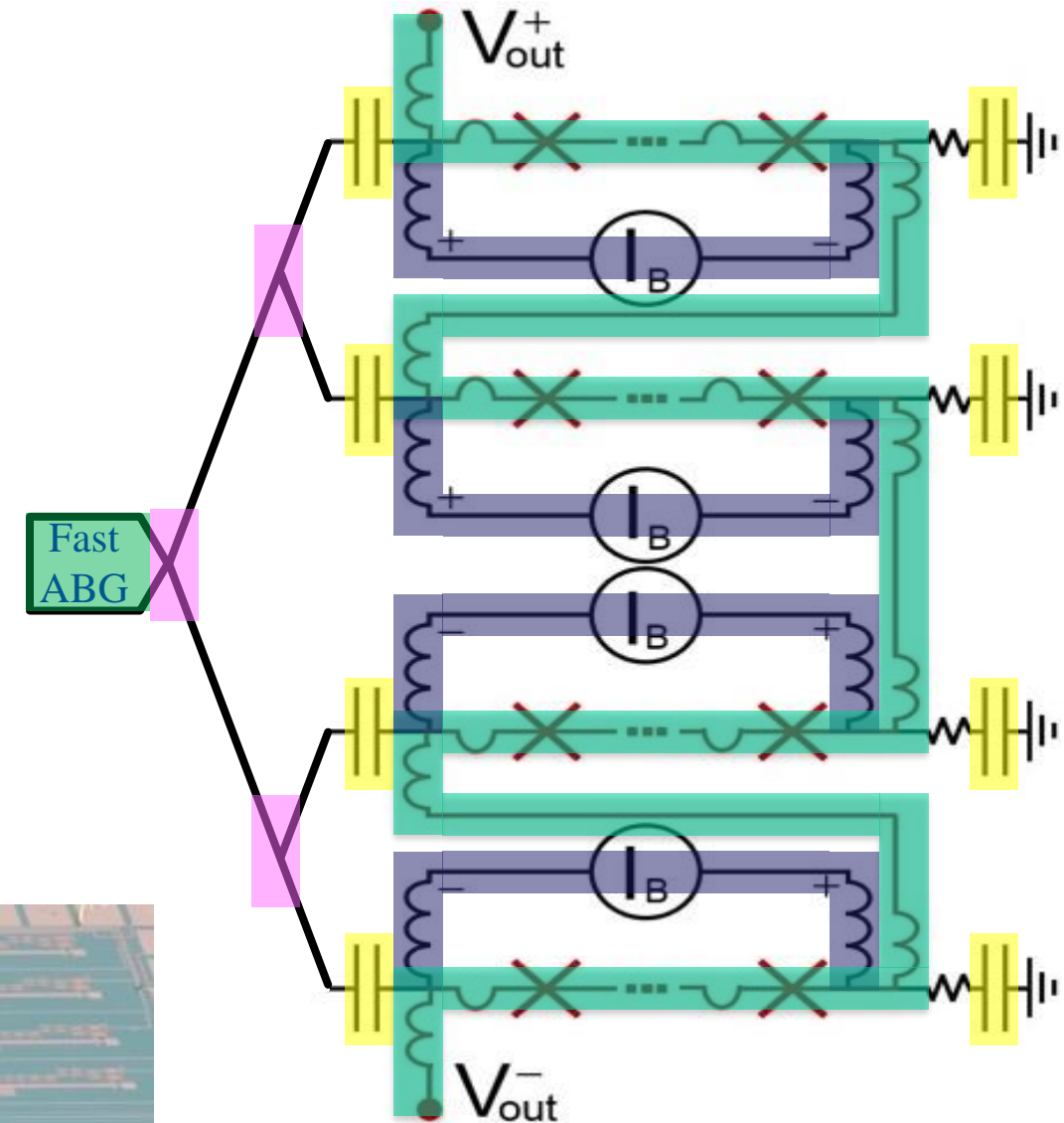
# Improvements: 1 V rms / half-chip

## • Instrumentation upgrade:

- 8-bit, 64 GSa/s arbitrary bitstream generator
- still operating at 14.4 Gpulses/s
- Just ONE pulse generator channel drives this 1V circuit

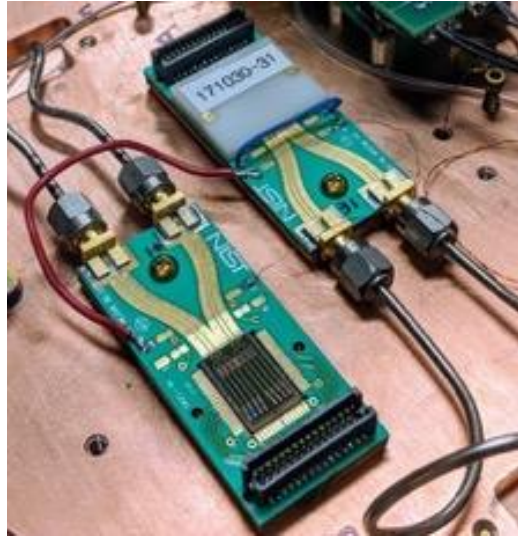
## • Circuit upgrade:

- two layers of on-chip Wilkinson dividers (4-way split)
- Four connected arrays
  - 12 810 JJ/array (51,240 JJs /circuit)
- On-chip dc blocks to add arrays
  - and also filter low-frequencies!
  - need to add it back in:  $I_B$



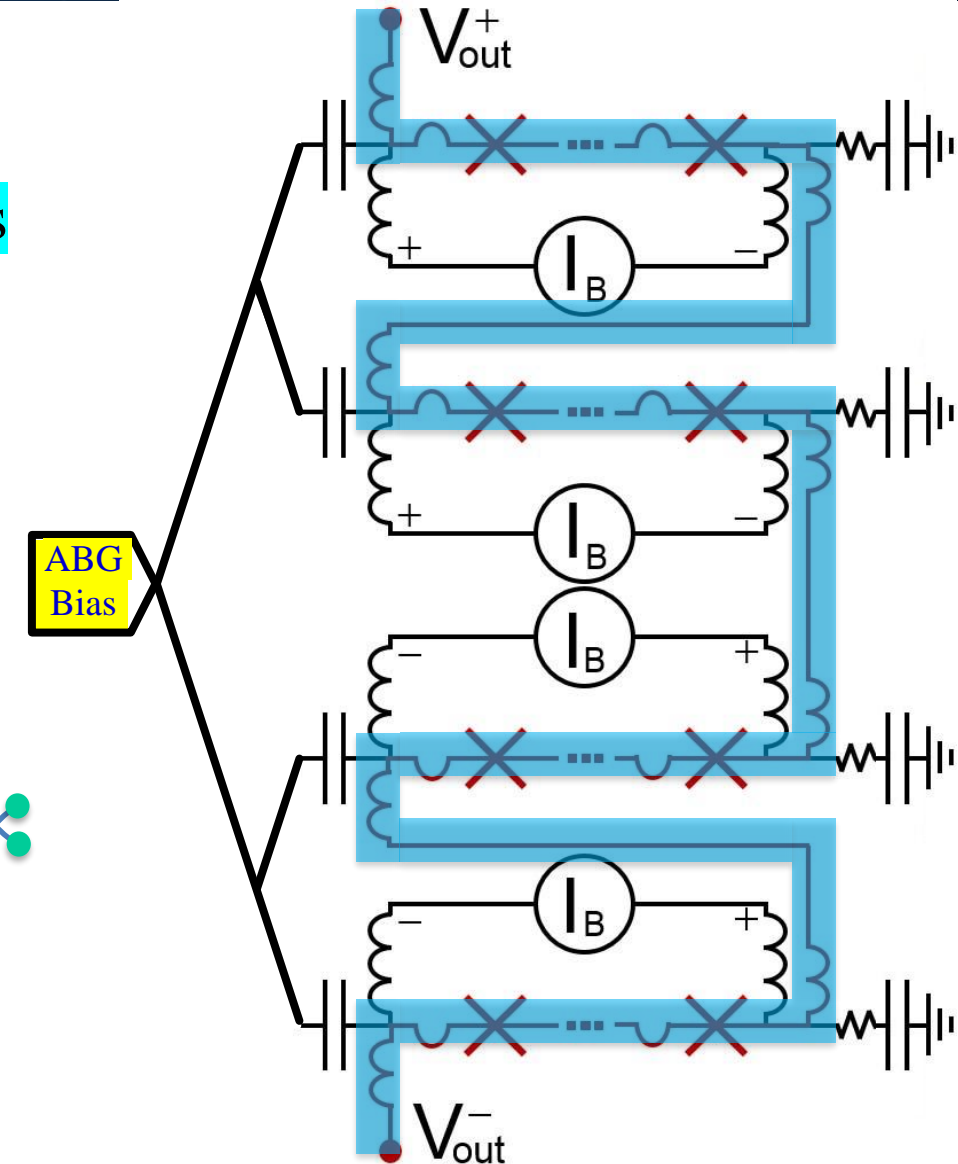
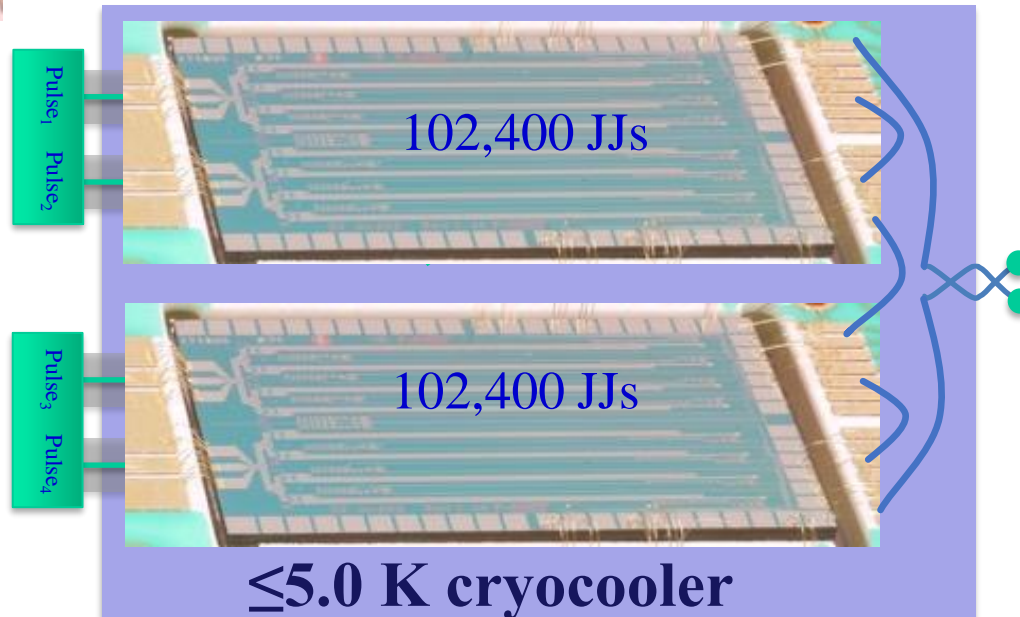


# 4 V rms Cryocooled JAWS



## 2 Cryopackaged Chips

- Four series-connected arrays
- 204,960 total JJs
- One pulse generator bias
- 14.4 Gpulses/sec

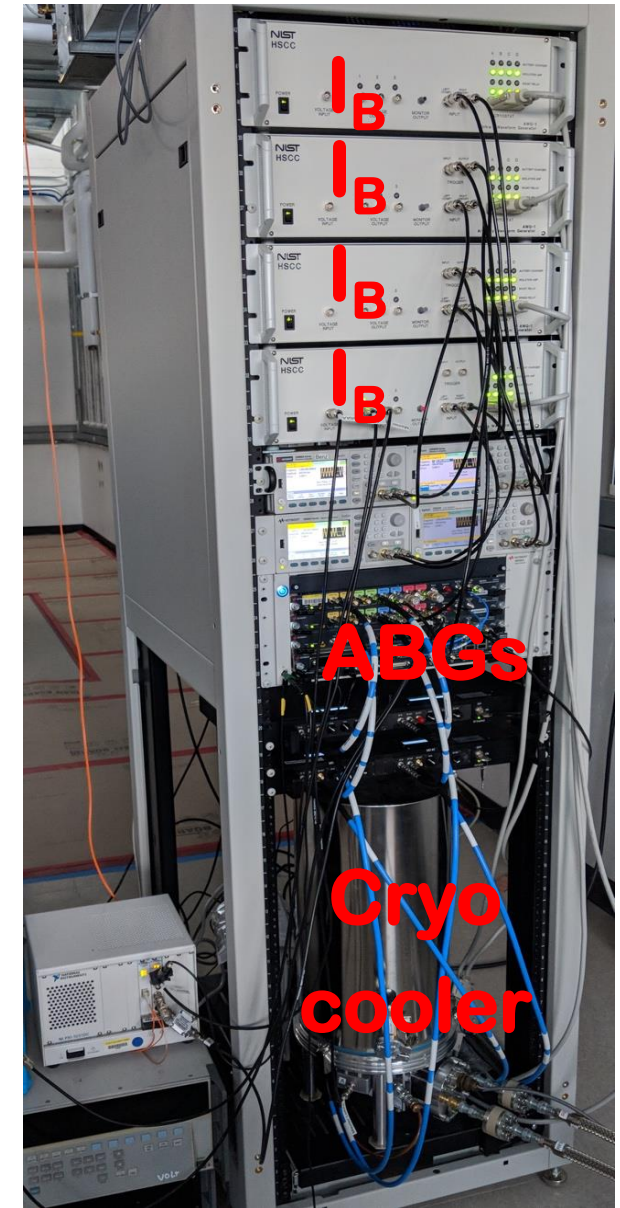
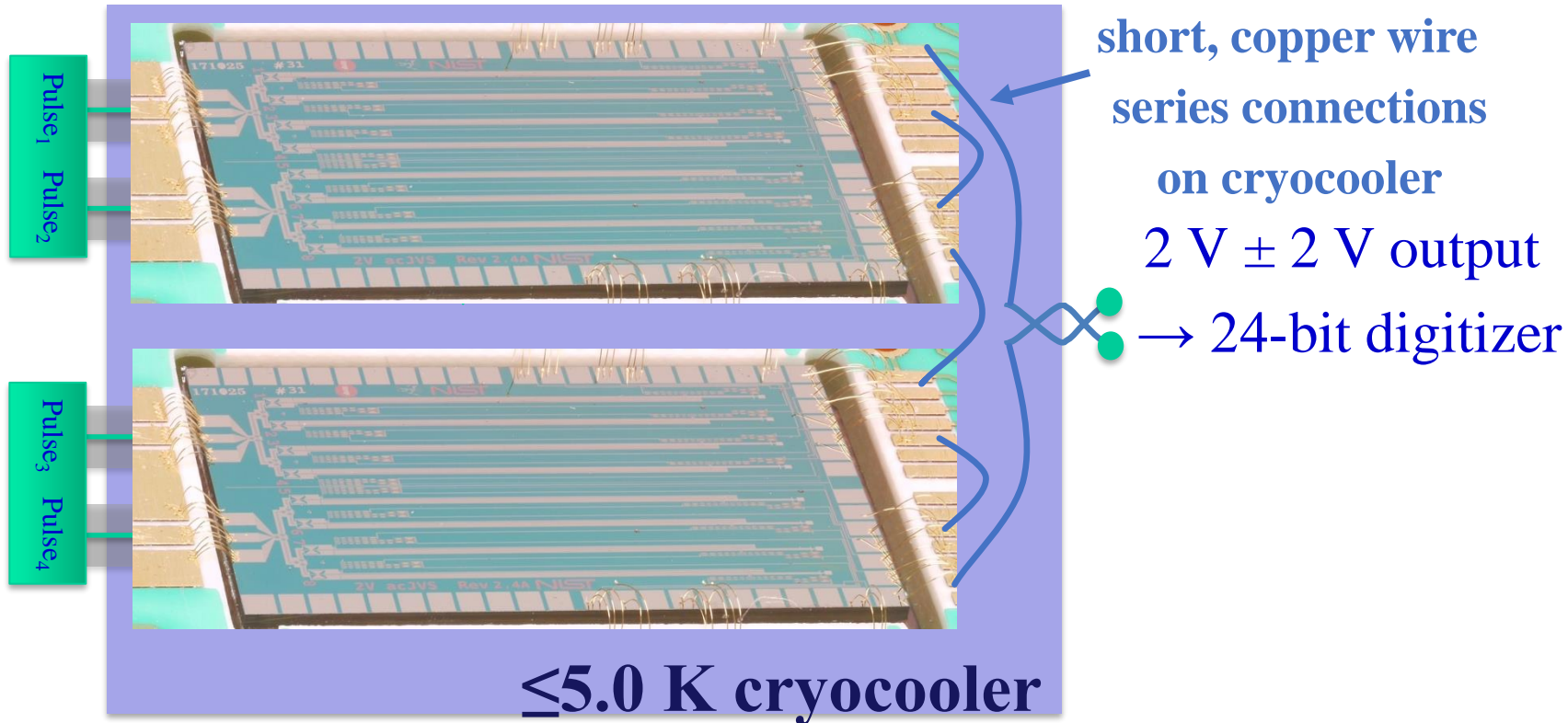


Nathan Flowers-Jacobs,  
ISEC Proceedings,  
Riverside, CA 2019

# 2 chips $\rightarrow$ 4 V Cryocooled JAWS System

**2016: 2 V rms** cryocooled system,  
4 pulse channels (2 sets of bias electronics,  $I_B$ )

**2018: 4 V rms** cryocooled system,  
4 pulse channels (4 sets of bias electronics,  $I_B$ )

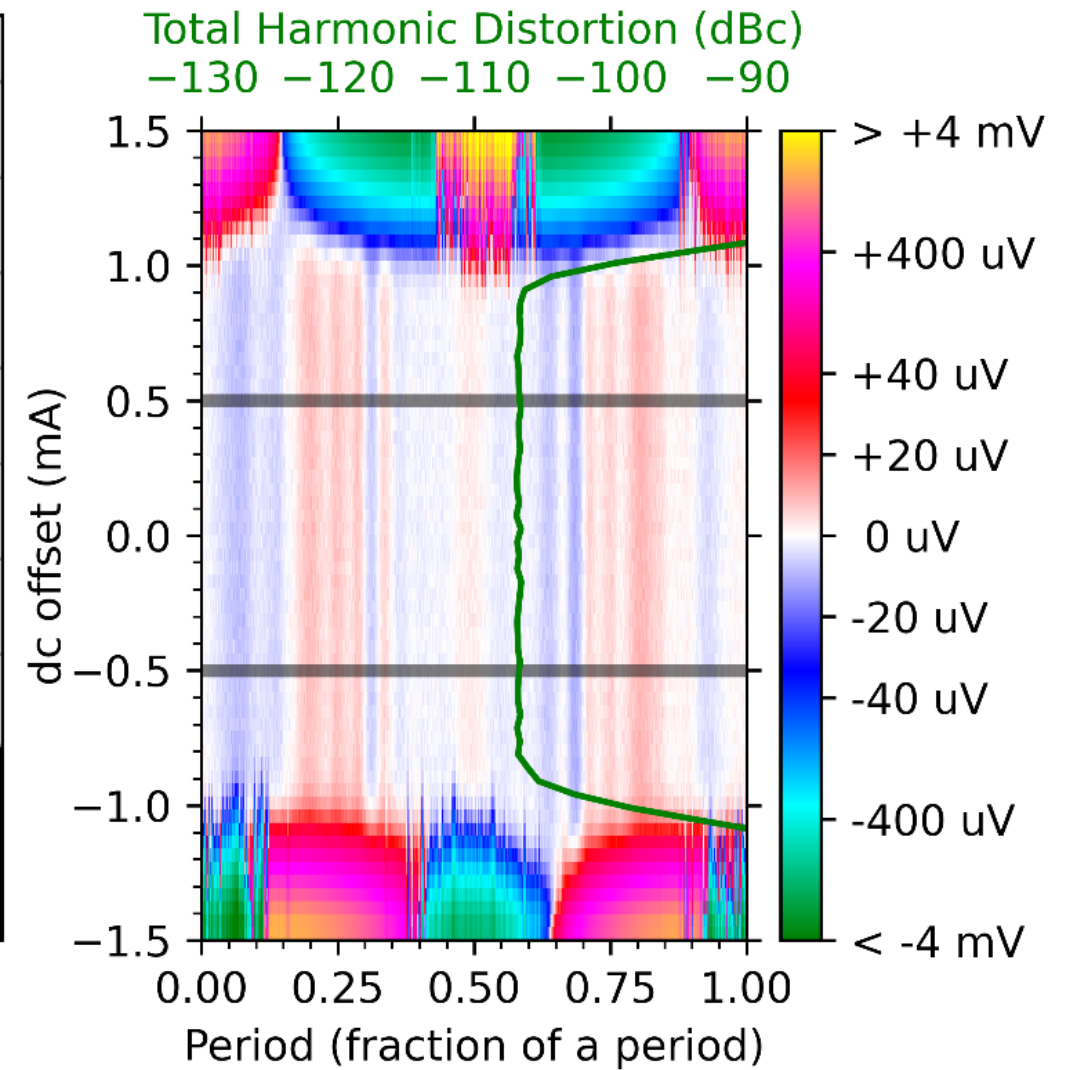
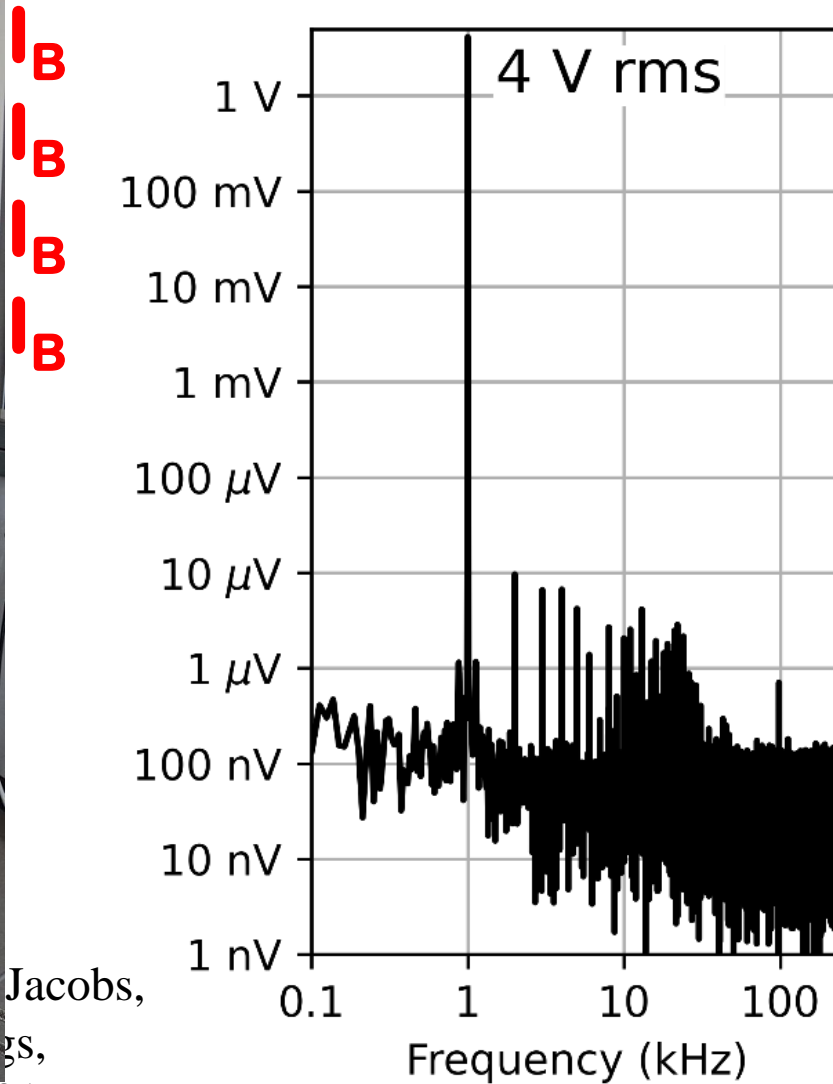




# 4 V rms Cryocooled JAWS



Riverside, CA 2019



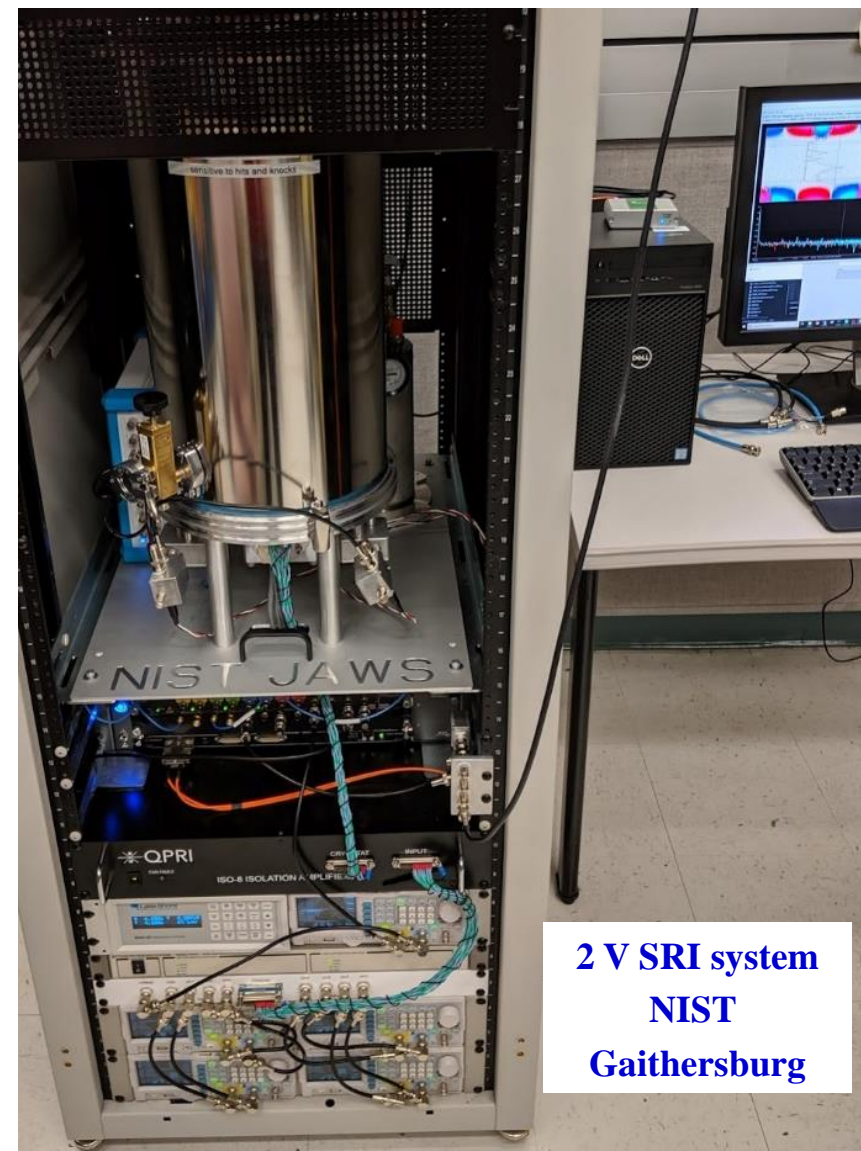
# JAWS Standard Reference Instrument (SRI)

- **User-friendly operation -> Automation**

- Full computer control
  - Verify quantum-accurate operation
    - Still can be systematic errors!!
  - Change/load patterns
  - Automatic AC-DC comparison
    - Fluke 792A, 5790, ...
- Available as a standard reference instrument (SRI)
  - Cryocooled 1 V rms system
  - includes new pulse generator: Keysight M8195a
    - 64 Gsample/sec, 8-bit arbitrary bitstream generator



- [www.nist.gov/sri/sri-6011-josephson-arbitrary-waveform-synthesizer](http://www.nist.gov/sri/sri-6011-josephson-arbitrary-waveform-synthesizer)



2 V SRI system  
NIST  
Gaithersburg



# NIST Josephson Voltage Standard Dissemination



## NIST Systems & Technology

60 Conventional JVS (incl. Hypres, Inc. up to 2015)

26 PJVS Systems + 20 Cryopackages since 2010

8 JAWS Systems + 2 Cryopackages since 2010

4 Johnson Noise Thermometer

## Measurement Labs

National Measurement Institutes: international

National Laboratories: NASA, Sandia, ORNL

Industry: HP, Lockheed, Fluke, Keithley, Keysight, Boeing

DOD: Army, Navy, Air Force

DOE: Sandia & Oak Ridge Nat. Labs

## STANDARD REFERENCE INSTRUMENTS

Standard Reference  
Instruments

SRI 6000 Series  
Programmable Josephson  
Voltage Standard (PJVS)

SRI 6002 Multi-Junction  
Thermal Converter

SRI 6003 Series Portable  
Vacuum Standard

SRI 6006 Precision Micro-  
machined Apertures

SRI 6008 Ozone Standard

SRI 6011 Josephson Arbitrary Waveform  
Synthesizer

The Josephson arbitrary waveform synthesizer (JAWS) is an instrument that synthesizes ac voltage waveforms and dc voltages whose metrological accuracy results from pulse biasing thousands of series-connected superconducting Josephson junctions into their identical quantum states. Technical Contact: [Paul Dresselhaus](#)

[Specifications Certificate](#) (PDF Format)

The prices listed below are for the individual instrument and do not include costs related to the final measurement calibration performed before delivery or post-delivery installation and training. The related Calibration Service ID for the SRI is [68000S](#). To obtain a quote for the instrument and calibration services, please contact Sales and Customer Service by phone at 301-975-2200 or email at [srminfo@nist.gov](mailto:srminfo@nist.gov).



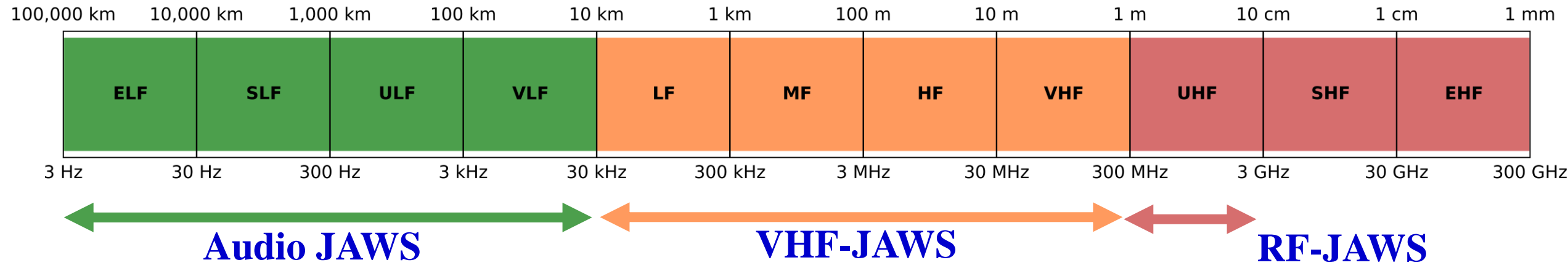
6011d	2V JAWS chip and cryopackage (standalone)	\$53,100
6011f	Cryocooled 2V JAWS System (water)	\$569,000
6011g	Cryocooled 2V JAWS System (water, no synthesizer)	\$328,700
6011h	Cryocooled 2V JAWS System (air-cooled compressor)	\$571,600
6011a	Cryocooled 1V JAWS System (water)	Discontinued
6011b	Cryocooled 1V JAWS System (air)	Discontinued
6011c	1V JAWS chip and cryopackage (standalone)	Discontinued
6011e	1V JAWS Cryopackage with Liquid Helium Cryoprobe	Discontinued



# RF JAWS Synthesizer with Quantum-based Accuracy for RF Communications

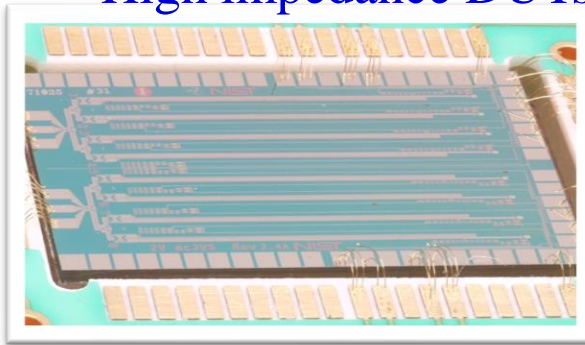
- J. Thomas, J Hoffmann, N E Flowers-Jacobs, A E Fox, R L Johnson-Wilkke, P D Dresselhaus, S P Benz, “Cryogenic On-chip In Situ S-parameter Calibration using Superconducting Coplanar Waveguides,” submitted to IEEE Trans. Micro. Theory Tech.
- J. Thomas, et al., “VHF Josephson Arbitrary Waveform Synthesizer”, IEEE Trans. Appl. Supercond., vol. 34, July 2024.
- A. A. Babenko, et al., “Quantum-Based Microwave Modulated Waveforms,” IEEE Trans. Microw. Theory Tech., vol. 72, Aug. 2024
- A. A. Babenko, et al., “A microwave quantum-defined millivolt source,” IEEE Trans. MTT, vol. 69, Dec 2022.

# NIST JAWS Chip Types



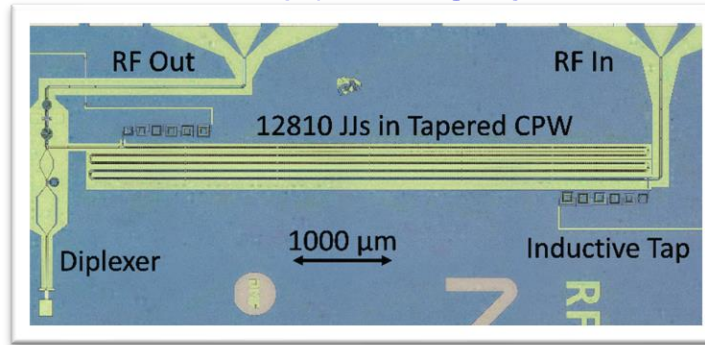
## Audio JAWS

- Established: 2V, <100 kHz
  - Dividers (more arrays)
  - Impedance tapered arrays (more JJs per array)
- High impedance DUTs



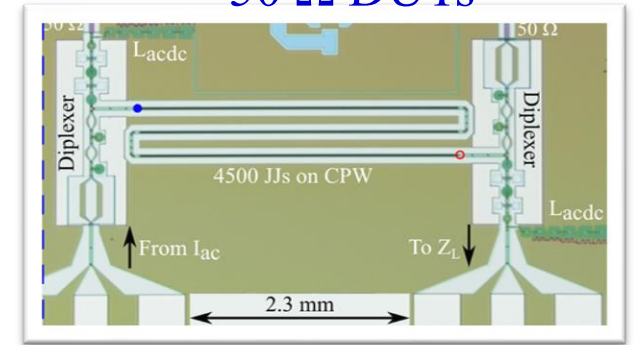
## VHF-JAWS

- Goal: 0 dBm, up to 300 MHz
  - Diplexers (remove feedthrough, termination)
  - Tapered arrays
- 50  $\Omega$  DUTs



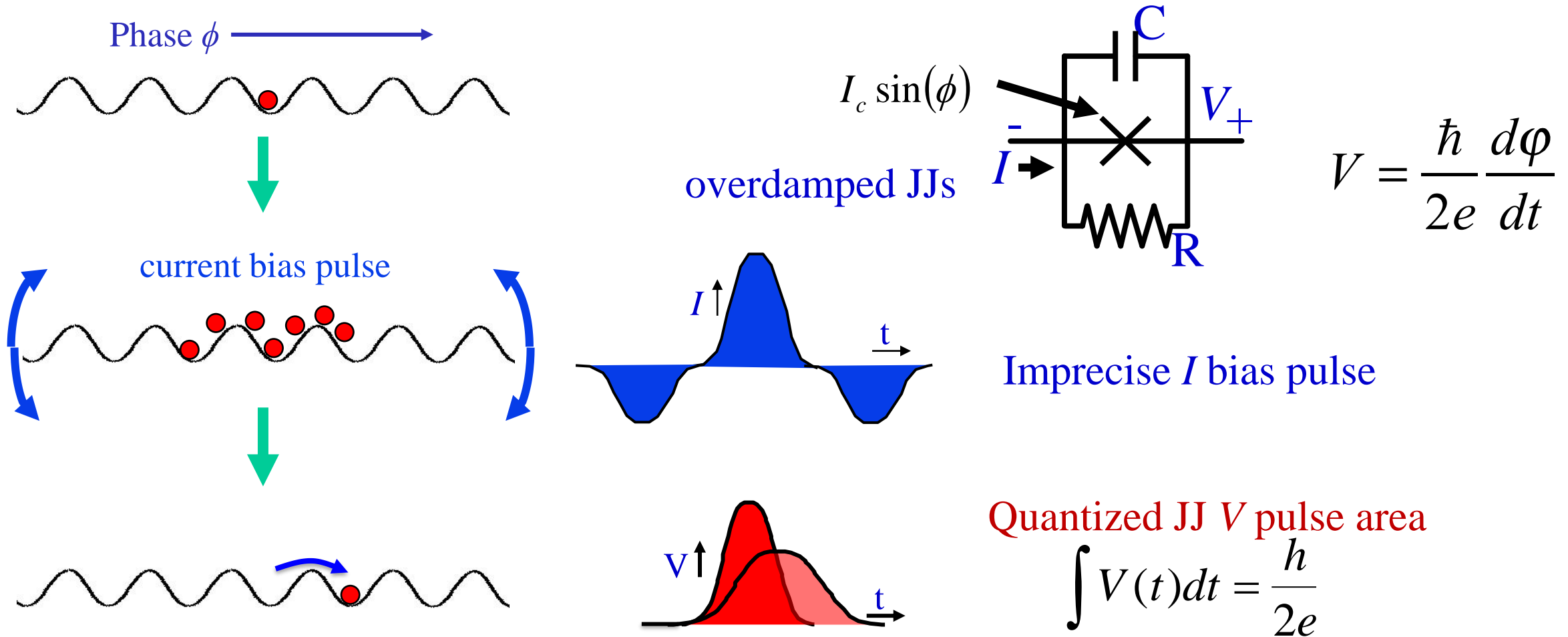
## RF-JAWS

- Goal: up to 3 GHz
  - Diplexers
- Un-tapered 50  $\Omega$  arrays ( $\lambda \rightarrow$  array length)
- 50  $\Omega$  DUTs





# “Zero-Compensation” bias pulses



# FFTs for Zero-Compensation Bias Coding

High  $\Rightarrow$  10

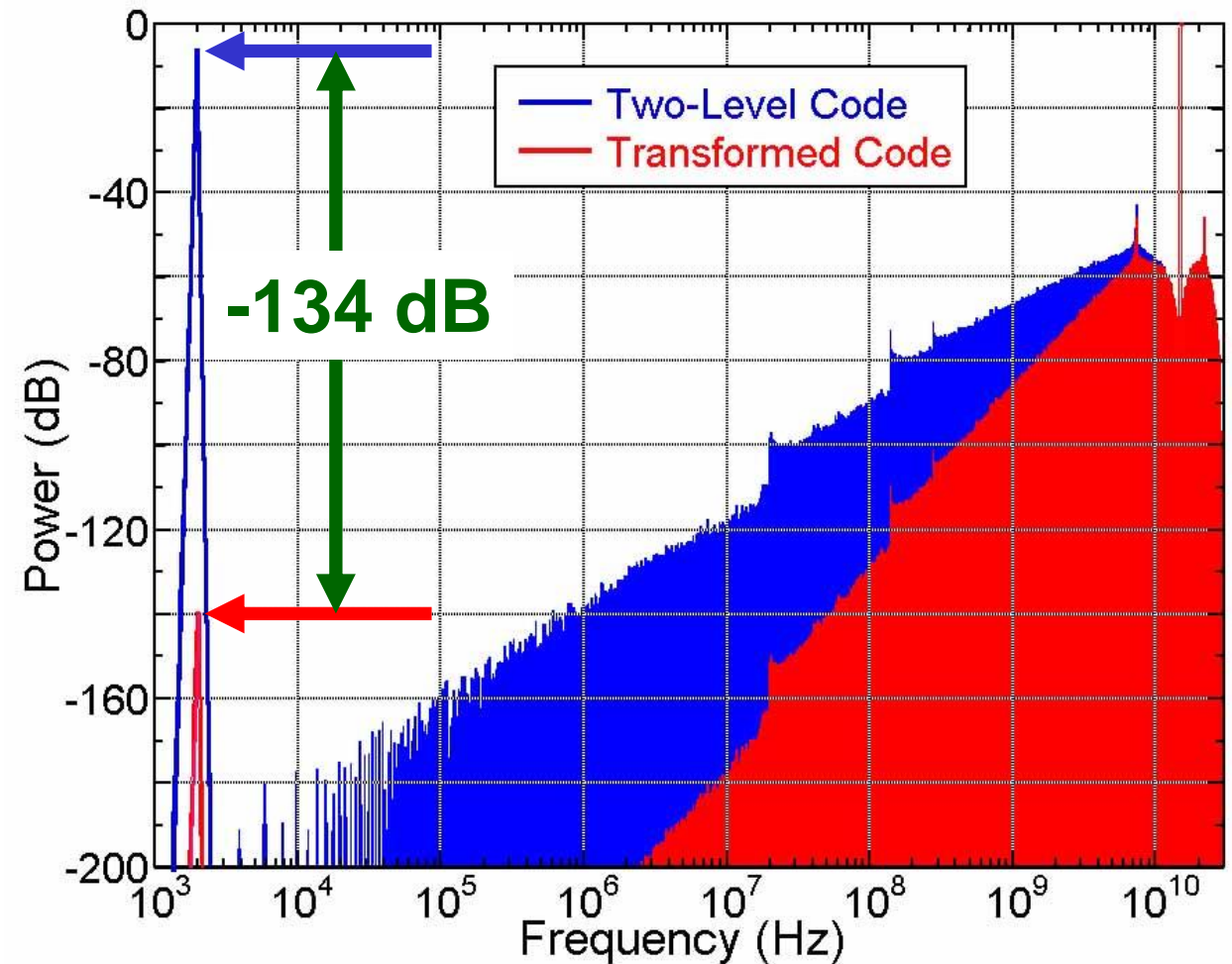
Low  $\Rightarrow$  01

Amplitude of Fundamental (Bias):

At 2 kHz is reduced  $\sim 2 \times 10^7$

At 2 MHz its reduced to  $\times 10^4$

- Lower Feedthrough error signals

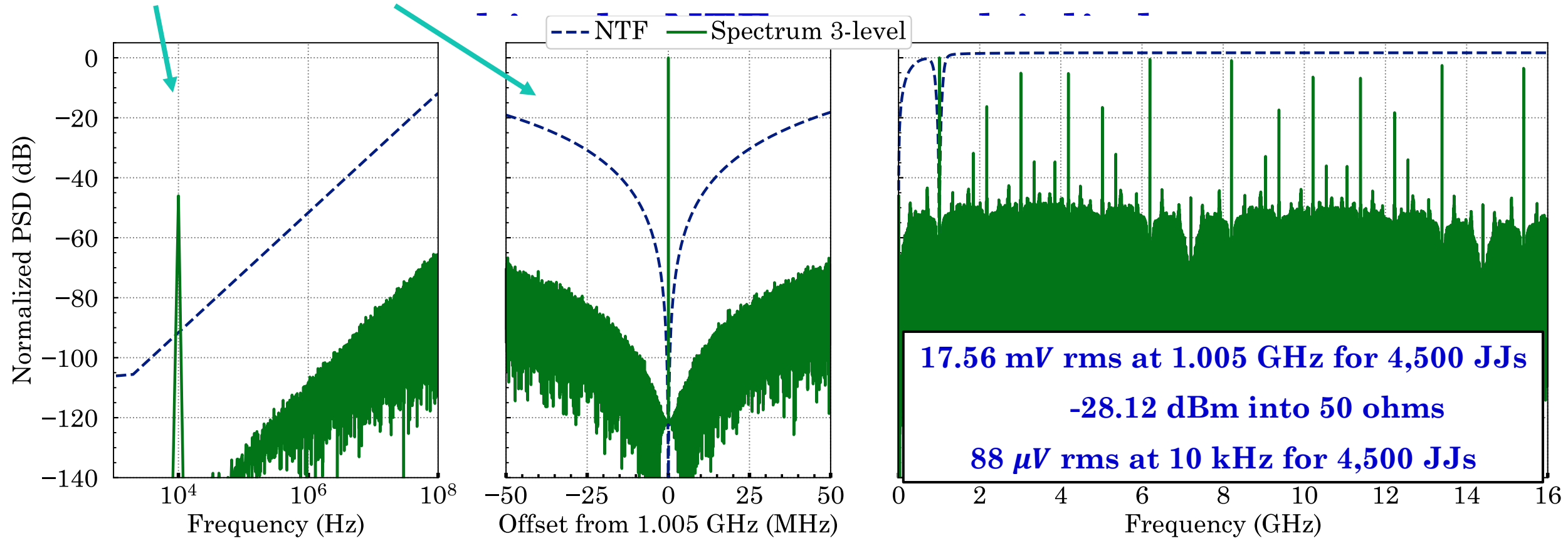




# Two-Tone Delta-Sigma waveform



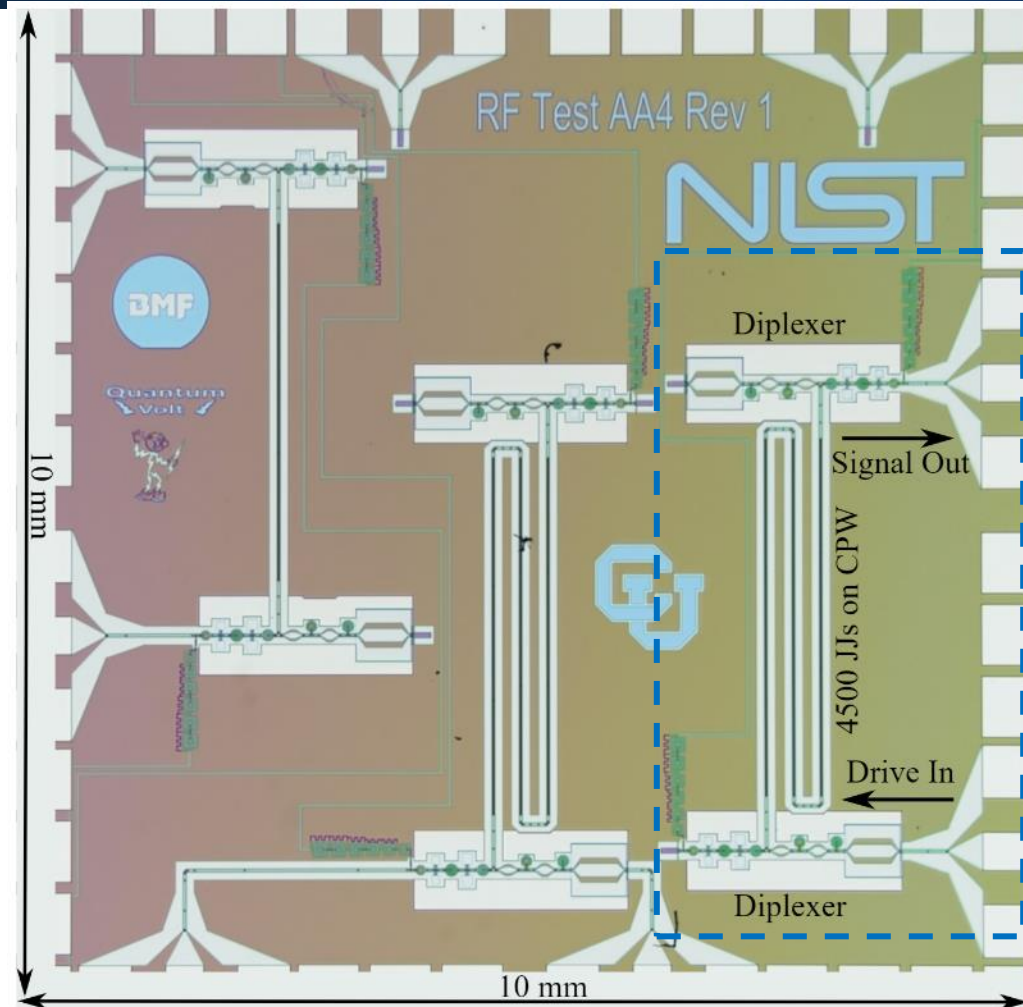
**Low-pass and Band-pass delta-sigma modulators can be**



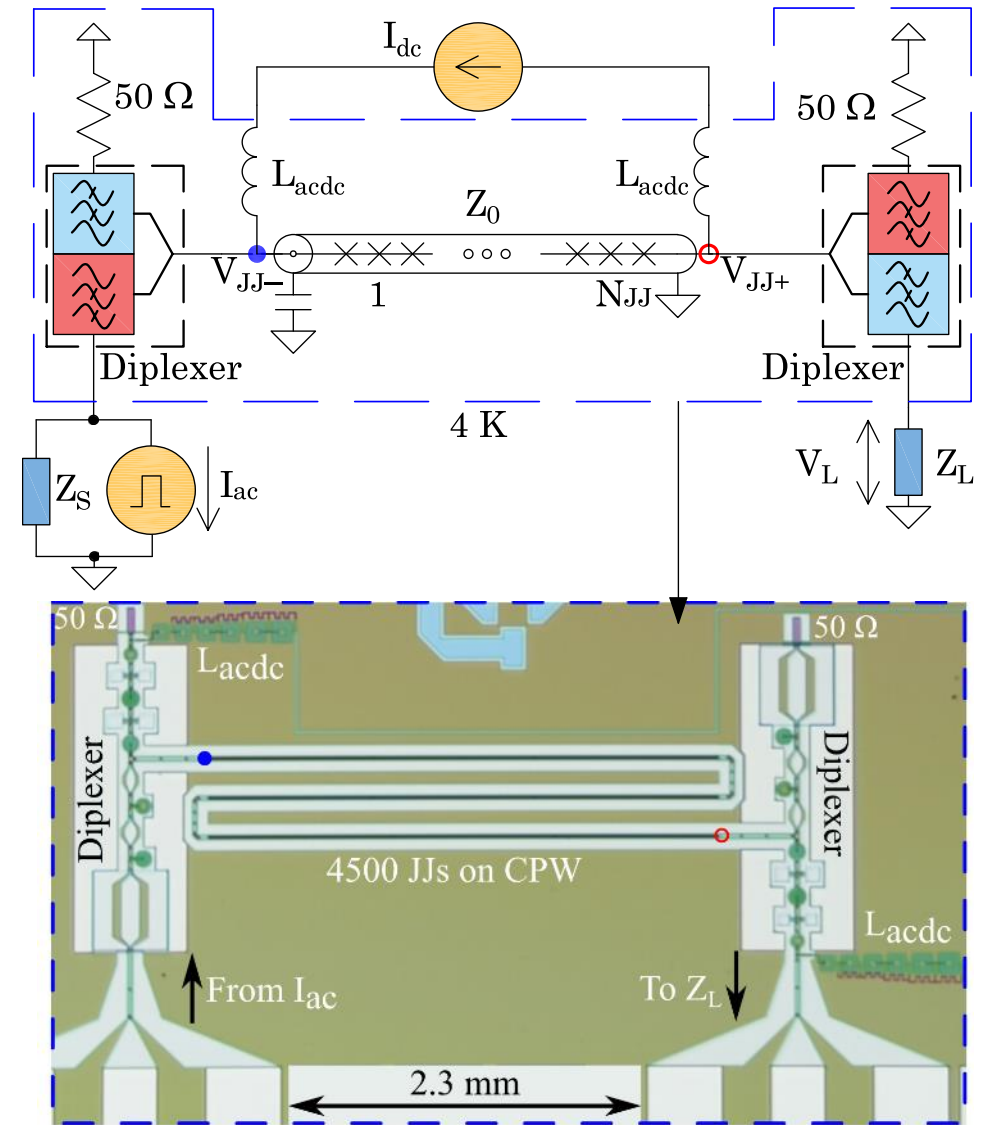
**Fast measurements at 10 kHz are used to verify and optimize 1.005 GHz synthesis**

NTF – noise transfer function

# VHD- & RF-JAWS on-chip Diplexers



The diplexers reduce reflections and feedthrough for the drive current pulses along the JJ array





# Quantum-Locking Ranges up to VHF-band **NIST**

## What is a QLR?

- The range over which a bias parameter can be changed while the output voltage remains constant and the Total Harmonic Distortion THD is minimized.

## Why is a large QLR important?

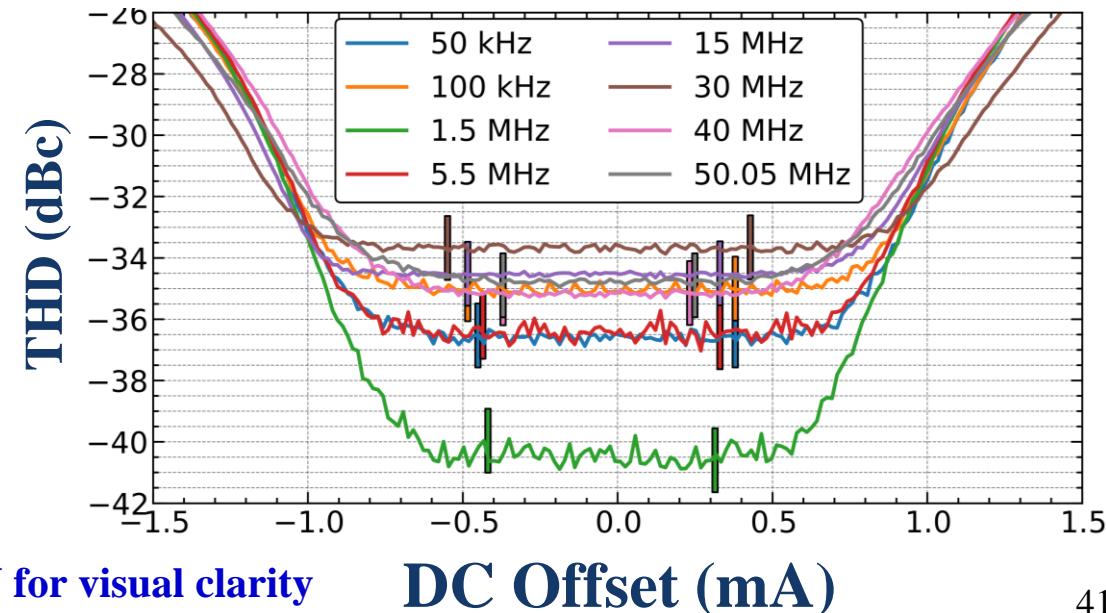
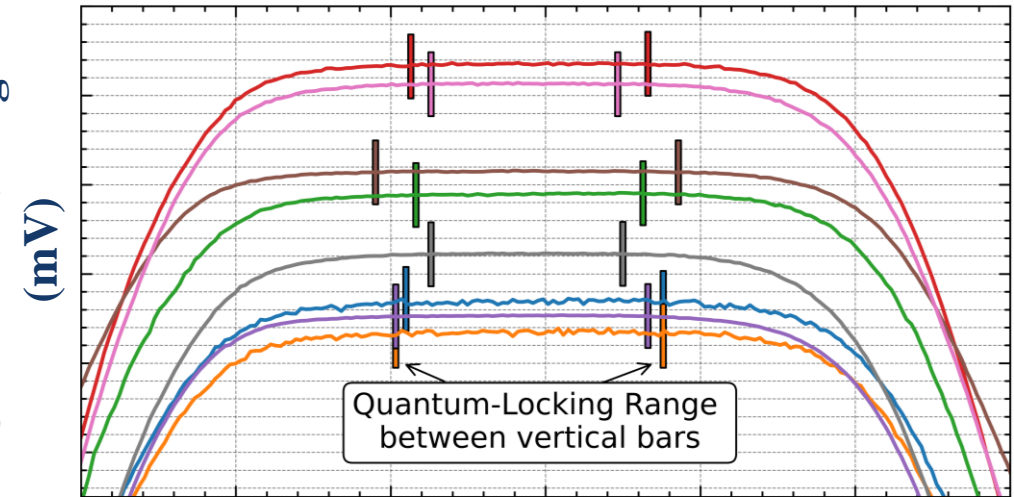
- It demonstrates that the device can operate correctly despite changes to the bias or grounding conditions.

## How can we use the QLR?

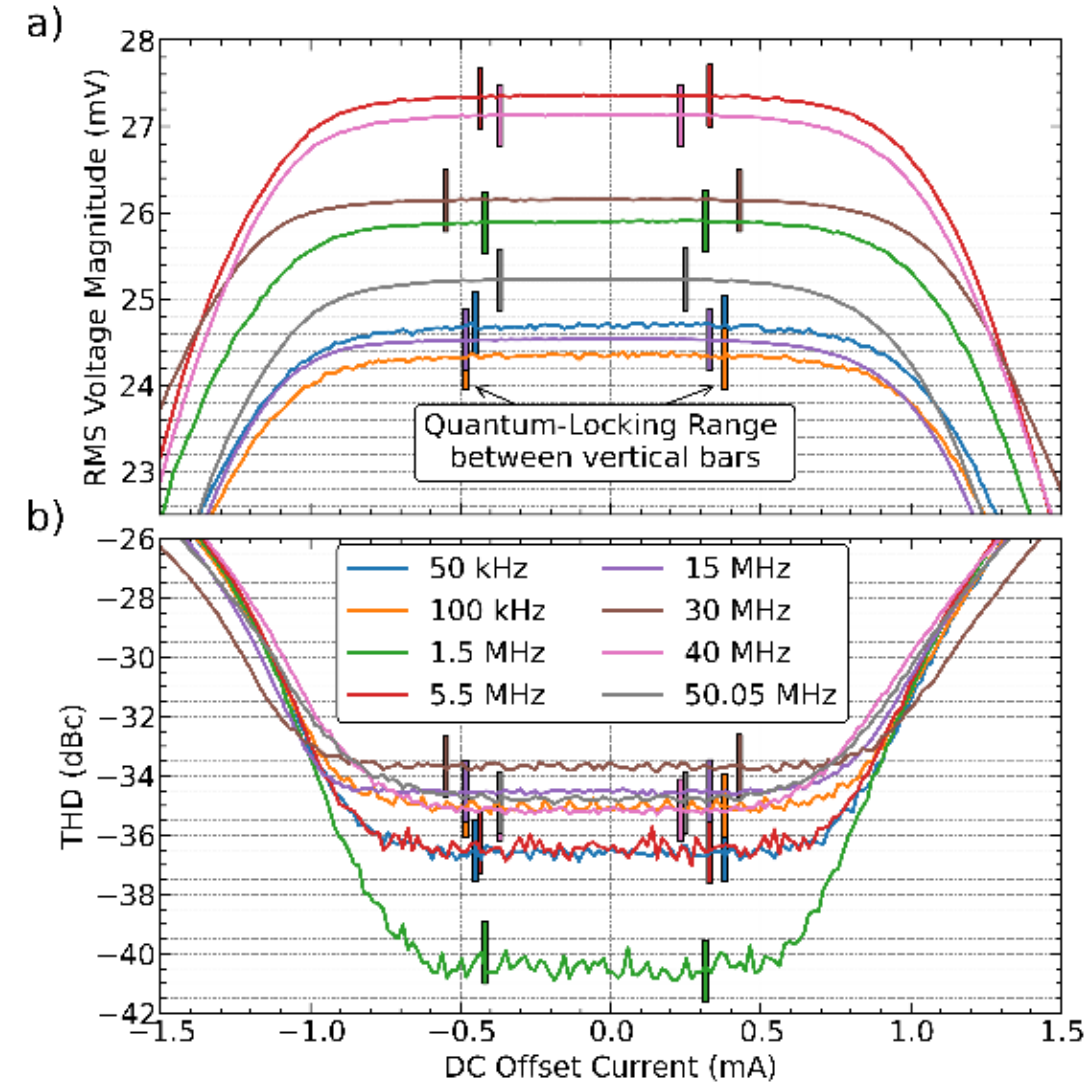
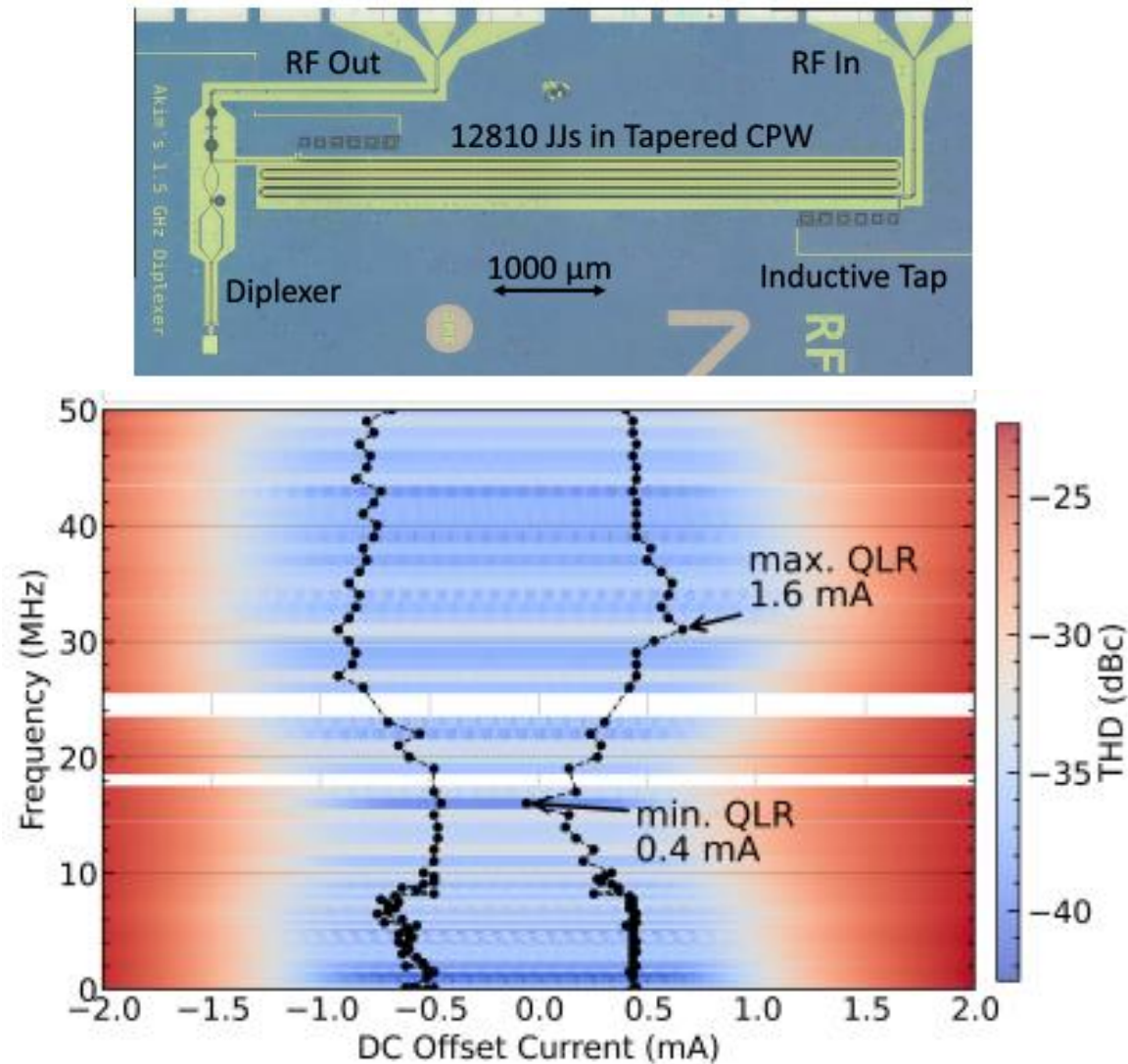
- Optimize pulse shape with FIR filters to optimize QLR
- Important tool for investigating systematic sources of error

Frequency-  
dependent  
voltage

Deviation from  
Calculated Voltage



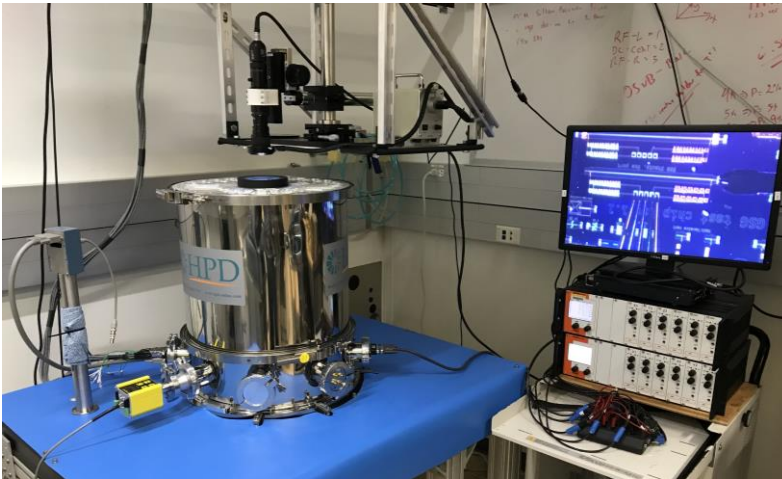
# VHF-JAWS 50kHz to 50 MHz





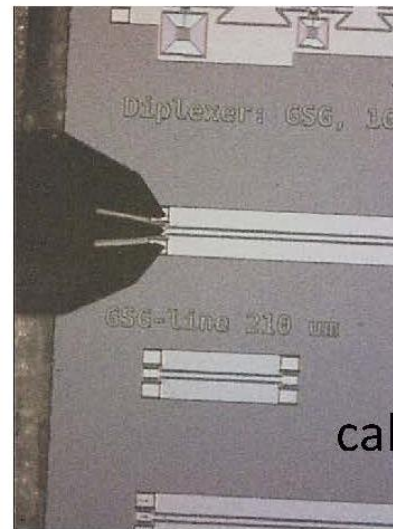
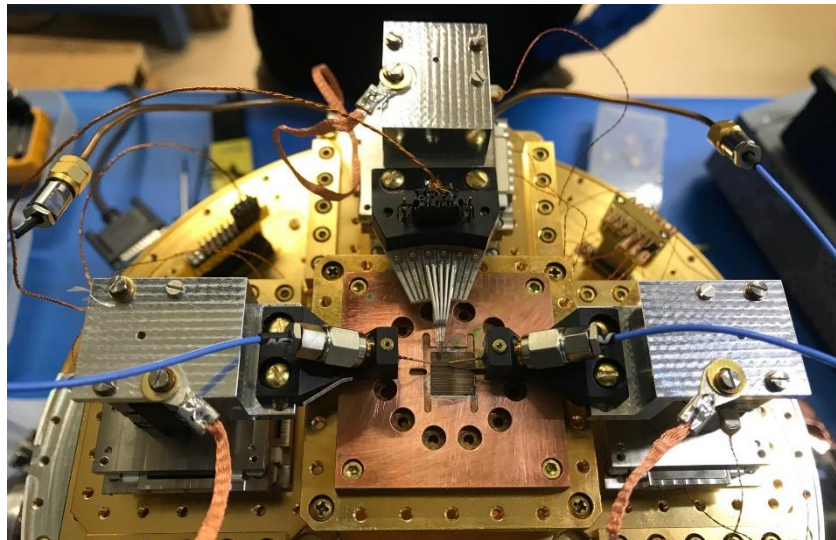
# Voltage is accurate only on chip

- Calibrate transfer function of room-to-chip leads at cryogenic temperatures

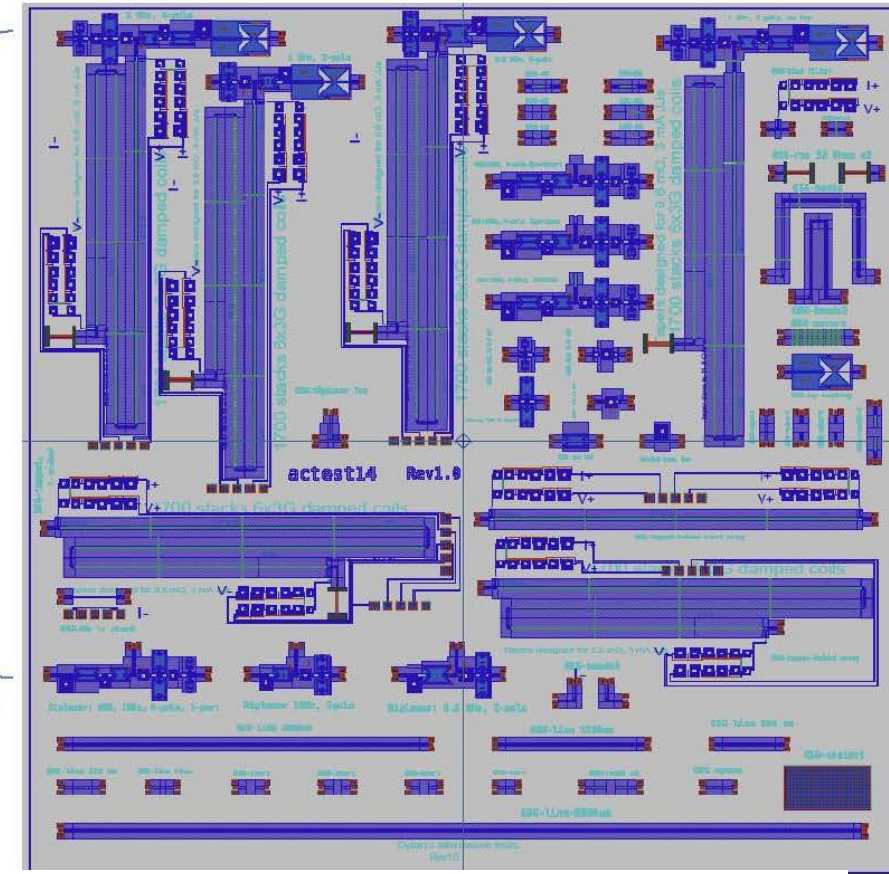


## 4 K Probe Stage with JJ Devices & Standards

JJ arrays for NIST Josephson arbitrary waveform synthesizer (JAWS)

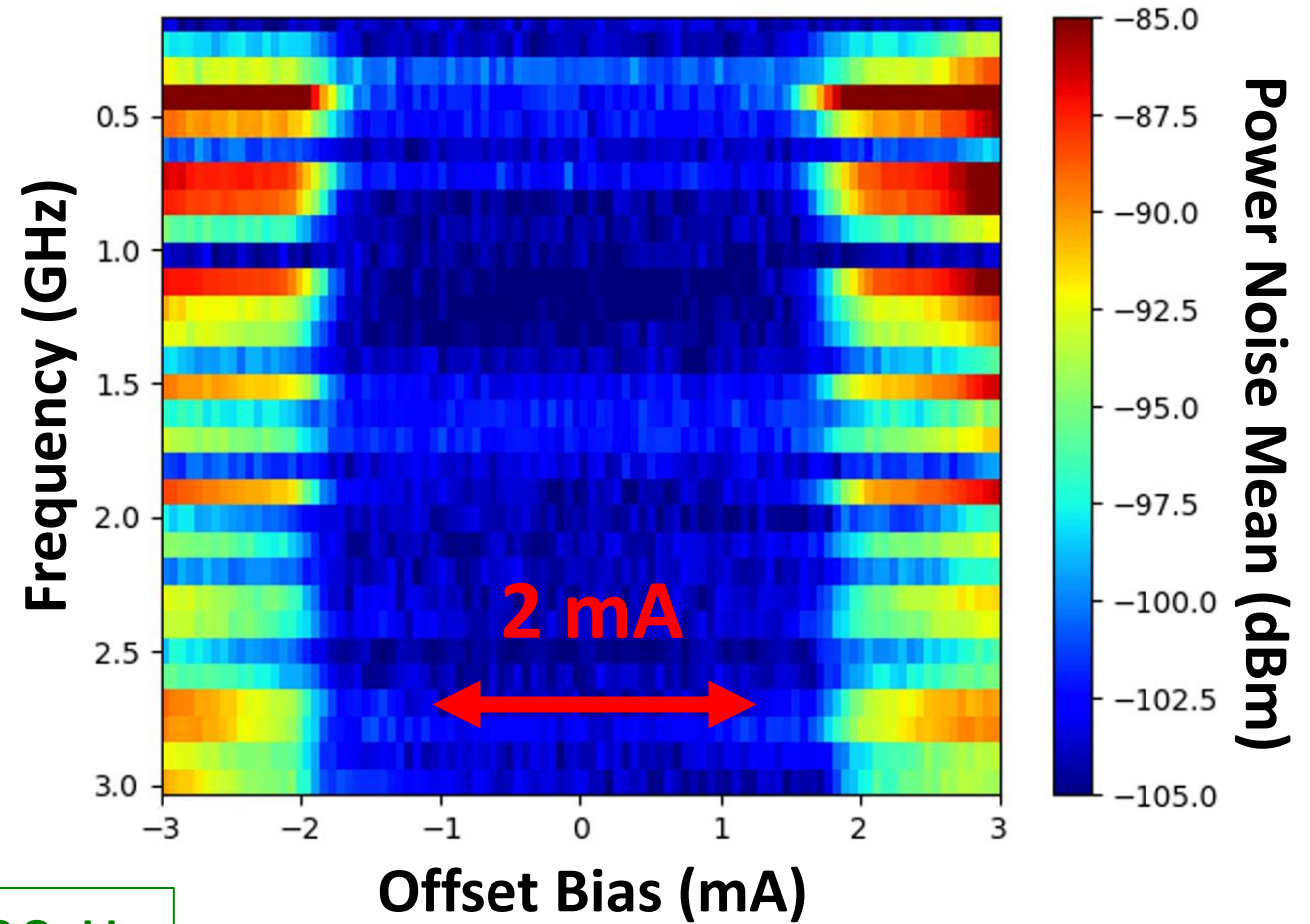
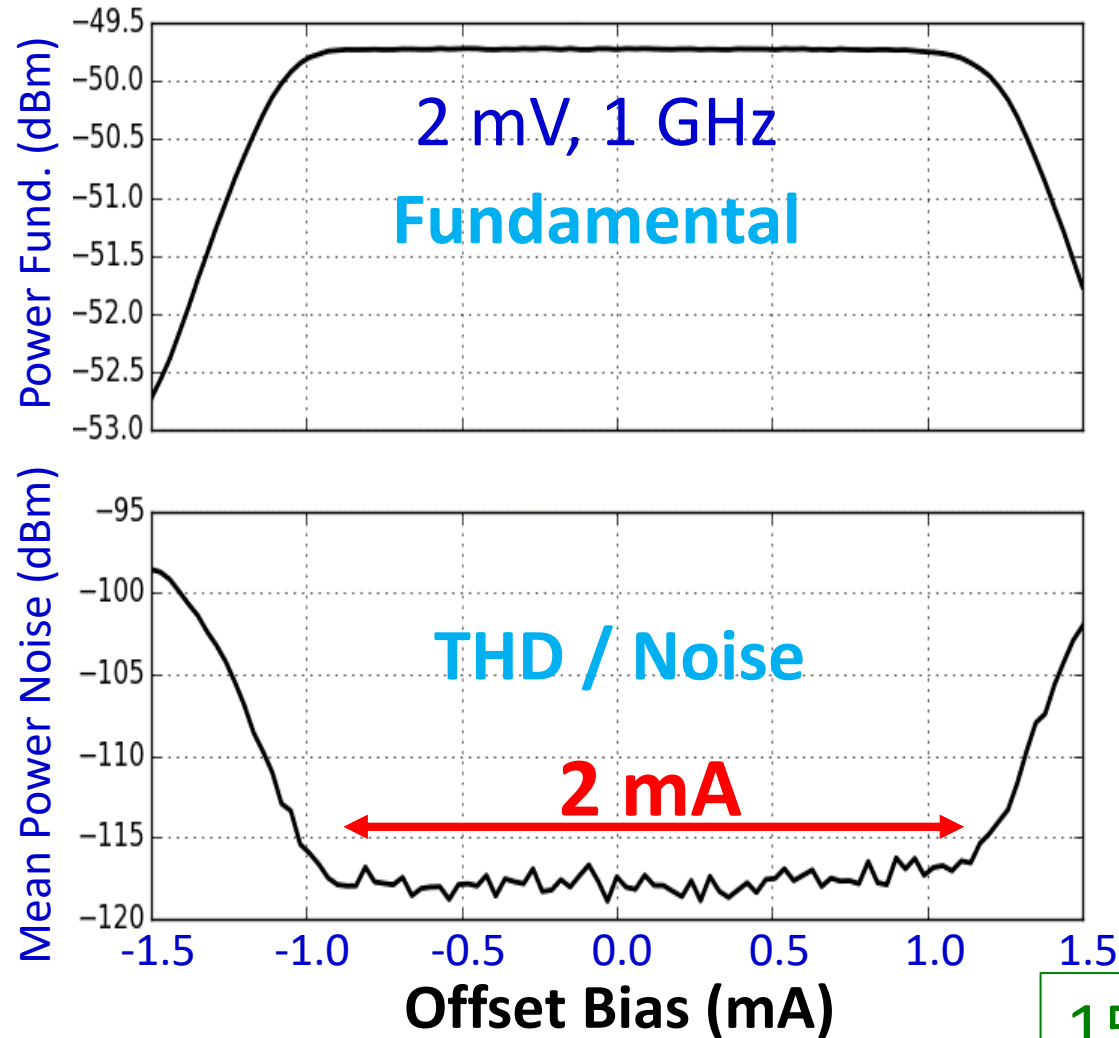


TRL calibrations



Dylan Williams 2016 ASC Conference 143

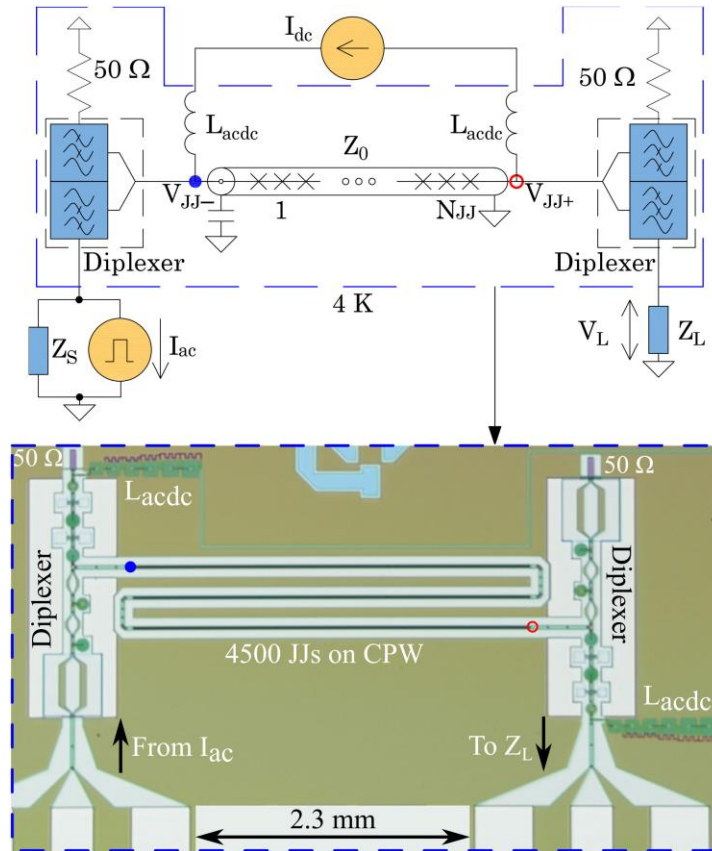
# RFJAWS Quantum Locking Range at 1 GHz





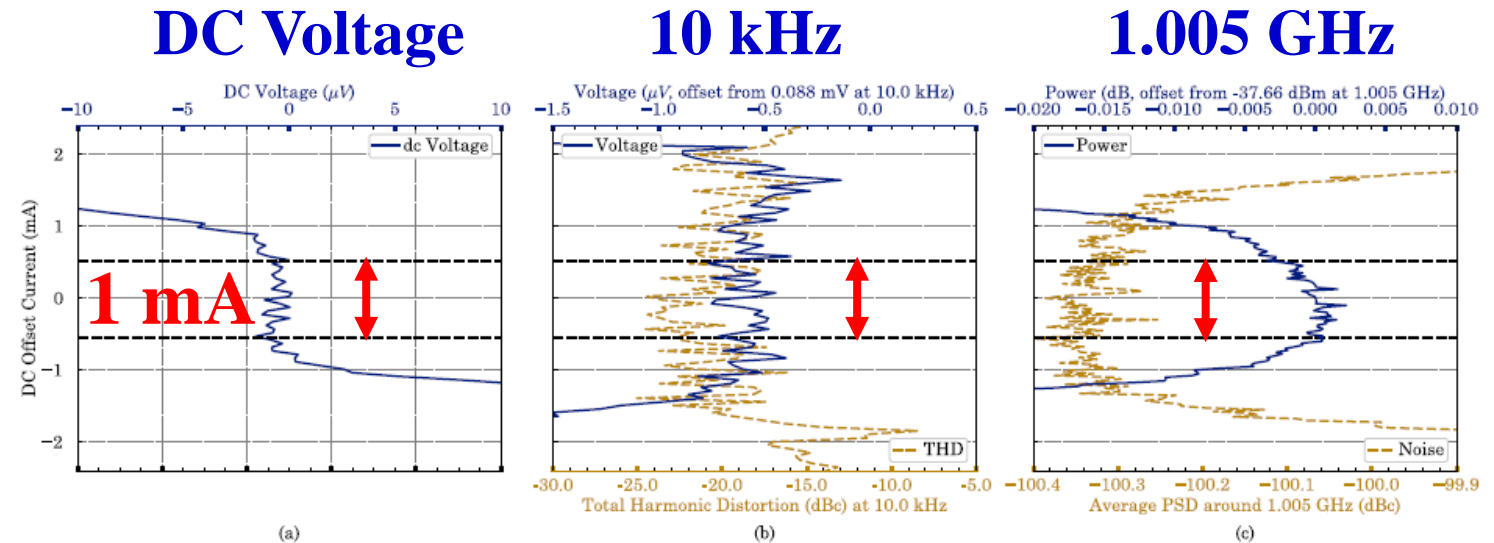
# Record 22 mV rms RF JAWS Quantum Locking Ranges

RF-JAWS circuit with 4500 Junctions

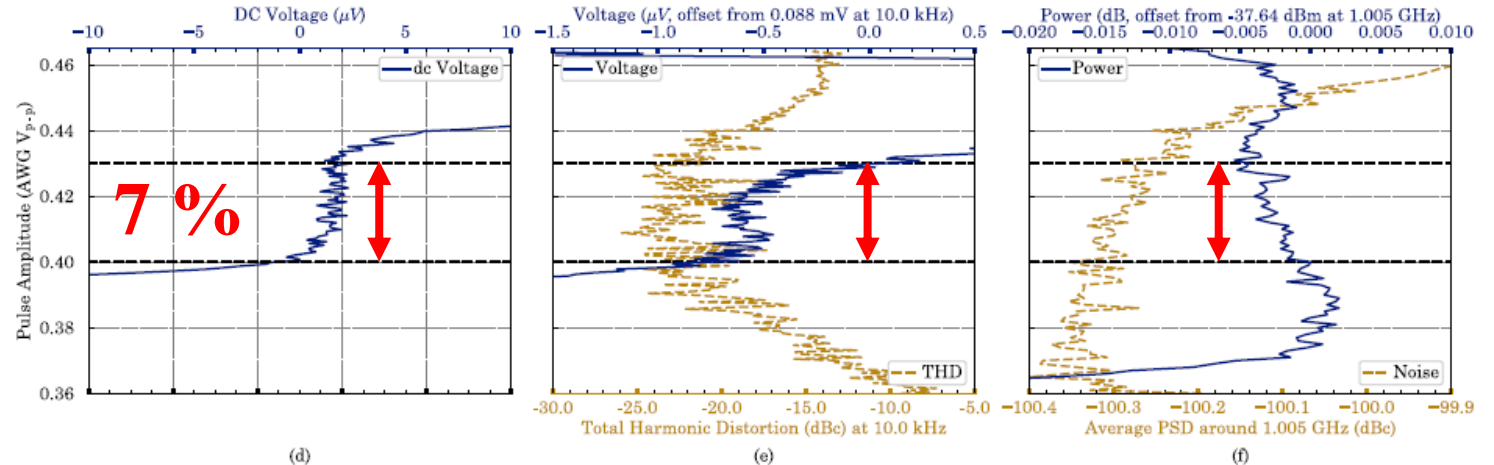


Record 22 mV rms ( $-26.18$  dBm) at 1.005 GHz

DC Current Bias



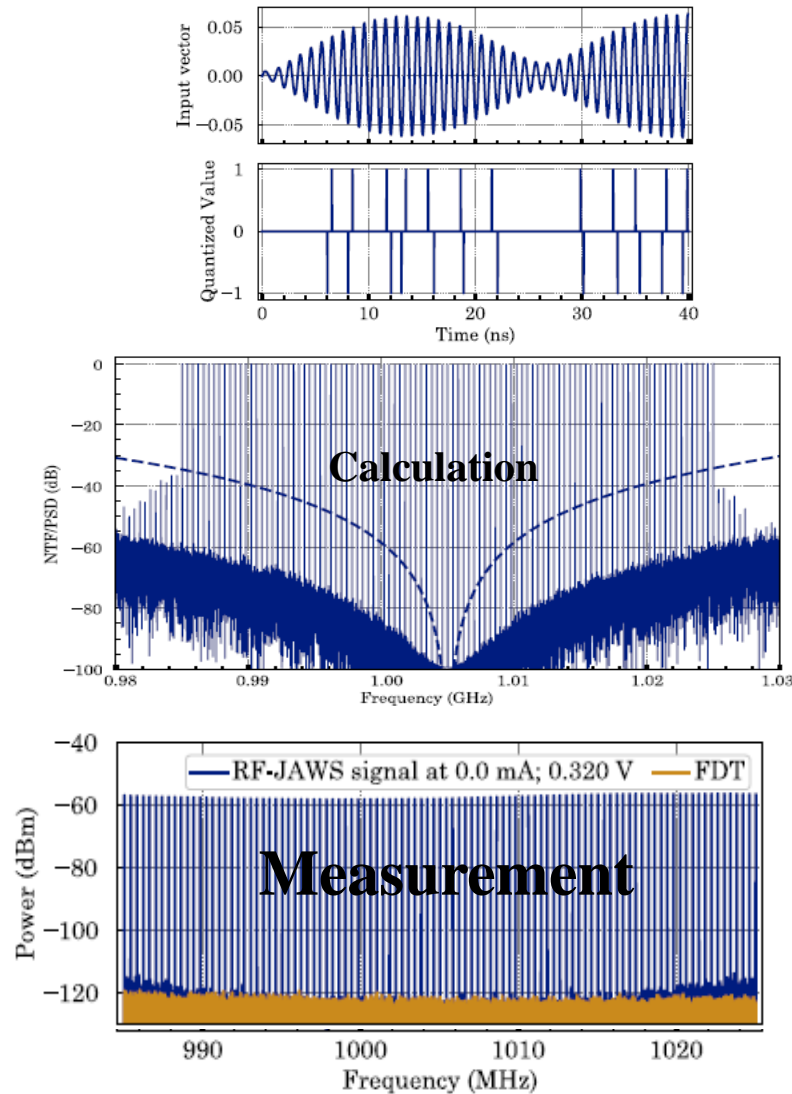
Pulse Bias



A. Babenko, et al., IEEE Trans. Appl. Supercond., Nov. 2022.

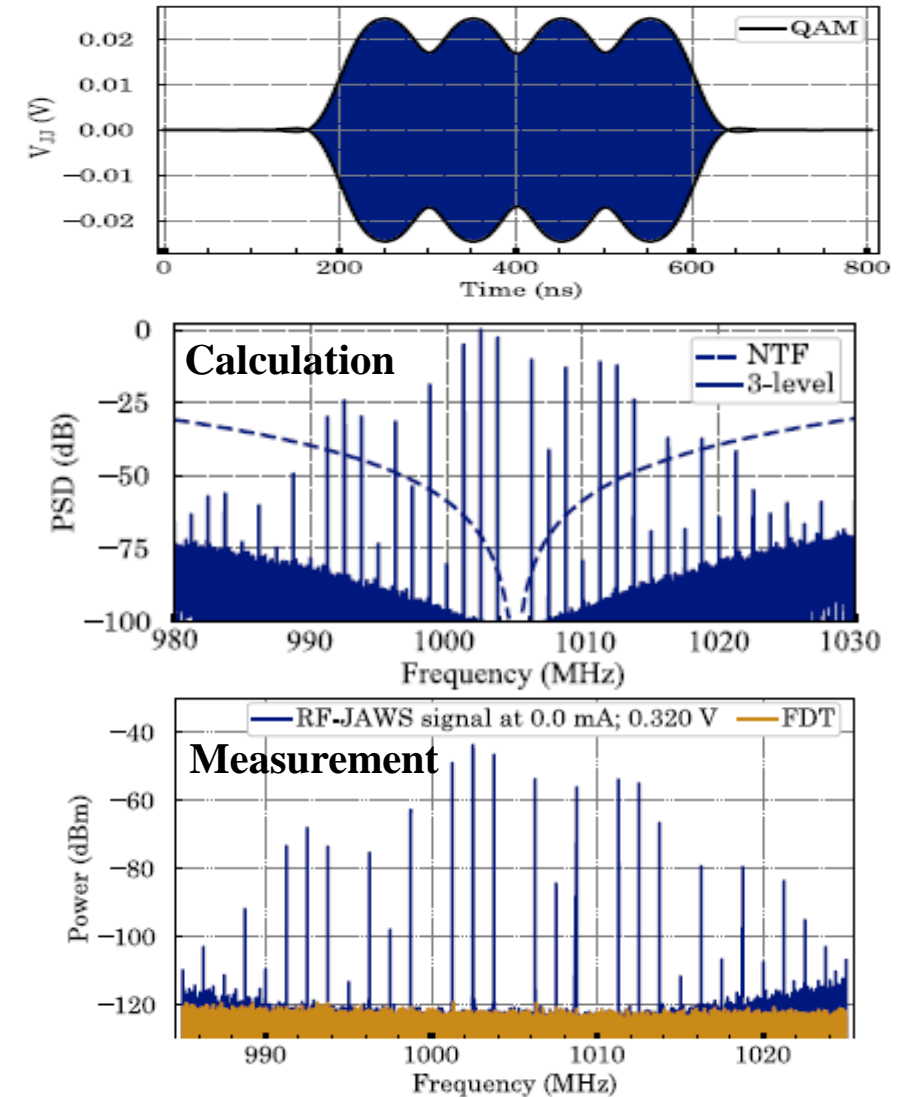
# Quantum-Based Modulated Microwave Waveforms

## 101-Tone Chirp Signal



Both  
waveforms on  
a 1.005 GHz  
carrier

## 10 MHz QPSK Signal



A. Babenko, IEEE MTT

April 2024



# Conclusion

- PJVS and JAWS are quantum-based voltage sources
  - Available as NIST Standard Reference Instruments (SRI)
- VHF- & RF-JAWS are in development
  - Linearity and waveform purity are primary features
  - Single sinewaves for power/phase calibrations
  - Multi-tones and pulses for measuring DUT non-linearities

