

Muon Colliders & Their Magnet Technology Needs

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Drawing on work conducted by:
*the US Muon Accelerator Program (MAP),
the International Design Study for a Neutrino Factory (IDS-NF),
the International Muon Ionization Cooling Experiment (MICE) and
the International Muon Collider Collaboration*



U.S. DEPARTMENT OF
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Themes of this Talk



High Energy
Physics

Perspectives
on the Field

Why
Muons?

A Vehicle for
Discovery

The Physics
Challenges

A Muon
Collider

Machine Concepts

The Magnet
Technology Pull



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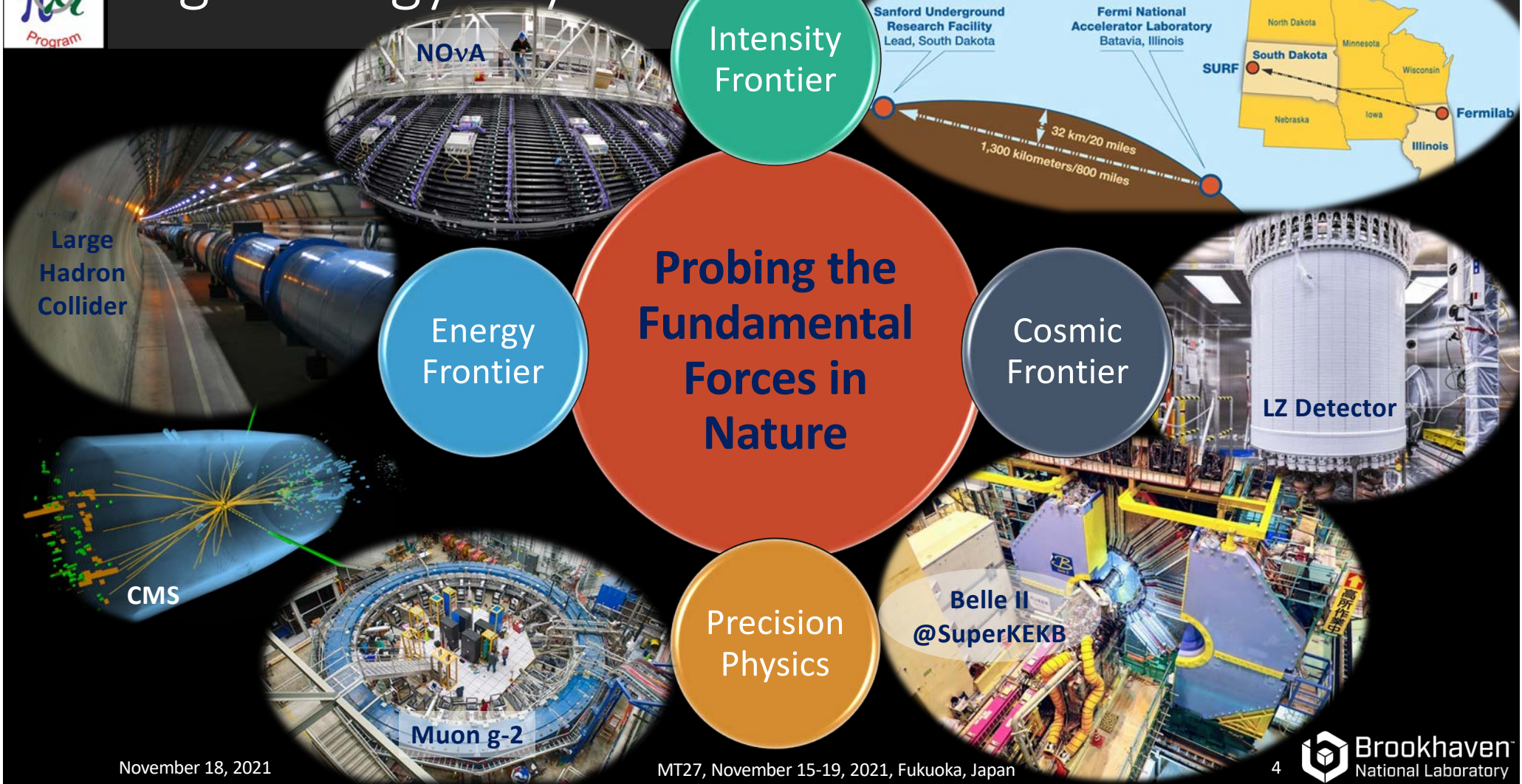
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High Energy Physics

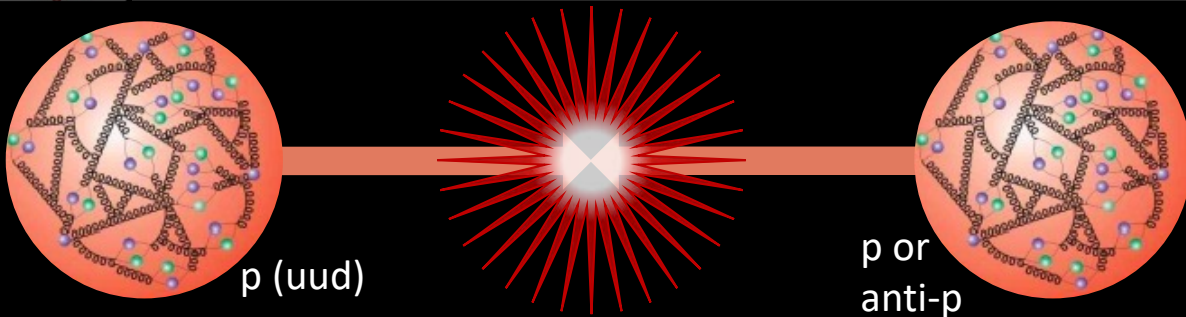


November 18, 2021

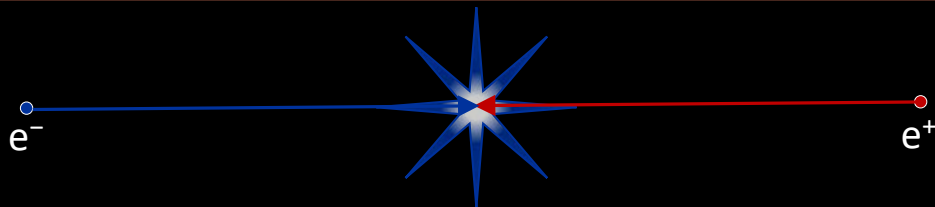
MT27, November 15-19, 2021, Fukuoka, Japan



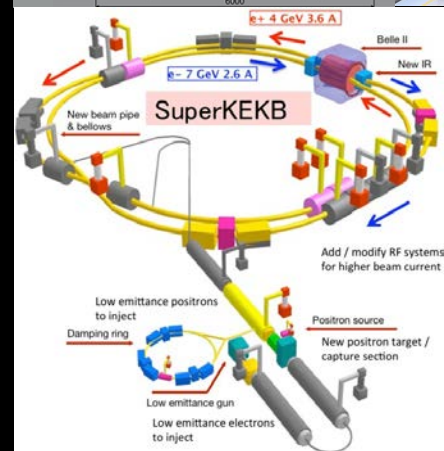
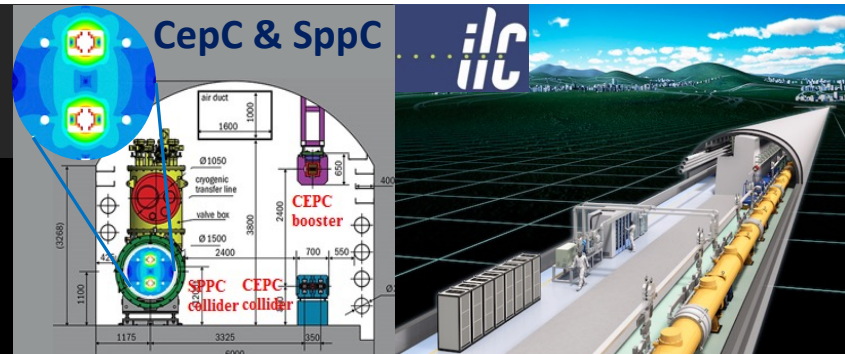
HEP Particle Colliders



- Proton-proton (or anti-proton) Collisions:**
- Offer highest achievable center-of-mass collision energies
 - Collisions of composite particles
 - Discovery potential via Electroweak and Strong Interactions

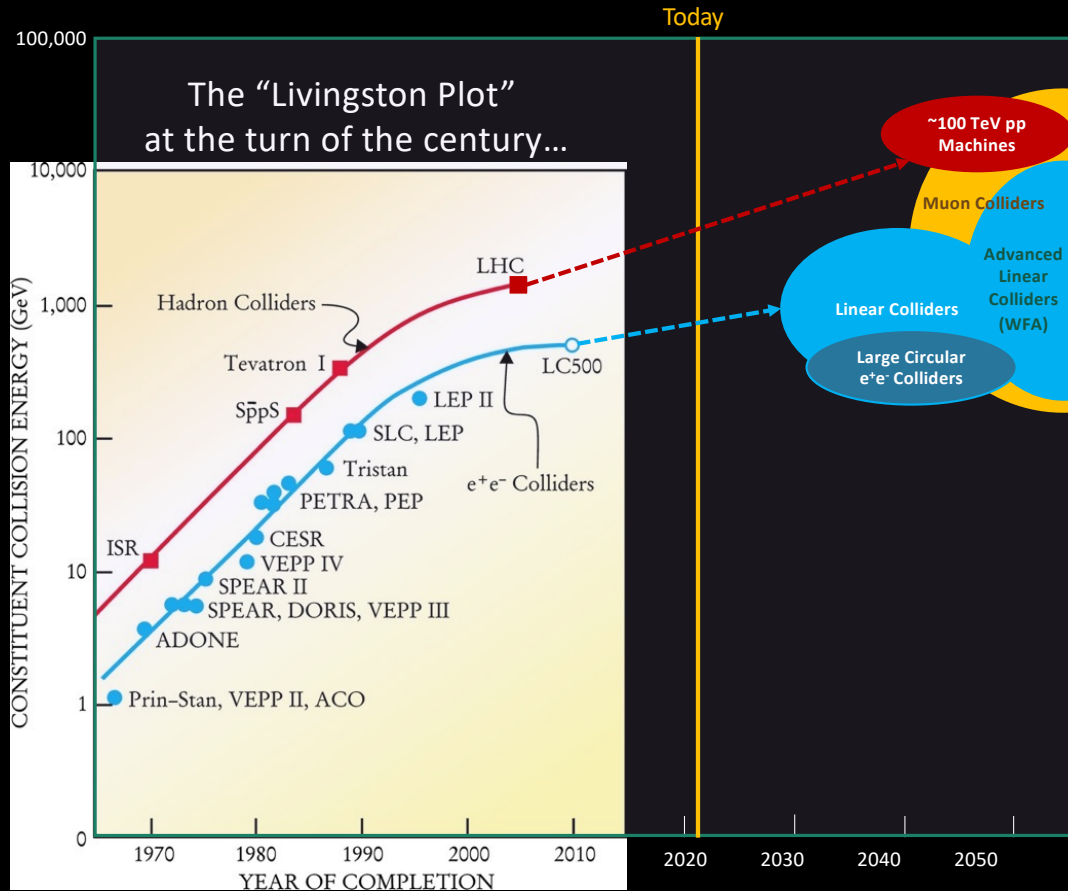


- Electron-Positron Collisions:**
- Collision of point-like fermions with well-defined initial state
 - Precision measurements via Electroweak Interactions





A Look at Where We Are



- Livingston Plot in 2001 [M. Tigner, Physics Today 54 , 1, 36 (2001)]
- Through the 1900s, progress driven by critical technology developments for many decades (1940s –)
- CoM Energies increasing by **~2 orders of magnitude** every **25 years**
- Where are we now?
 - Progress has become much more challenging
 - Machine Complexity
 - Costs (R&D and capital)
 - **What are our options and priorities for the next HEP machine?**

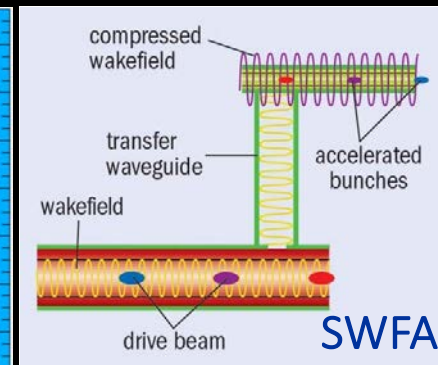
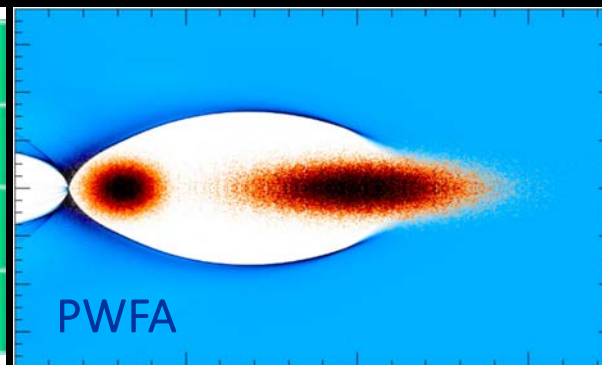
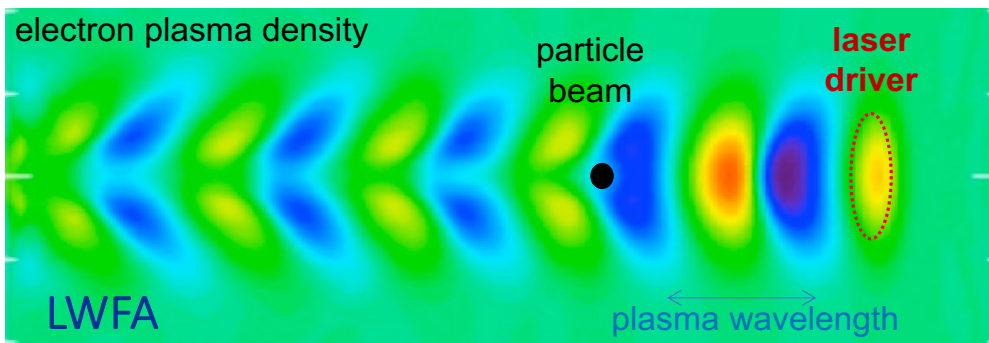
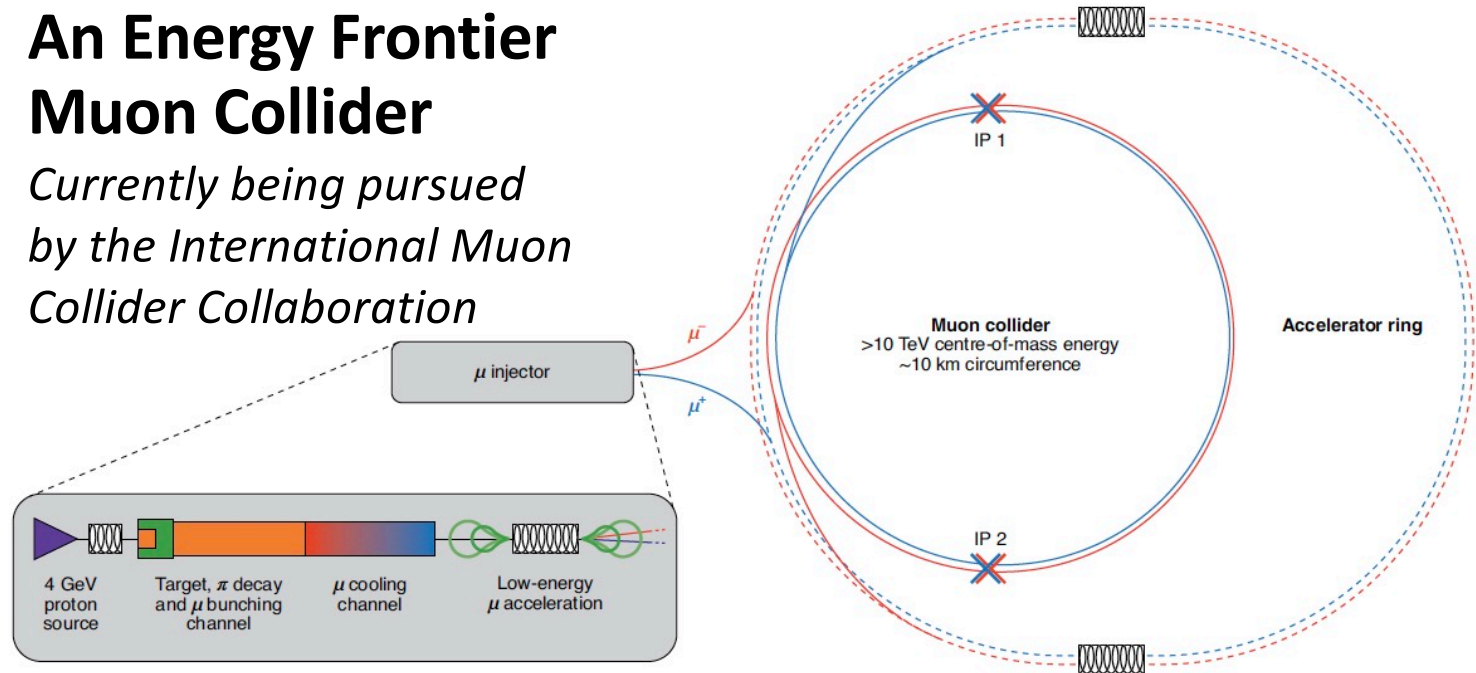


Advanced Concepts

- Emerging Options
 - Muon Collider with strong dependence on advanced magnet technology
 - Wakefield Acceleration
 - Laser-Driven Plasma
 - Beam-Driven Plasma
 - Beam-Driven Structure

An Energy Frontier Muon Collider

Currently being pursued by the International Muon Collider Collaboration





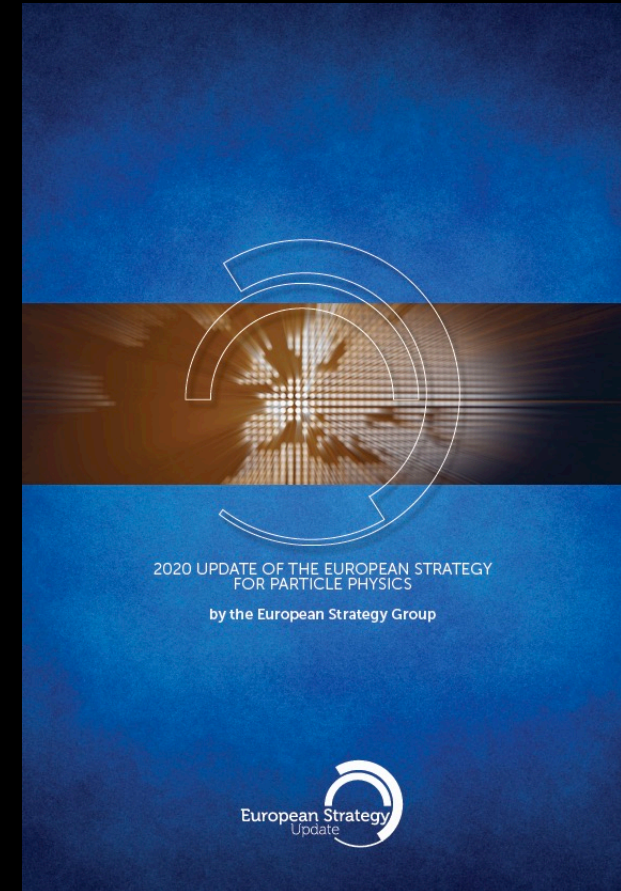
Perspectives



- Community planning processes are underway around the world
 - 2020 Update of the European Strategy for Particle Physics
 - [European Strategy Update](#)
 - European Accelerator R&D Roadmap presently in preparation
 - US Snowmass Community Planning Process will continue through mid-2022
 - [Snowmass](#)



A major focus of each effort is the technology required to deliver an Energy Frontier discovery machine by roughly the middle of the century!





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Why Muons?



Physics Frontiers

- **Intense and cold muon beams** \Rightarrow **unique physics reach**

- Tests of Lepton Flavor Violation
- Anomalous Magnetic Moment (g-2)
- Precision sources of neutrinos
- Next generation lepton collider

$$m_\mu = 105.7 \text{ MeV} / c^2$$
$$\tau_\mu = 2.2 \mu\text{s}$$

Colliders

- **Opportunities**

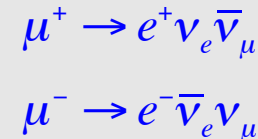
- s-channel production of scalar objects \Rightarrow strong coupling to Higgs
- Strong coupling to particles like the Higgs
- Reduced synchrotron radiation (E^4/m^4) \Rightarrow multi-pass acceleration feasible
- Beams can be produced with small energy spread
- Beamstrahlung effects suppressed at the collider IP

$$\sim \left(\frac{m_\mu^2}{m_e^2} \right) \cong 4 \times 10^4$$

- **BUT the accelerator complex and detector must be able to handle the impacts of μ decays**

Collider Synergies

- High intensity beams required for a long-baseline Neutrino Factory are readily provided in conjunction with a Muon Collider Front End
- Such overlaps offer unique staging strategies to guarantee physics output while developing a muon accelerator complex capable of supporting collider operations





$\mu^+\mu^-$ Collider Luminosity

Detector and Physics Performance at a Muon Collider
 N. Bartosik et al 2020 JINST 15 P05001



- For a muon collider, we can write the luminosity as:

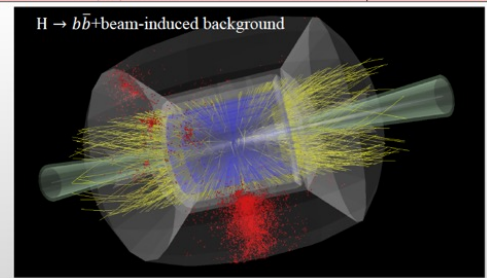
$$\mathcal{L} = \frac{N^2 f_{coll}}{4\pi\sigma_x\sigma_y} = \frac{\langle N^2 \rangle n_{turns} f_{bunch}}{4\pi\sigma_{\perp}^2}$$

- For the 1.5 TeV muon collider design, we have
 - $N = 2 \times 10^{12}$ particles/bunch
 - $\sigma_{x,y} \sim 5.9 \mu\text{m}$, $\beta^* = 10 \text{ mm}$, $\varepsilon_{x,y}(norm) = 25 \mu\text{m-rad}$
 - $n_{turns} \sim 1000 \propto 150 \langle B[T] \rangle$
 - $f_{bunch} = 15 \text{ Hz}$ (rate at which new bunches are injected)

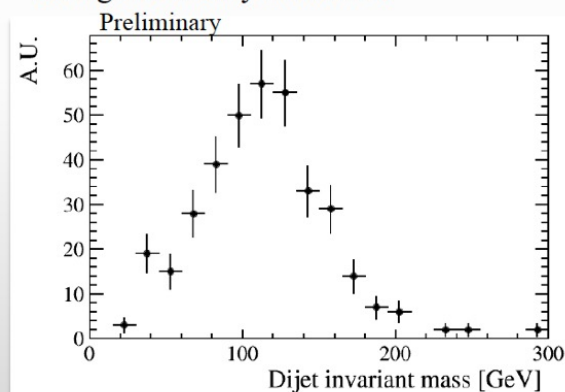
$$\mathcal{L} \approx \frac{N_0^2 n_{turns} f_{bunch}}{4\pi\sigma_{\perp}^2} \approx 1.4 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$$

$b\bar{b}$ Studies at $\sqrt{s} = 1.5 \text{ TeV}$

Process	cross section [pb]
$\mu^+\mu^- \rightarrow \gamma^*/Z \rightarrow b\bar{b}$	0.046
$\mu^+\mu^- \rightarrow \gamma^*/Z\gamma^*/Z \rightarrow b\bar{b} + X$	0.029
$\mu^+\mu^- \rightarrow \gamma^*/Z\gamma \rightarrow b\bar{b}\gamma$	0.12
$\mu^+\mu^- \rightarrow HZ \rightarrow b\bar{b} + X$	0.004
$\mu^+\mu^- \rightarrow \mu^+\mu^- H H \rightarrow b\bar{b}$ (ZZ fusion)	0.018
$\mu^+\mu^- \rightarrow \nu_{\mu}\nu_{\mu} H H \rightarrow b\bar{b}$ (WW fusion)	0.18



$\mu^+\mu^- \rightarrow H\nu\bar{\nu} \rightarrow b\bar{b}\nu\bar{\nu}$ + beam-induced background fully simulated



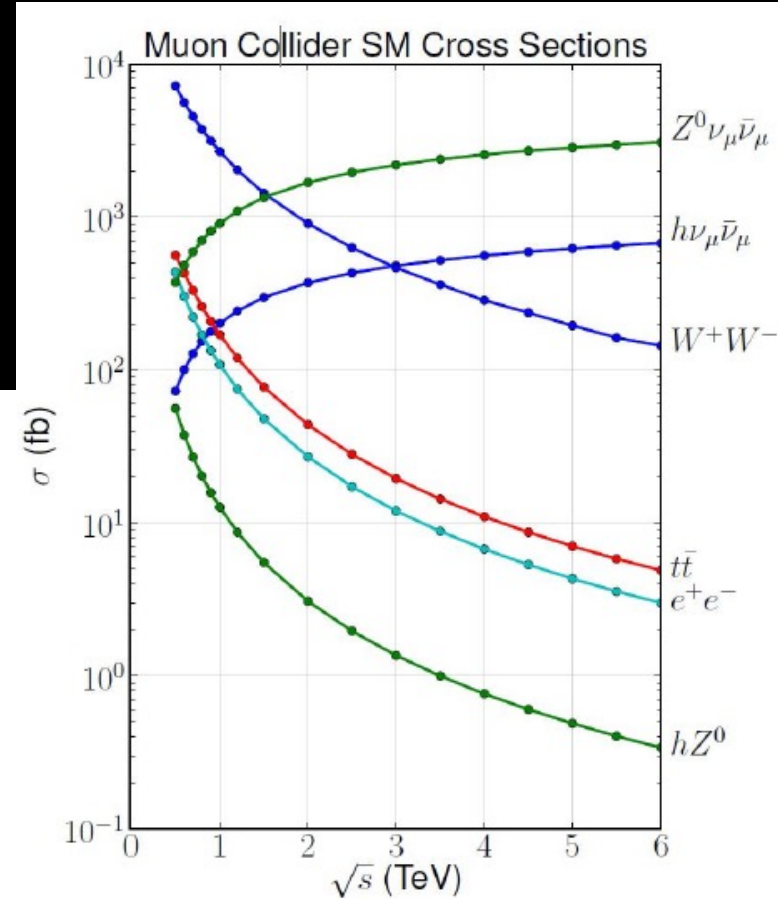
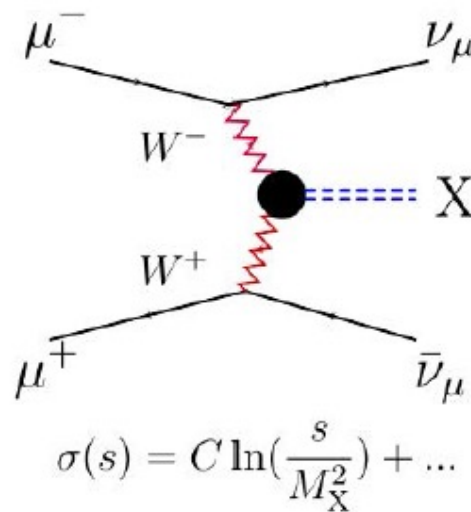
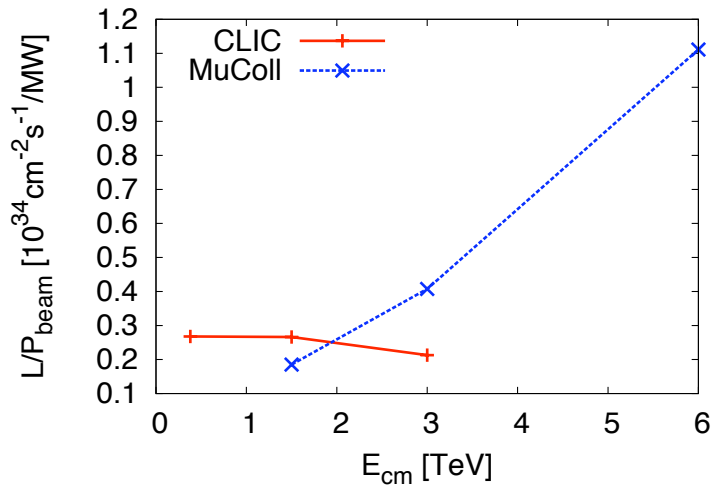


Potential as an Energy Frontier Discovery Machine



High Energy Collisions

- At $\sqrt{s} > 1$ TeV: Fusion processes dominate
 - An Electroweak Boson Collider
 - Discovery machine complementary to high energy pp collider
- At >5 TeV: Higgs self-coupling resolution $<10\%$
- Luminosity scaling at multi-TeV energies is favorable when compared to e^+e^-





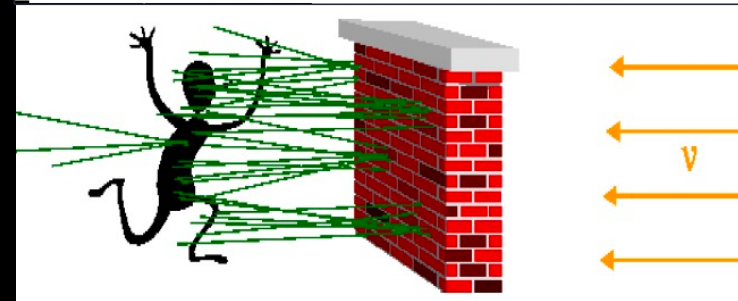
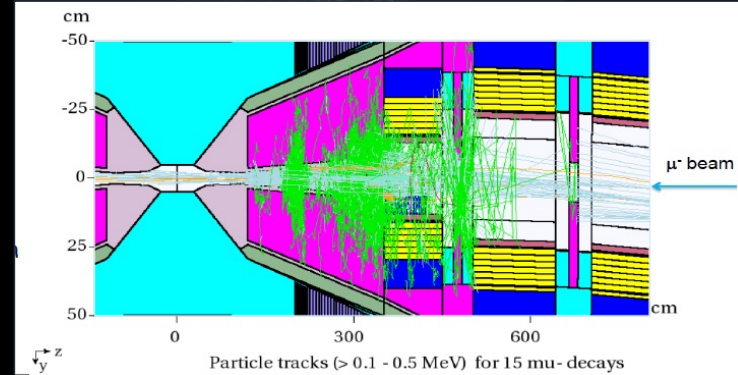
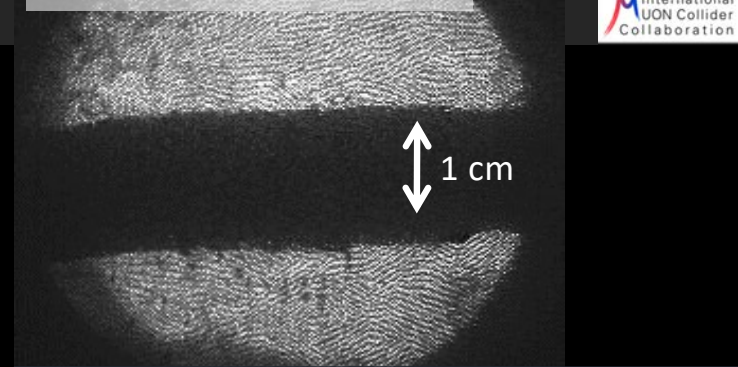
The Physics Challenges

- Muons are difficult to produce
 - Most effective route is tertiary production from a multi-MW proton beam on a target: $p \rightarrow \pi \rightarrow \mu$
 - Beams must be bunched and cooled to produce luminosity in a collider
- Muons decay
 - All beam manipulations must be rapidly carried out to deliver useable beams to a collider
 - Bunching
 - Cooling
 - Acceleration
 - Electrons from the muon decays deposit significant energy in the accelerator components and physics detector
 - Neutrinos from the muon decays can produce ionizing radiation far from the accelerator complex

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MERIT Experiment – CERN
Liquid Hg Target





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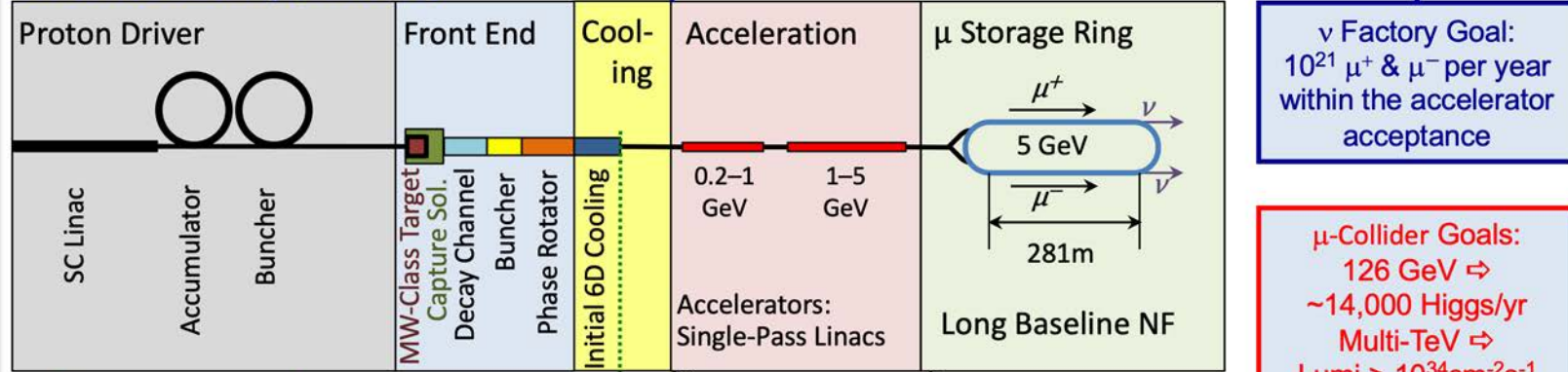
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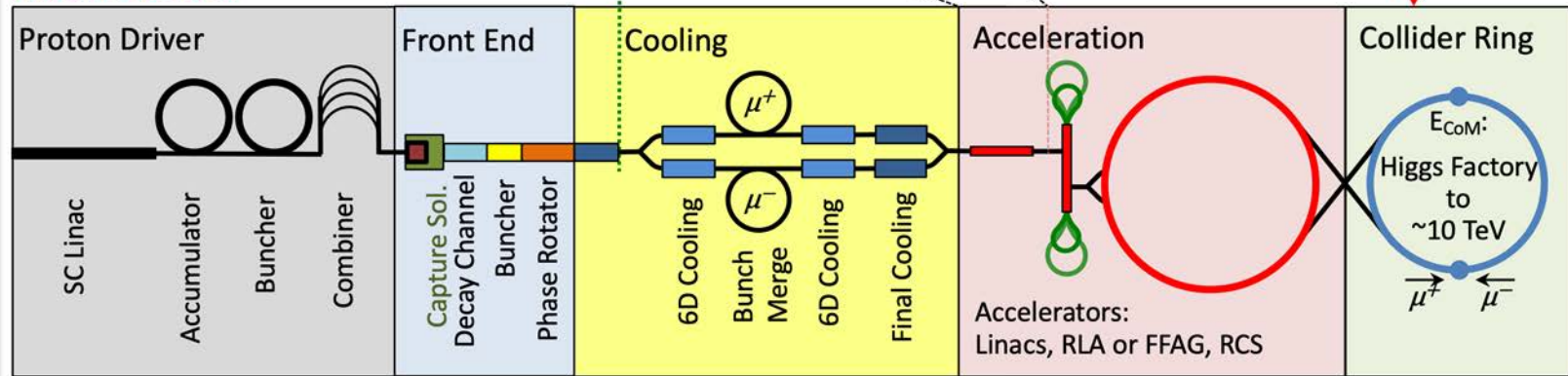
Elements of a Muon Collider (and ν Factory)

Neutrino Factory (NuMAX)



Share same complex

Muon Collider





MC Parameters as Developed by MAP

RAST, Vol 10, No. 01, pp. 189-214 (2019)



Table 3. Main parameters of the various phases of an MC as developed by the MAP effort.

Parameter	Units	Higgs	Top-high resolution	Top-high luminosity	Multi-TeV *		
CoM energy	TeV	0.126	0.35	0.35	1.5	3.0	6.0*
Avg. luminosity	$10^{34} \text{ cm}^{-2} \text{ s}^{-1}$	0.008	0.07	0.6	1.25	4.4	12
Beam energy spread	%	0.004	0.01	0.1	0.1	0.1	0.1
Higgs production/ 10^7 sec		13,500	7000	60,000	37,500	200,000	820,000
Circumference	km	0.3	0.7	0.7	2.5	4.5	6
Ring depth [1]	m	135	135	135	135	135	540
No. of IPs		1	1	1	2	2	2
Repetition rate	Hz	15	15	15	15	12	6
$\beta_{x,y}^*$	cm	1.7	1.5	0.5	1 (0.5–2)	0.5 (0.3–3)	0.25
No. muons/bunch	10^{12}	4	4	3	2	2	2
Norm. trans. emittance, ε_T	π mm-rad	0.2	0.2	0.05	0.025	0.025	0.025
Norm. long. emittance, ε_L	π mm-rad	1.5	1.5	10	70	70	70
Bunch length, σ_s	cm	6.3	0.9	0.5	1	0.5	0.2
Proton driver power	MW	4	4	4	4	4	1.6
Wall plug power	MW	200	203	203	216	230	270

* Accounts for off-site neutrino radiation

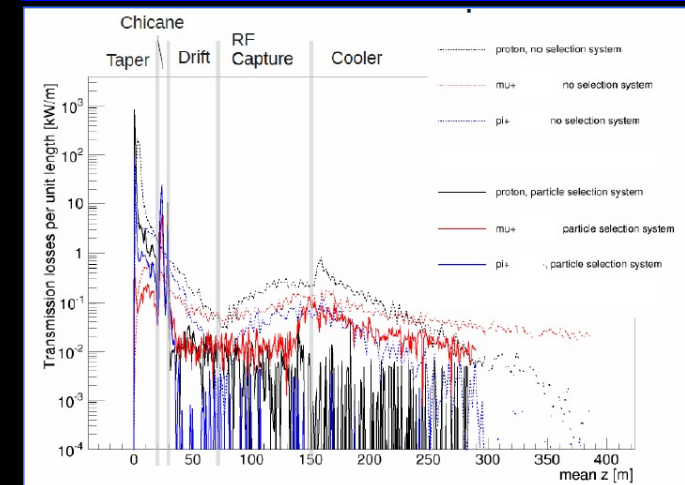
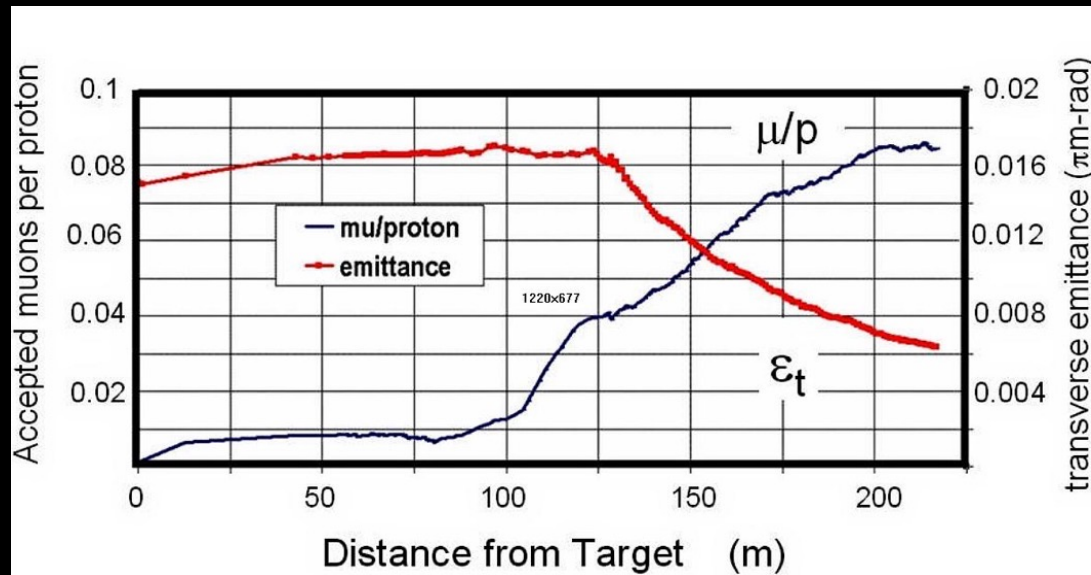
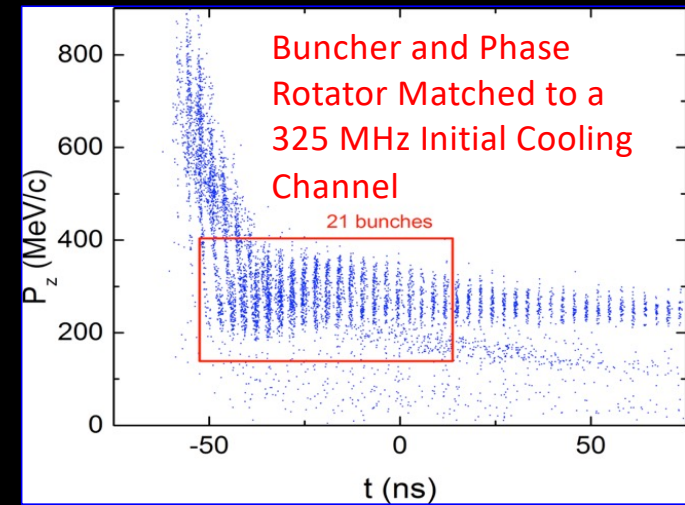
The IMCC aims for a 10+ TeV Design



Target & Capture System



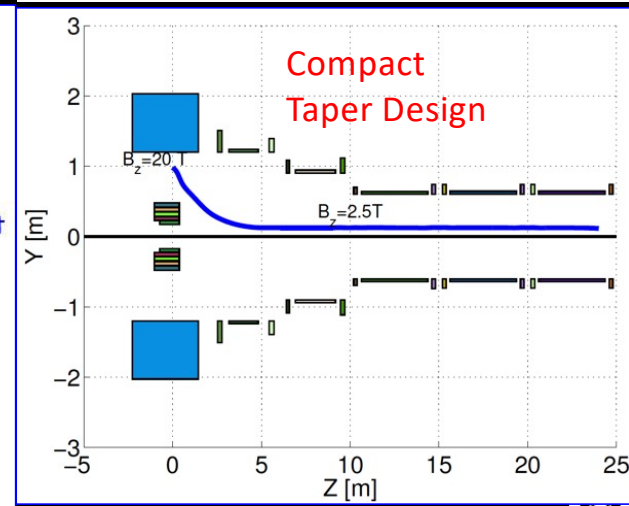
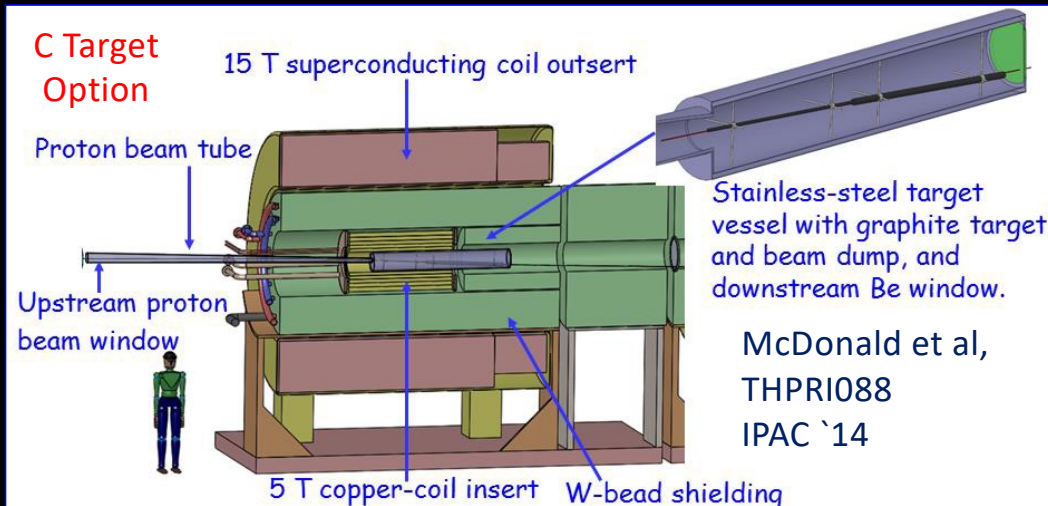
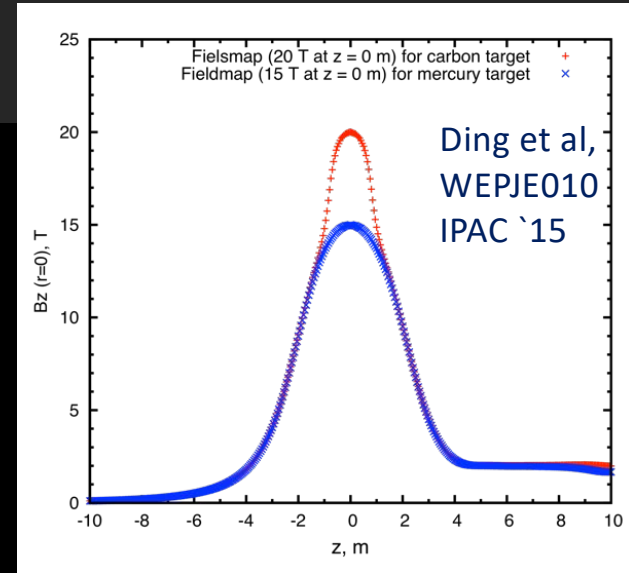
- Produce muons through tertiary production from protons on target
- Prepare the beams for the ionization cooling channel
- Requires significant radiation protection of all system components





Target & Capture Magnets

- 20T Capture Solenoid
 - Solenoid allows capture of both signs of pions
 - Initially operate with graphite target module
 - Upgrade to highest power using a liquid metal target
 - Magnet
 - 15T SC Outsert (3 GJ, 100 tons)
 - 5 T Inset: Copper \Rightarrow HTS?
 - Very high radiation environment
 - Possible use of CICC technology
 - Internal shielding required
- Solenoid Decay channel \Rightarrow taper to ~ 2.5 T guide field



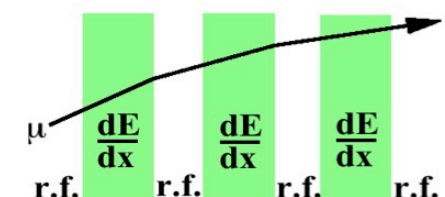


Cooling Methods



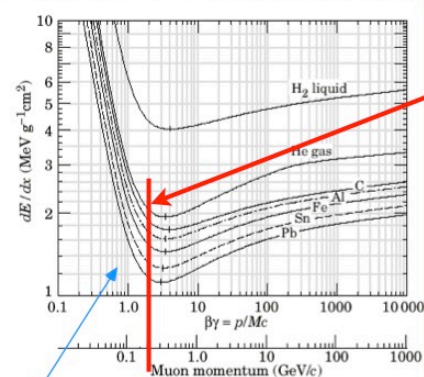
- Muon Cooling
 - Must take place very quickly
 - ⇒ Utilize energy loss in materials with RF re-acceleration
 - Operating in a solenoid-based guide field
- Equilibrium emittance in the solenoid-based lattice
 - $\epsilon_{equilib} \propto \beta_{\perp} \propto B^{-1}$
 - Large aperture HTS magnets desirable for 6D Cooling
 - Ideally 50-60 T in Final Cooling channel
 - Aperture ~50 mm (dia)
 - Synergistic with Very High Field User Magnet development

Muons cool via dE/dx in low-Z medium



- Absorbers:

$$\begin{cases} E \rightarrow E - \left\langle \frac{dE}{dx} \right\rangle \Delta s \\ \theta \rightarrow \theta + \theta_{space}^{rms} \end{cases}$$



• ionization minimum is \approx optimal working point:

- ▶ longitudinal +ive feedback at lower p
- ▶ straggling & expense of reacceleration at higher p

• 2 competing effects \Rightarrow \exists equilibrium emittance

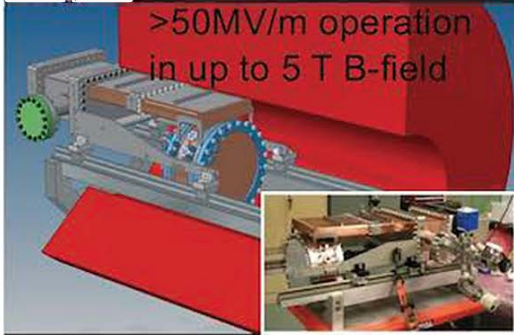
- RF cavities between absorbers replace ΔE
- Net effect: reduction in p_{\perp} at constant p_{\parallel} , i.e., transverse cooling

$$\frac{d\epsilon_N}{ds} \approx -\frac{1}{\beta^2} \left(\frac{dE_{\mu}}{ds} \right) \frac{\epsilon_N}{E_{\mu}} + \frac{\beta_{\perp} (0.014 \text{ GeV})^2}{2\beta^3 E_{\mu} m_{\mu} X_0}$$

(emittance change per unit length)

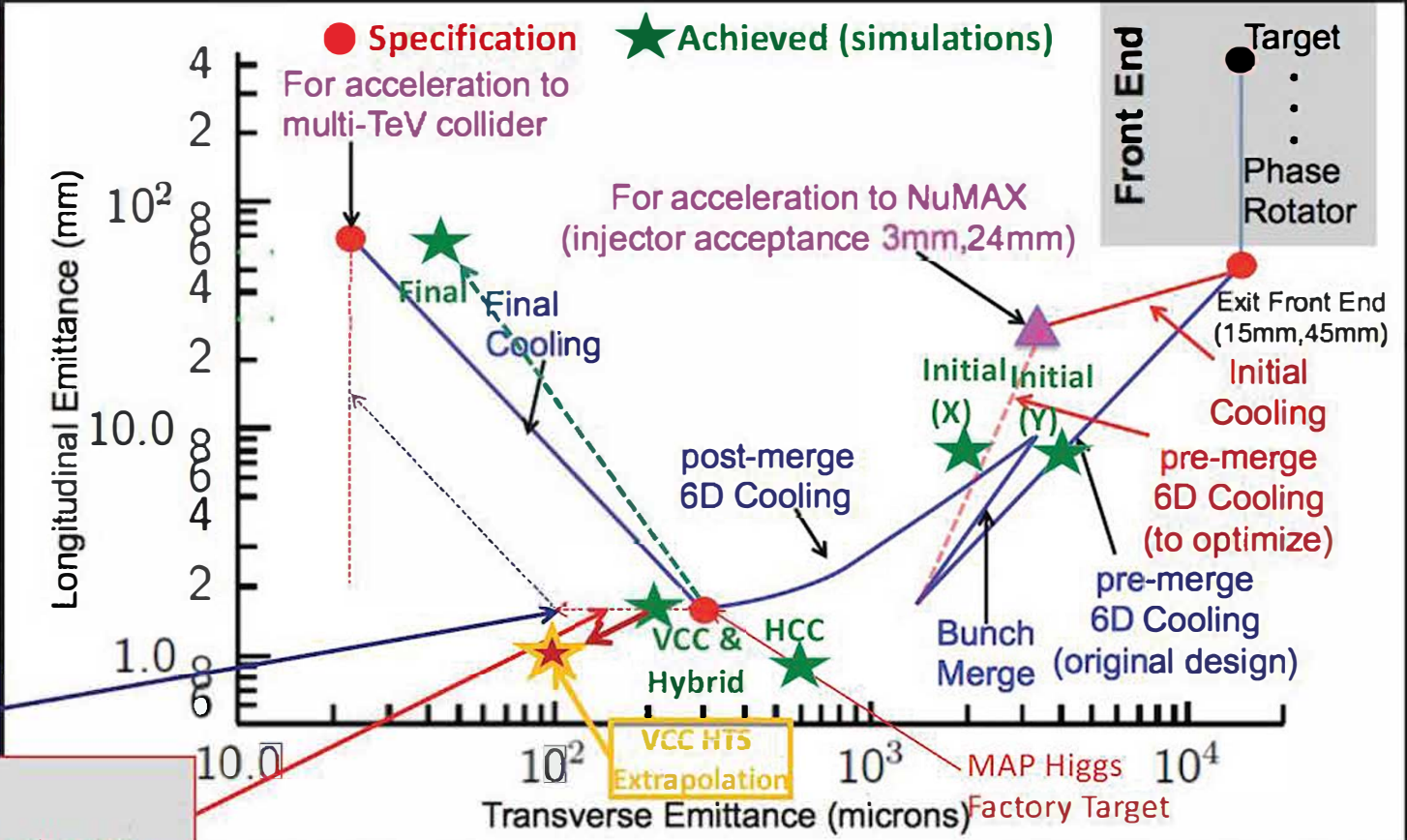


Ionization Cooling



PIC assumed in Carlo Rubbia's Proposal

Advanced techniques \Leftrightarrow
 Improved HF Luminosity
 Simplified Final Cooling requirements





6D Cooling

- Initial Cooling
 - RF Cavities inside focusing solenoids
 - Wedge absorber materials
 - Ability to cool both signs of muons simultaneously
 - $\varepsilon_{6D} \ 60 \text{ cm}^3 \Leftrightarrow \sim 50 \text{ mm}^3$; Trans = 67%

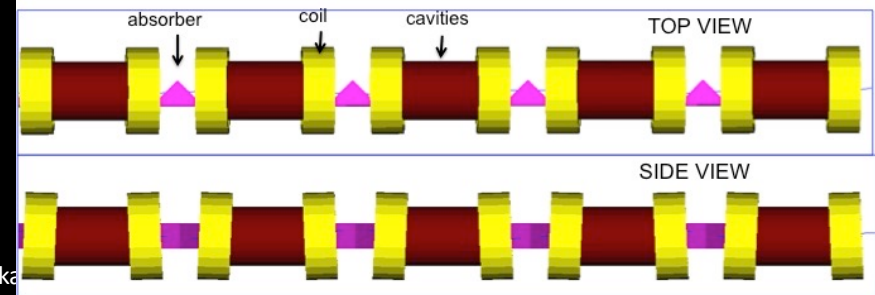
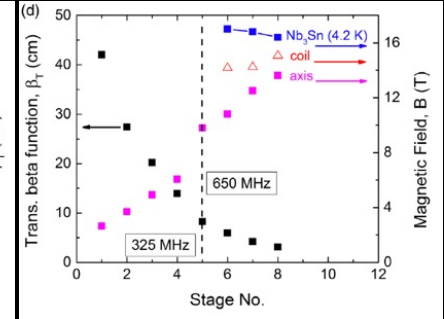
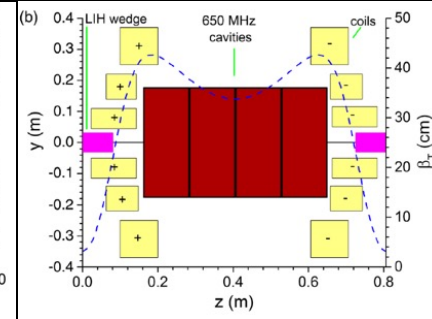
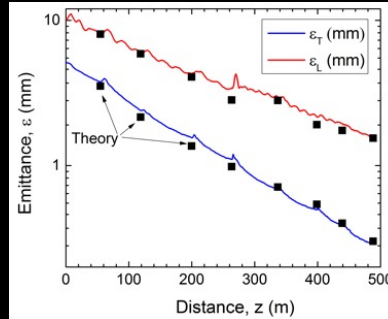
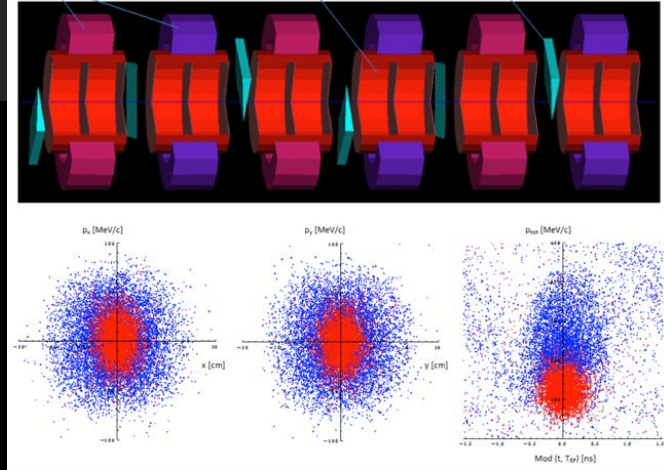
Rectilinear Cooling Channel

- Current design uses Nb₃Sn coils
 $\varepsilon_T = 0.28 \text{ mm}$, $\varepsilon_L = 1.57 \text{ mm}$
 Transmission = 55%(40%)
 w/o(with) bunch recombination
- Next step to extend performance to HTS coils
- Helical Cooling Channel is an alternative 6D Cooling design

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coils: $R_{in}=42\text{cm}$, $R_{out}=60\text{cm}$, $L=30\text{cm}$; RF: $f=325\text{MHz}$, $L=2 \times 25\text{cm}$; LIH wedges

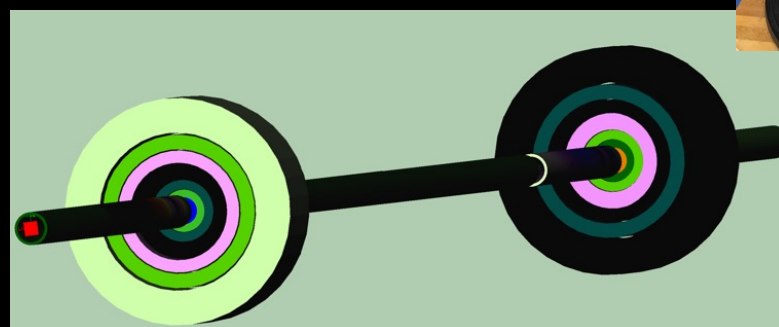
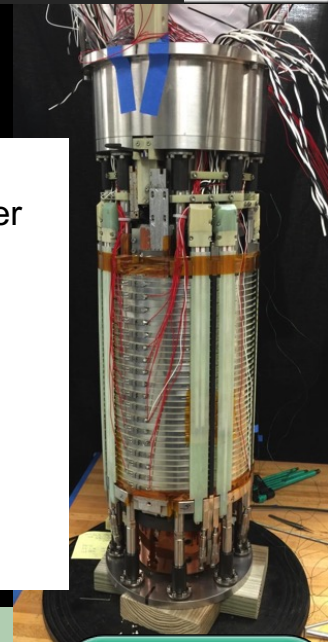
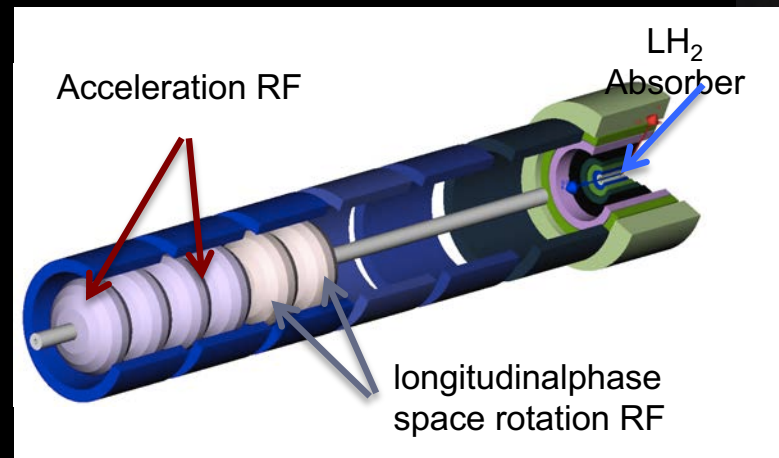
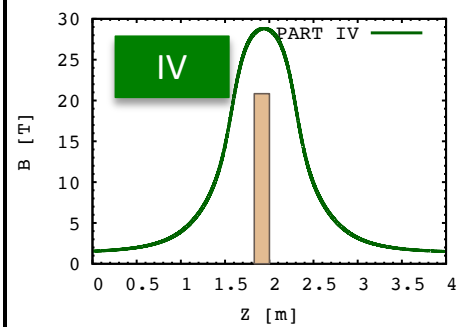
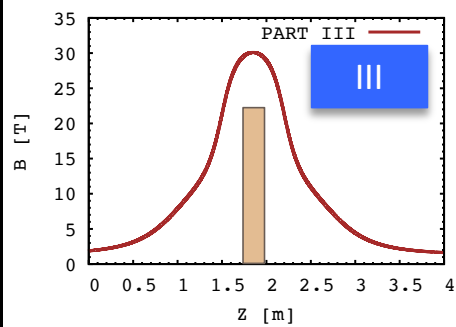
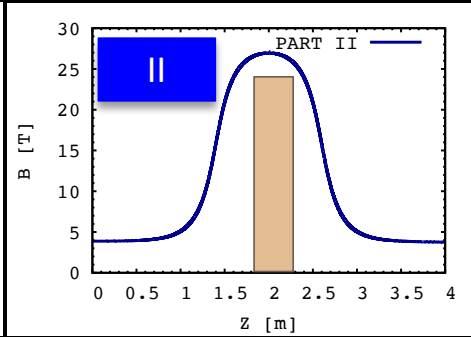
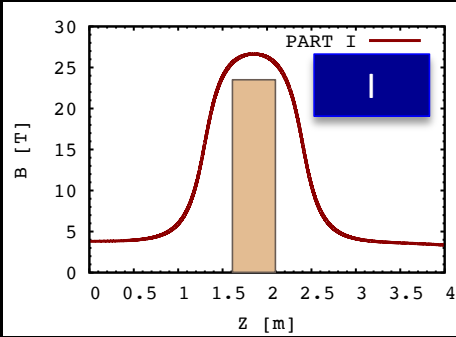
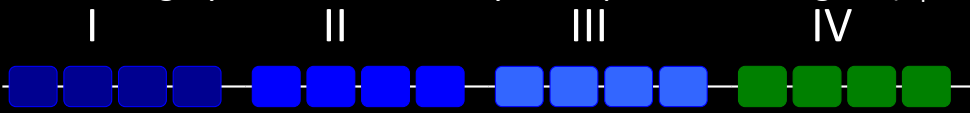




Final Cooling



- Performance studies with ~ 30 T limit
- Roughly a factor of 2 away from performance goal ($\epsilon_T = 55\mu\text{m}$, $\epsilon_L = 75\text{mm}$)



World Record
LTS-HTS
Hybrid
Magnet
 32T on-axis field
NHFML



Cooling Channel Magnet Pull



- 6D Cooling Requires:
 - Large-bore high field magnets
 - RF cavities must fit within the magnet structure
 - Space required for cryogenic design
 - HTS Solenoid development will directly enable higher performance
 - Structural engineering of cryomodules will be challenging
- Final Cooling:
 - Magnets are separated from acceleration elements
 - Bores of ~50mm diameter required
 - Very high field solenoid development improves performance linearly with field
 - Ideal range to deliver MC parameter sets: 50-60 T [30-40 T acceptable]



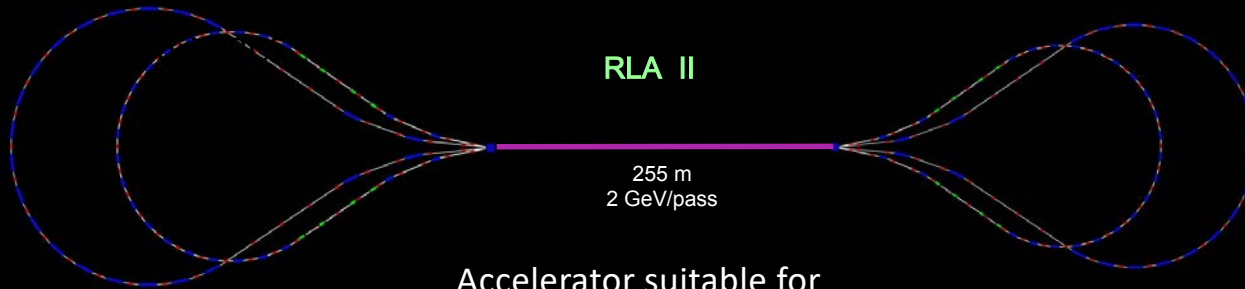
Acceleration

Technologies Include:

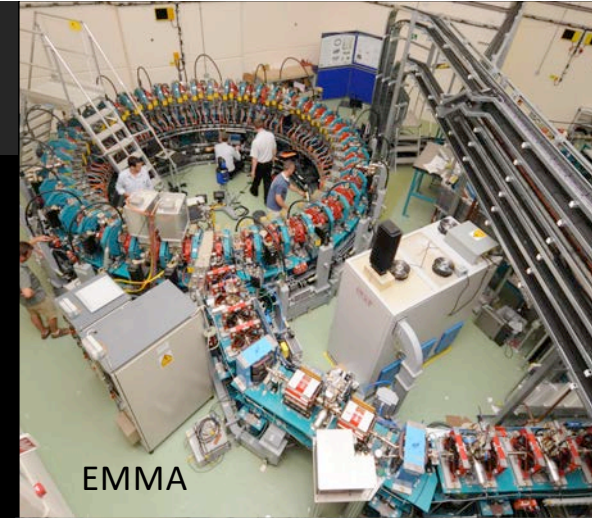
- Superconducting Linacs
- Recirculating Linear Accelerators (RLAs)
- Fixed-Field Alternating-Gradient Rings (FFAs)
- Hybrid Rapid Cycling Synchrotrons (magnetic field ramps with RF acceleration)

Designs to
125 GeV CoM

Needed for
Multi-TeV Scale



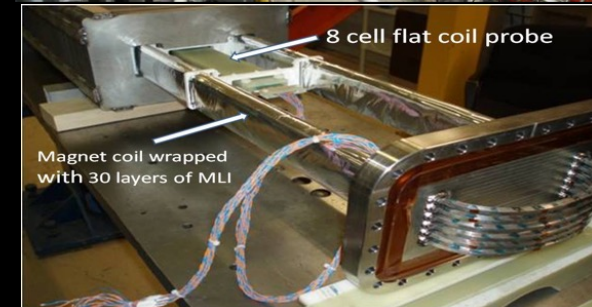
Accelerator suitable for
Neutrino Factory Applications



EMMA



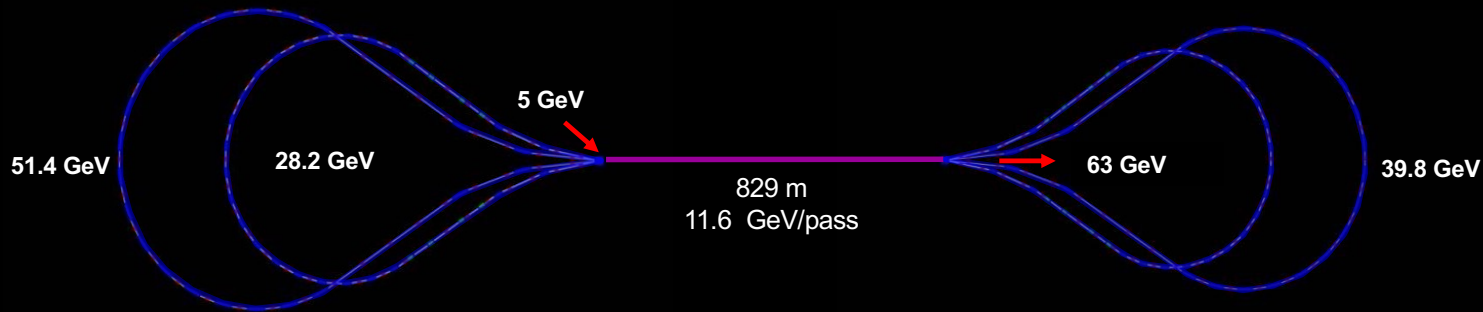
CBeta @ Cornell



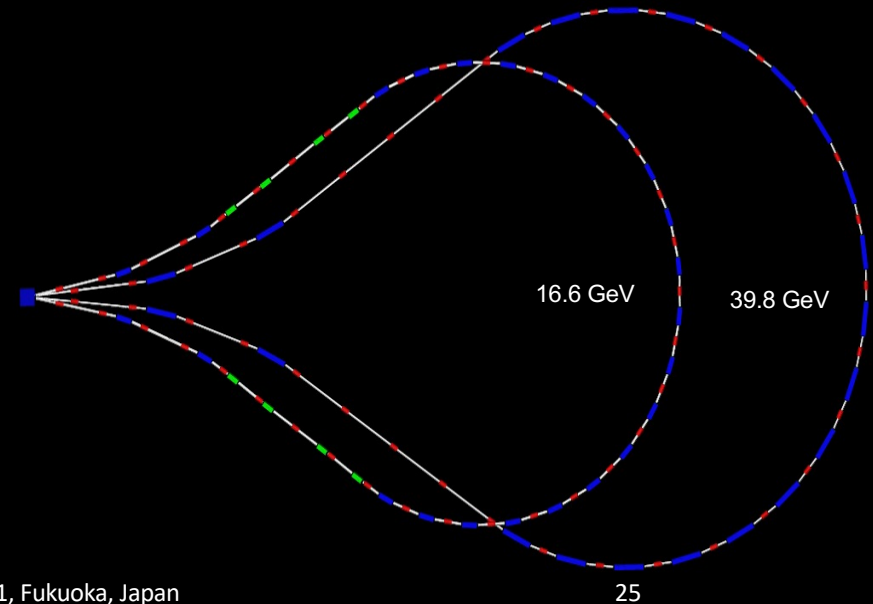
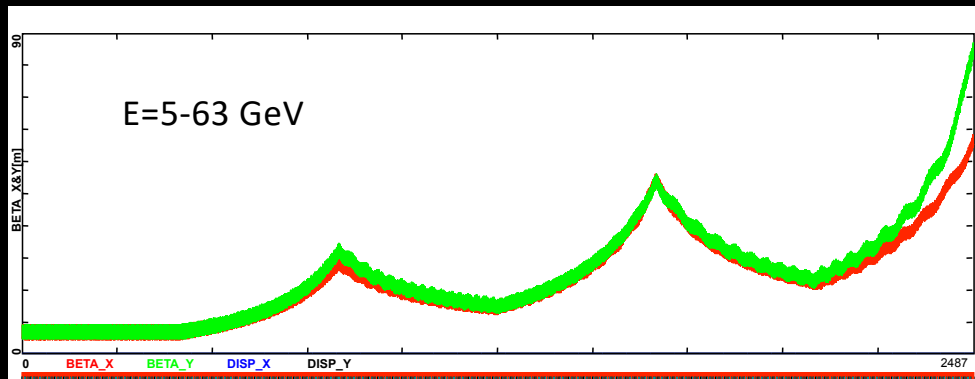
8 cell flat coil probe
Magnet coil wrapped with 30 layers of MLI



Acceleration to 125 GeV Center-of-Mass



Magnet Pull: Arcs benefit from application of FFA concepts to maximize energy bandwidth
See, for instance: [CBETA: First Multipass Superconducting Linear Accelerator with Energy Recovery](#) Phys. Rev. Lett. 125, 044803, July 2020



RF: $f = 650$ MHz cells/cavity = 5 Gradient = 25 MV/m phase = 22°

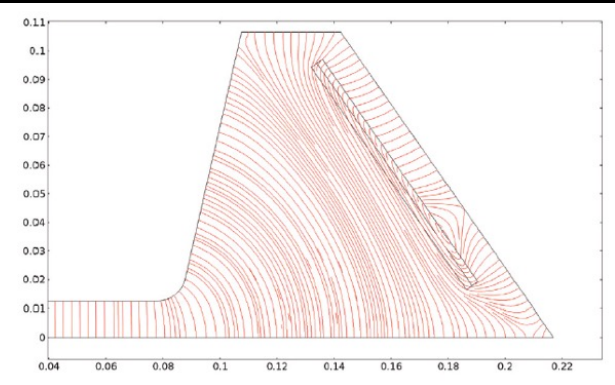
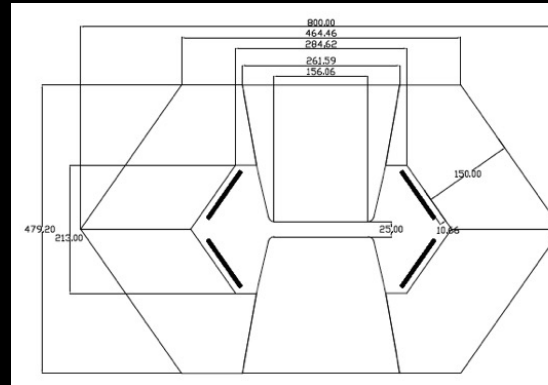


TeV-Scale Acceleration

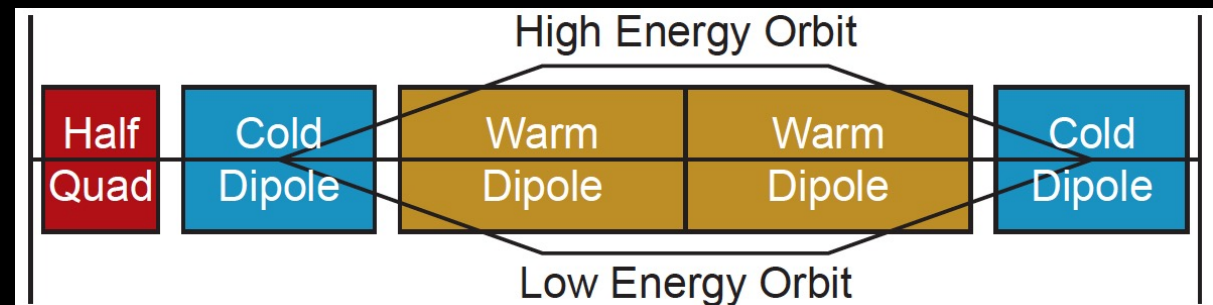


Challenges:

- Large energy bandwidth lattice at high energies
- Fast-ramping magnets
 - Grain-oriented silicon steel can support ramp rates at the kT/s level
 - Modeling remains a challenge
 - Eddy currents
 - Anisotropy
- Power supply system efficiency at high ramp rates must be demonstrated

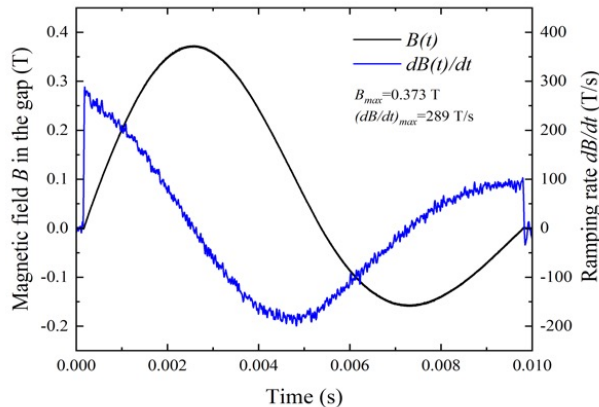


Hybrid Rapid Cycling
Synchrotron Cell Concept



Advances in Fast Ramping HTS Magnets

- $dB/dt = 289 \text{ T/s}$ demonstrated (H. Piekarz, this conference)
- TeV-class muon acceleration ideally wants $>1000 \text{ T/s}$ (E. Barzi, this conference)
- Power system with acceptable dissipation also challenging



November 18, 2021



MT27, November 15-19, 2021, Fukuoka, Japan

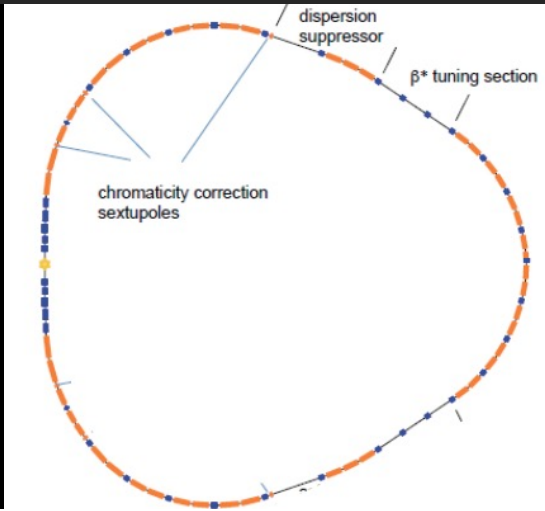
27



Higgs Factory (125 GeV) Lattice Design



MC Higgs Factory:
 MAP design
 with a single IP



Alexahin, et al., JINST 13 P11002

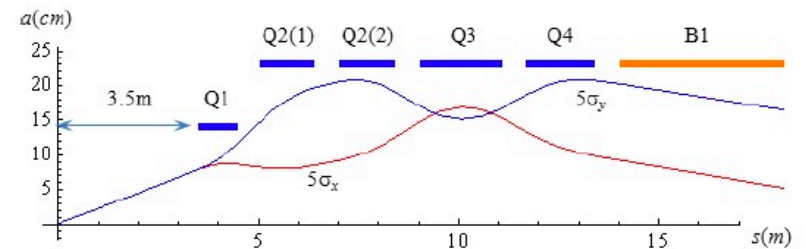


Figure 12. Higgs factory IR quadrupoles aperture and 5σ beam envelopes for $\beta^* = 2.5$ cm. Beam parameters are given in table 3.

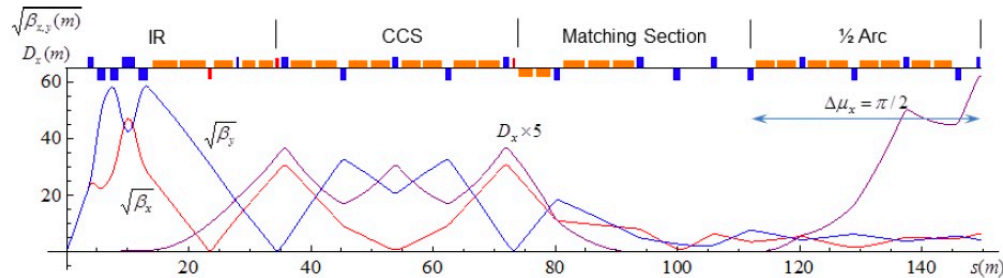


Figure 13. Layout and optics functions in half ring of the Higgs factory.

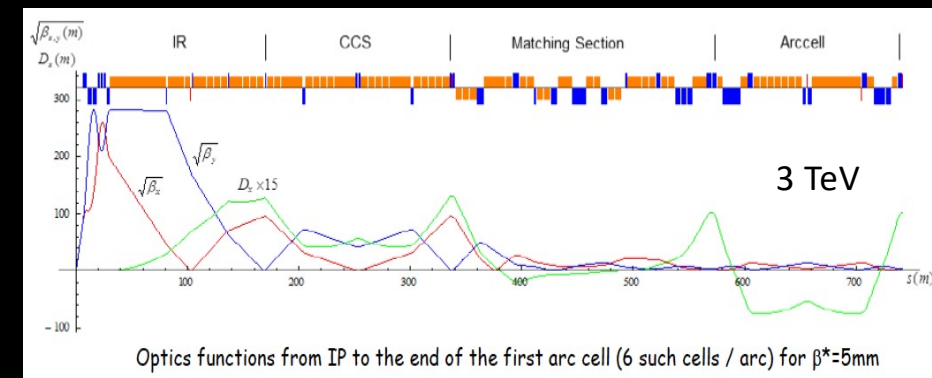
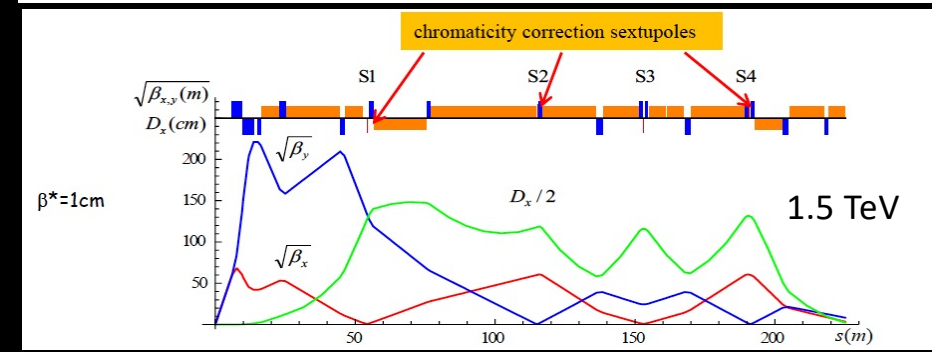
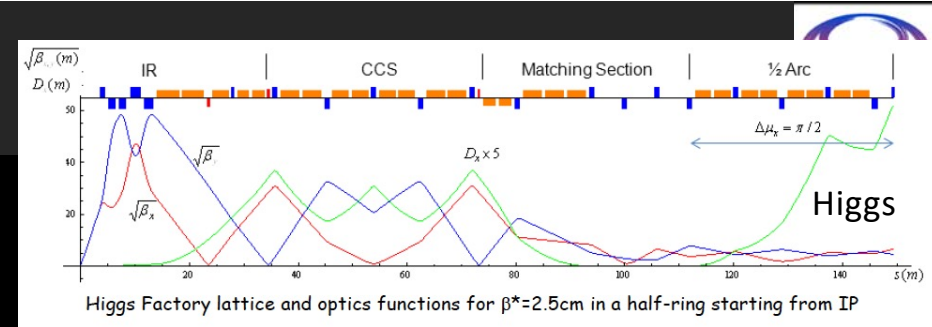
Table 4. Higgs Factory IR Magnet Specifications

Parameter	Q1	Q2	Q3	Q4	B1
Aperture (mm)	270	450	450	450	450
Gradient (T/m)	74	-36	44	-25	0
Dipole field (T)	0	2	0	2	8
Magnetic length (m)	1.00	1.40	2.05	1.70	4.10



Multi-TeV Colliders

- MAP Optics Designs for
 - Higgs Factory (125 GeV)
 - 1.5 TeV CoM
 - 3.0 TeV CoM
 - 6.0 TeV CoM
- Magnet Characteristics
 - MAP designs assumed $B_{\text{dipole}} \sim 10$ T
 - Higher is better \Rightarrow strong coupling to HFM R&D Program
 - MC luminosity $\propto B_{\text{dipole}}$
 - Large apertures required to accommodate shielding around beam
 - Muon decays \Rightarrow radiation loads $O(\text{kW}/\text{m})$
 - Particularly an issue for the Interaction Region magnets
 - IR combined function magnets to mitigate ν radiation

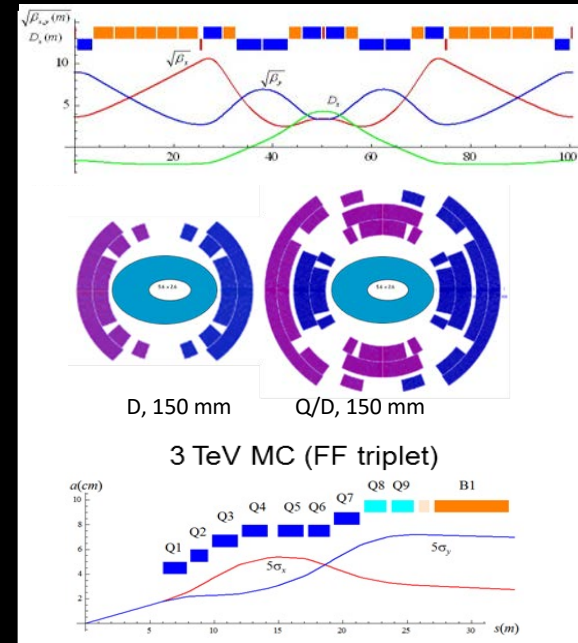




A look at the 3 TeV Collider Magnets

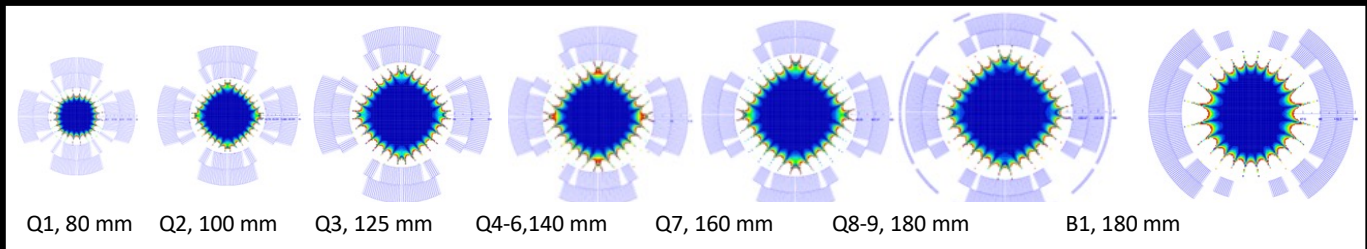
- Arc magnets

- $B_{op}=10.4$ T, $G_{op}=31-85$ T/m, $B_{op}=8-9$ T, 56 mm×26 mm
- 15 cm aperture cos θ D and combined Q/D
- Elliptical liner with shifted bore
- Results
 - $B_{op}=10.4$ T with ~30% margin at 4.5 K => 2-layer coils
 - $B_{op}\sim 8-9$ T and $G_{op}\sim 80$ T/m with ~20% margin ($B_{coil}\sim 18$ T) at 4.5 K => nested Q/D with 4-layer coils



- IR magnets

- $B_{op}=8$ T (D), $B_{op}\sim 11$ T (Q)
- Aperture 80-180 mm
- Results
 - $B_{des}=14-15$ T with 2-layer coils
 - 20-30% (Q) and 45% (D) operation margin



- Tungsten masks and inner absorbers

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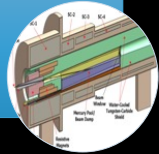
MT27, November 15-19, 2021, Fukuoka, Japan



Summary of the Muon Collider Magnet Pull

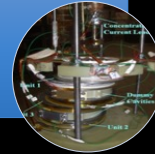
- Characteristics:
 - High field (15-20T)
 - Large bore (meter-scale)
 - Intense radiation environment
 - NC or HTS insert coil

Capture Solenoid for Simultaneous mu+ & mu- Beams



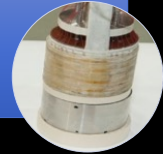
- Characteristics:
 - Solenoid-based cooling channel (LH₂/LiH absorbers)
 - RF cavities integral to focusing channel
 - Fields ranging from LTS to HTS conductor regime

Muon Ionization 6-Dimensional Cooling Channel



- Characteristics:
 - Emittance exchange channel for TeV-scale colliders – trade increased longitudinal beam emittance for smaller transverse emittance
 - Goal: 40-60 T HTS solenoids with d ~ 50mm

Muon Ionization Final Cooling Channel



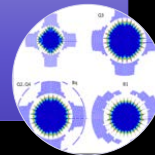
- Characteristics:
 - Present baseline based on the use of Rapid Cycling Synchrotrons
 - Requires magnets capable of ~400Hz operation with B>1.5T
 - Novel magnets, suitable modeling, efficient power system

Acceleration to the TeV Energy Scale for Muon Colliders



- Characteristics:
 - Decaying muon beams mean that luminosity is inversely proportional to circumference
 - 10T dipole ⇒ 15-20T dipoles improves luminosity
 - Radiation environment
 - Challenging IR magnets

Muon Collider Magnet Needs



- Characteristics:
 - A MC (w/decaying beams) obtains the greatest performance enhancement of any HEP collider from HTS magnet technology
 - High quality HTS cables and magnets must be a priority

HTS Magnet Development





Looking Forward...



- Muon Colliders offer an energy-efficient path to multi-TeV CoM energies
- Recent physics studies indicate that important collider physics is accessible
- The MAP R&D Program and the MICE Experiment have demonstrated the feasibility of key accelerator physics concepts
- A new International Muon Collider Collaboration is now leading the design effort with the goal of being able to deliver a multi-TeV muon collider sometime in the 2040s
- ***This effort needs the strong engagement of the magnet community in order to succeed!***



Some Useful References and Links



- Muon colliders to expand frontiers of particle physics, K.R. Long et al., Nature Physics **17**, pp 289–292 (2021)
- The Future Prospects of Muon Colliders and Neutrino Factories, Boscolo, Delahaye, Palmer, RAST, Vol 10, No. 01, pp. 189-214 (2019)
- The JINST dedicated volume on Muon Collider Research and Technology: Muon Accelerators for Particle Physics
<https://iopscience.iop.org/journal/1748-0221/page/extraproc46>
- Demonstration of cooling by the Muon Ionization Cooling Experiment, MICE Collaboration, Nature 578, 53-59(2020)
- [The International Muon Collider Collaboration](#)



Thank you for your
attention!