



# High-precision pulse-driven AC Josephson voltage standard up to 1 V at PTB

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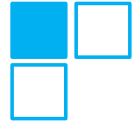
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# outline



- 1. Principle PJVS and JAWS**
- 2. 1 V JAWS @ PTB**
  - a) design**
  - b) fabrication**
  - c) setup**
  - d) overview : features**
- 3. Precision of JAWS**
  - a) comparison JAWS vs. JAWS**
  - b) comparison JAWS vs. QVM**
- 4. Summary**

# outline

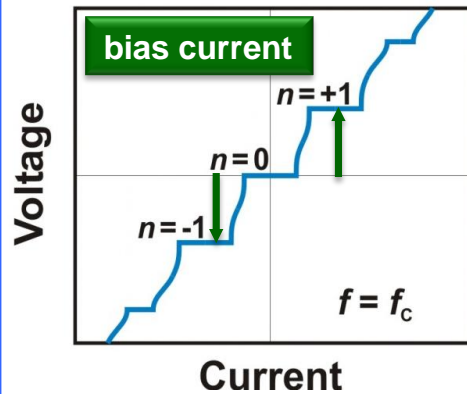
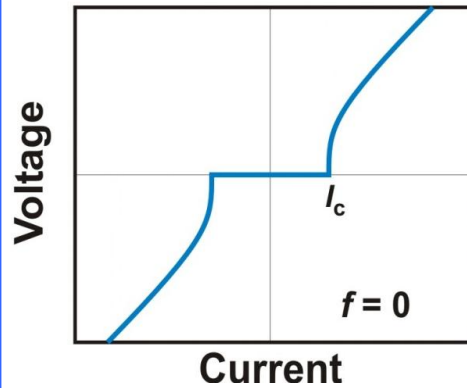


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# AC-QVM : Design of PJVS



SNS junctions :  
non-hysteretic IVC

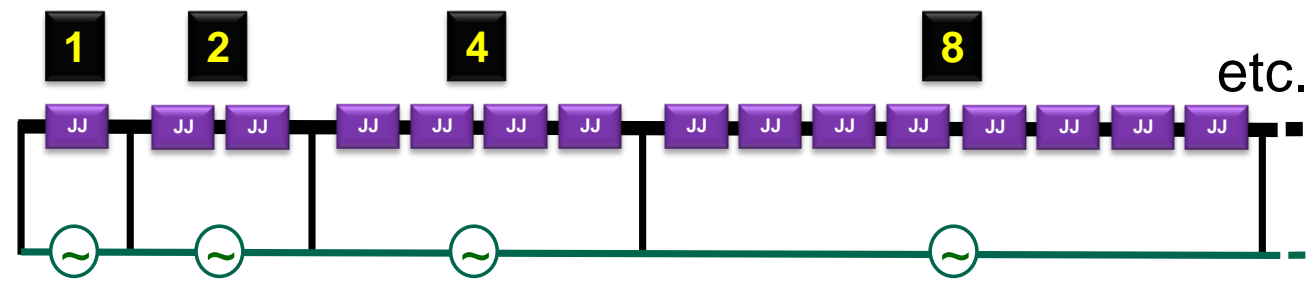


70 GHz : CW

AC-QVM : is based on  
Programmable Josephson Voltage Standard



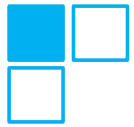
Josephson Junctions are arranged  
in a **binary** sequence



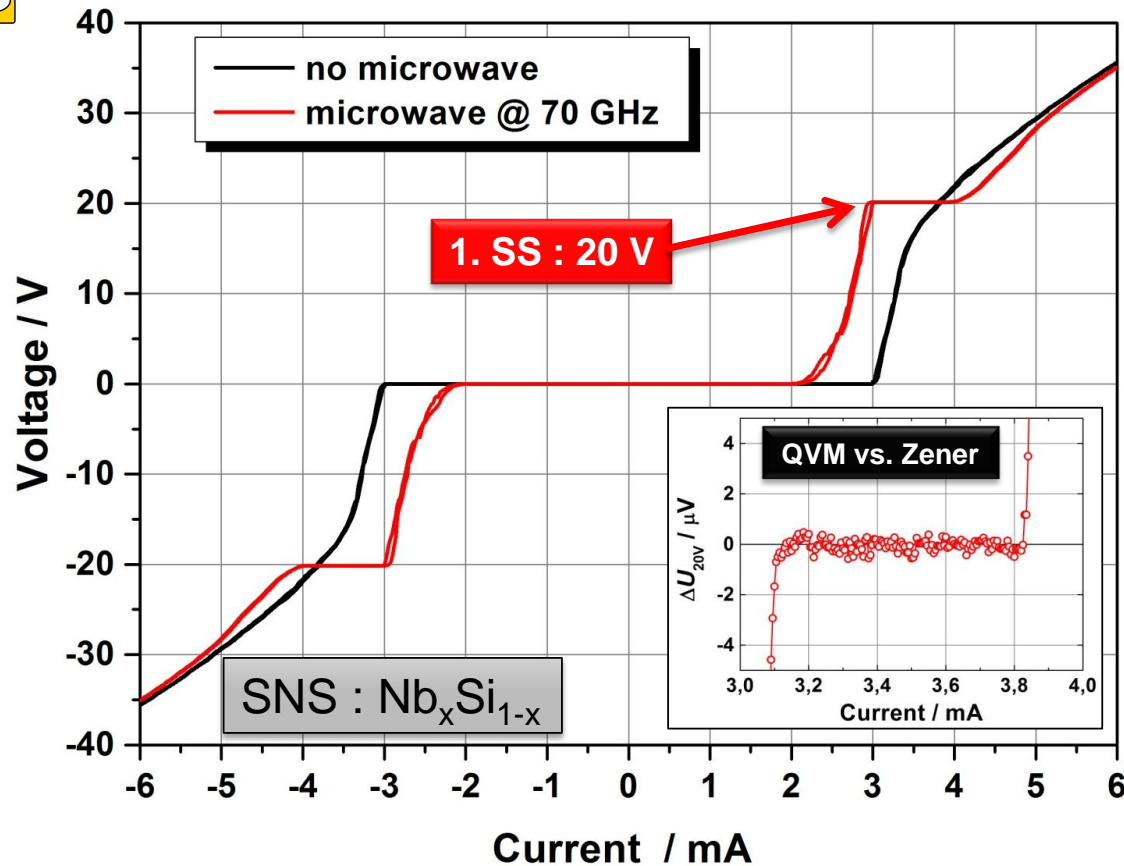
fast multi-channel current bias source

1 V PJVS	: 8192 junctions	: 1,2,4,...,4096
10 V PJVS	: 69632 junctions	: 1,2,4,...,17,34,...,34816





# PJVS circuits : 10 V and 20 V



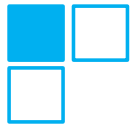
2008 worldwide first  
10 V SNS @ 70 GHz

2012 worldwide first  
20 V SNS @ 70 GHz



PTB circuits in  
more than  
20 countries

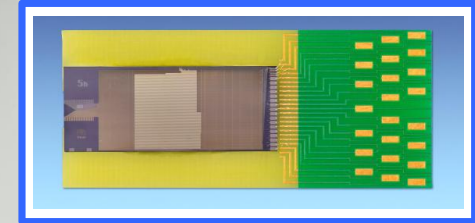
10 V : 69 632 junctions  
20 V : 139 264 double-stacked junctions



# PJVS : AC-Quantum Voltmeter



- electronics : commercially available
- computer controlled



commercially available by SUPRACON



# JAWS : principle of pulse-mode



idea and first realization : S.P. Benz and C.A. Hamilton, *Appl. Phys. Lett.* 68 (1996) 3171

a current pulse ( pulse repetition frequency  $f_p$  ) transfers  $N$  flux-quanta  $\Phi_0 = h/2e$  through a Josephson junction (number of junctions  $M$  ).

pulse repet. freq.  $f_p = \text{const.}$

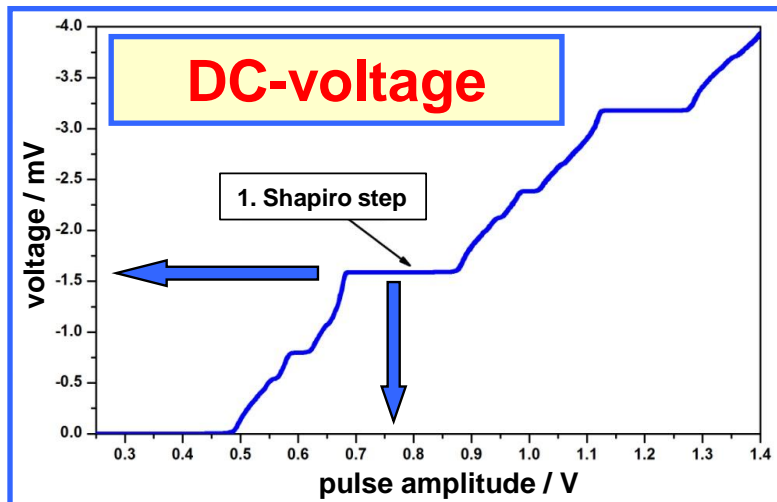
Josephson-equation :

$$V_{DC} = M \cdot N \cdot \Phi_0 \cdot f_p$$

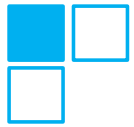
pulse repet. freq.  $f_p \neq \text{const.}$

Josephson-equation in pulse-mode :

$$V_{AC}(t) = M \cdot N \cdot \Phi_0 \cdot f_p(t)$$



AC-voltage  
arbitrary waveform

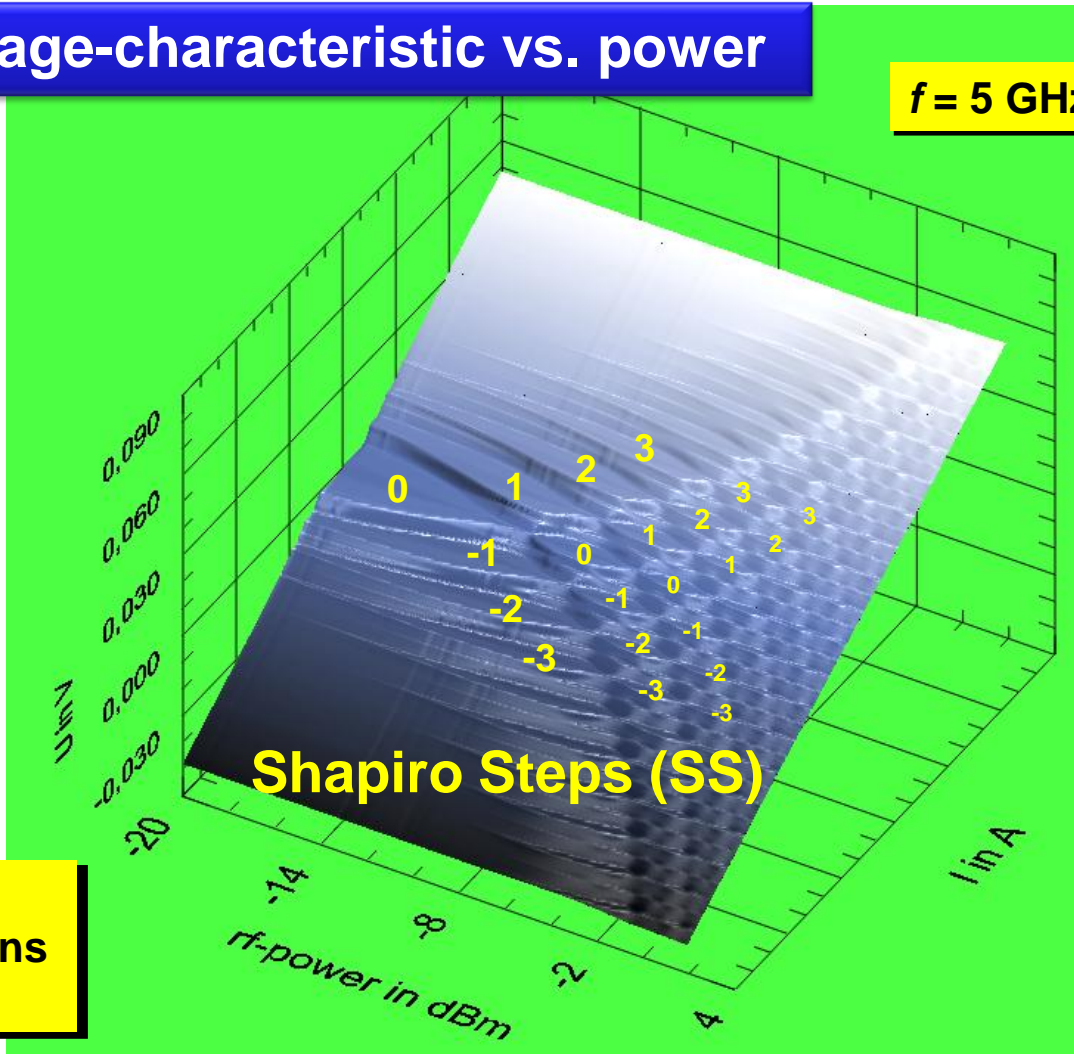


# JAWS : Shapiro steps vs. power (I)

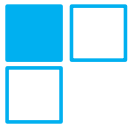


current-voltage-characteristic vs. power

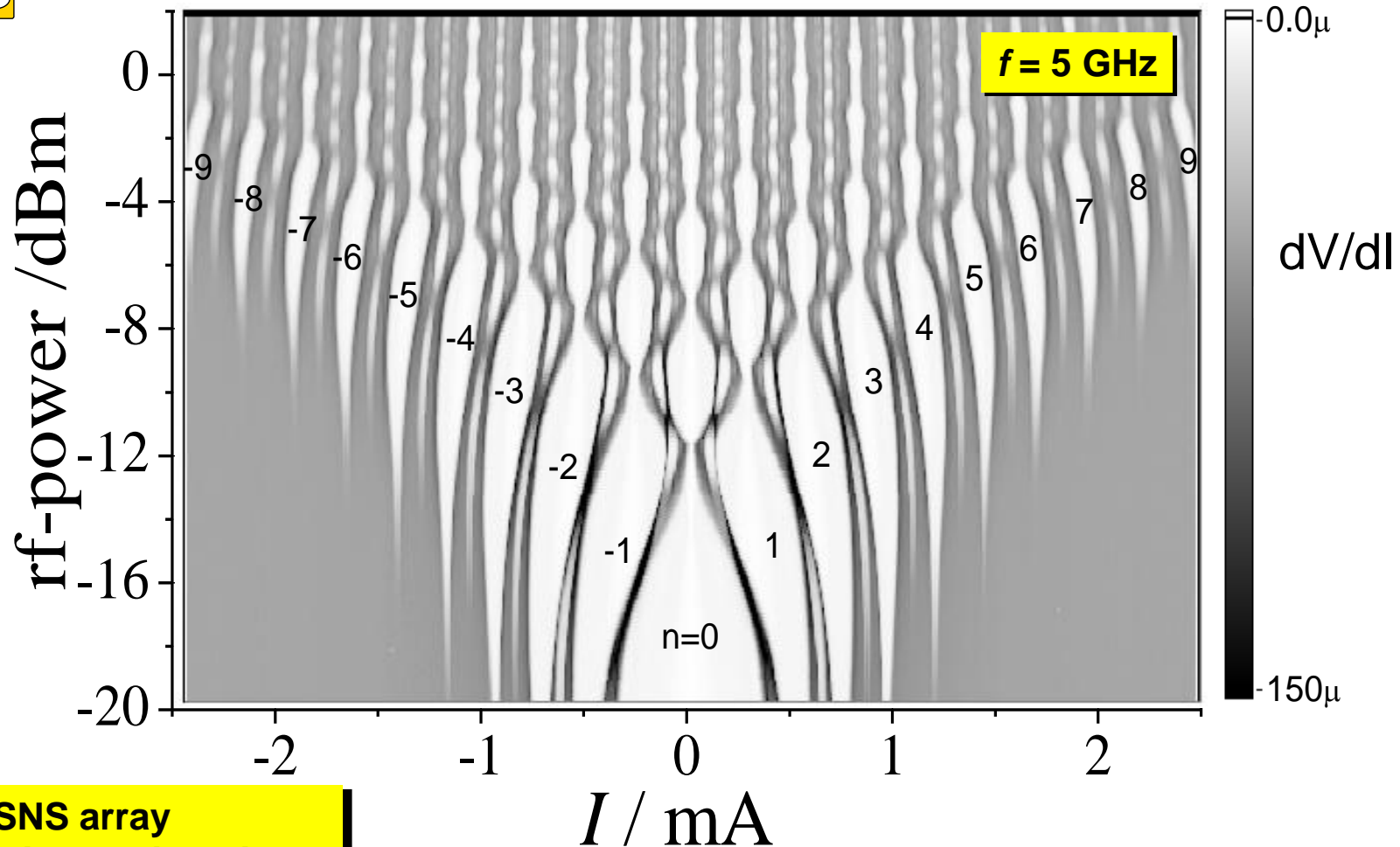
$f = 5 \text{ GHz}$



SNS array  
with 512 junctions  
( $0.7 \times 0.7 \mu\text{m}^2$ )



## JAWS : Shapiro steps vs. power (II)



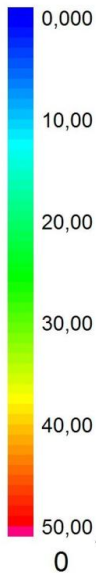
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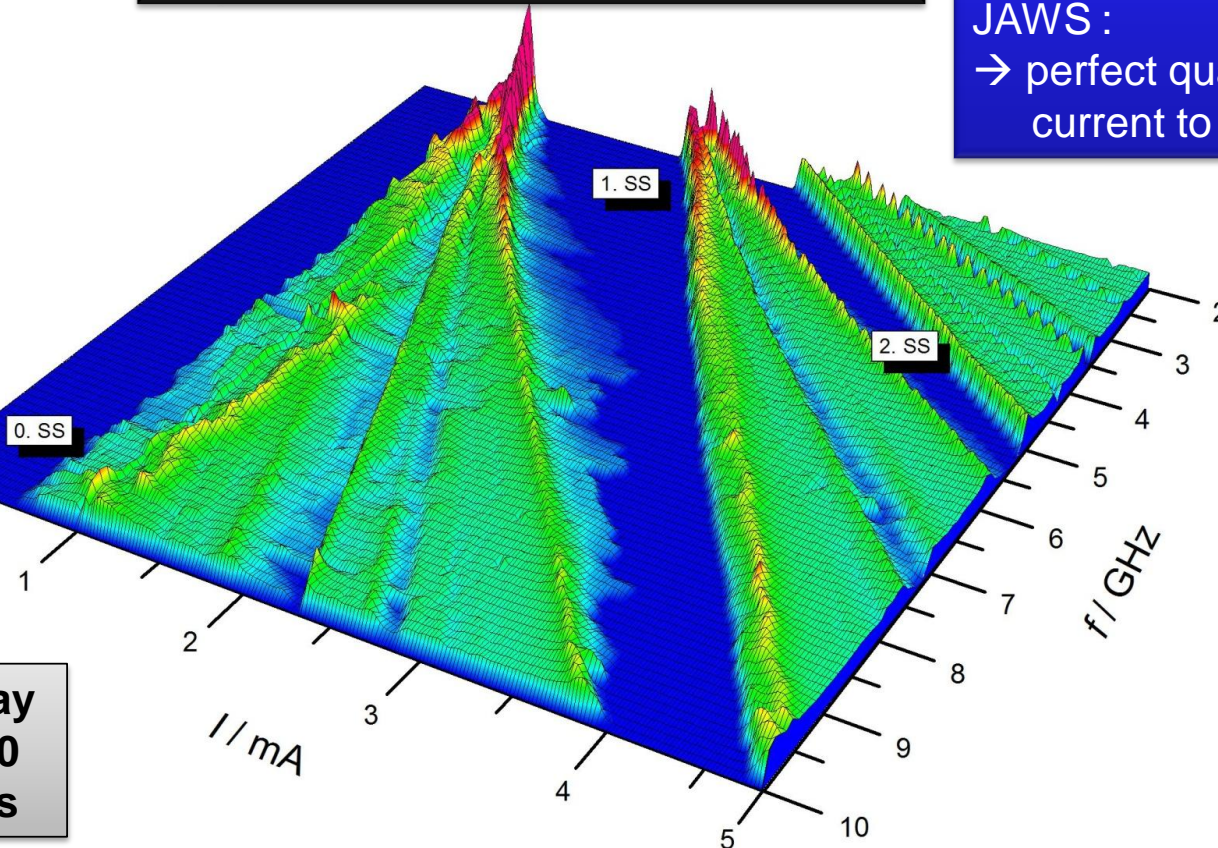
# JAWS : Shapiro steps @ all frequencies



$dV/dI$



JAWS operated with pulses



not „important“ :  
➤ shape of the current pulses  
➤ jitter in time & amplitude  
JAWS :  
→ perfect quantizer  
current to voltage

JAWS array  
with 2990  
junctions

current-voltage-characteristic vs. frequency

# JAWS : practical realization



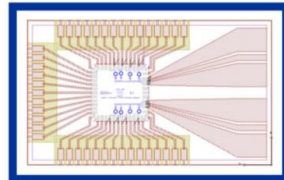
computer



pulse-pattern-generator (PPG)



SNS JAWS chip @ LHe : 4.2 K

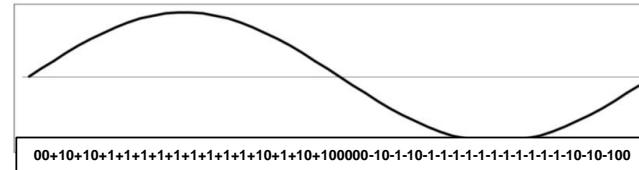


spectrum analyzer

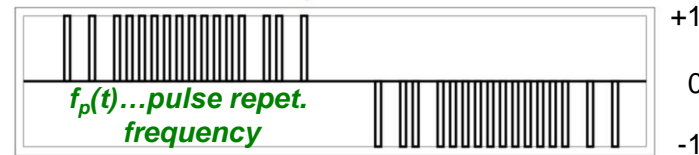


$$V(t) = M \cdot N \cdot \Phi_0 \cdot f_p(t)$$

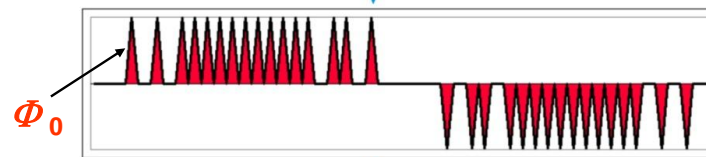
arbitrary waveform



$\Sigma\Delta$  - modulation



current pulses



array output



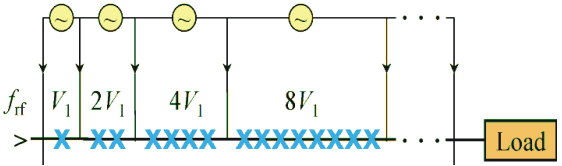
quantized waveform

# PJVS and JAWS : basic principle

**AC-Programmable Josephson Voltage Standard**

**70 GHz**  $V_{AC}(t) = M \cdot N \cdot \Phi_0 \cdot f$  **15 GHz**

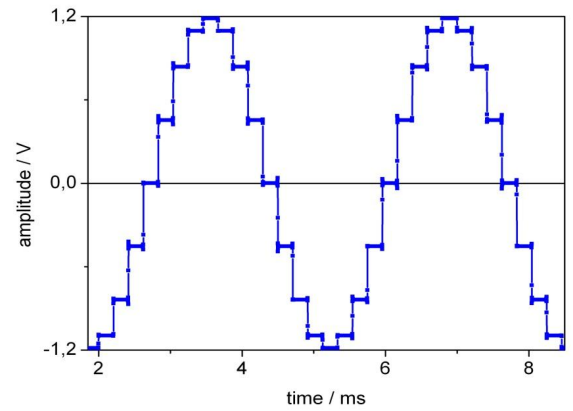
binary



$f_{ff}$   $V_1$   $2V_1$   $4V_1$   $8V_1$  Load

$M(t)$

**number Josephson junctions**



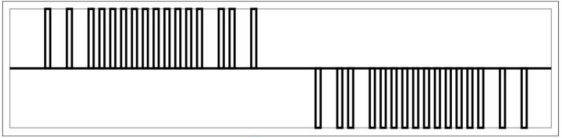
amplitude / V

time / ms

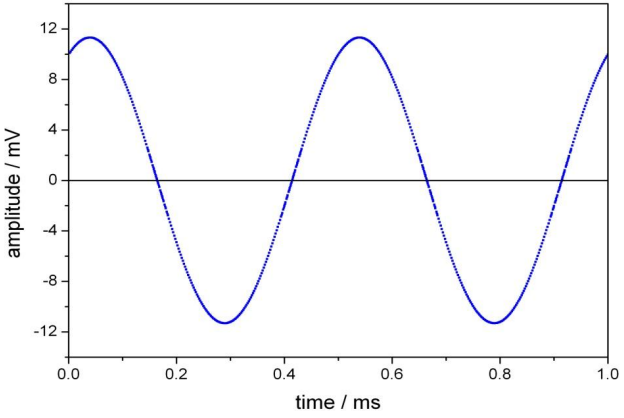
**Josephson Arbitrary Waveform Synthesizer**

$f_p(t)$

pulse operation



**pulse repetition frequency**



amplitude / mV

time / ms



# PJVS and JAWS : basic principle

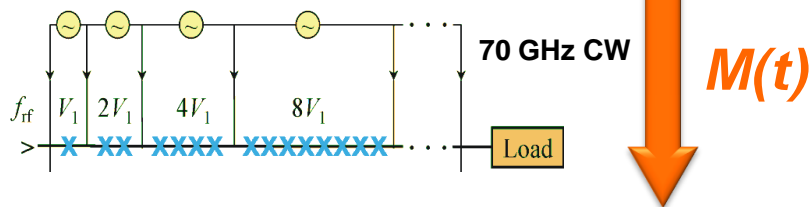
## AC-Programmable Josephson Voltage Standard

70 GHz

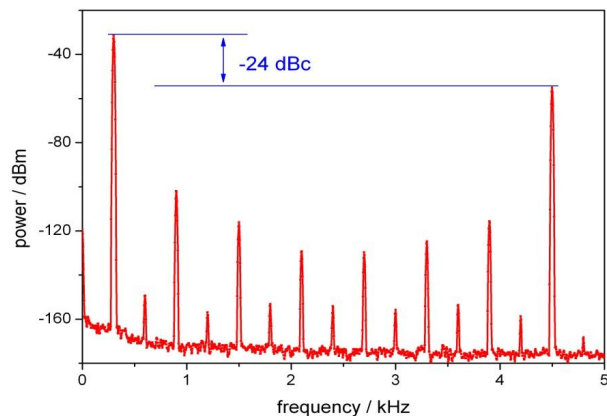
$$V_{AC}(t) = M \cdot N \cdot \Phi_0 \cdot f$$

15 GHz

binary



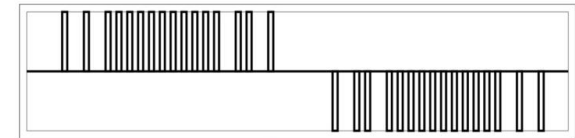
number Josephson junctions



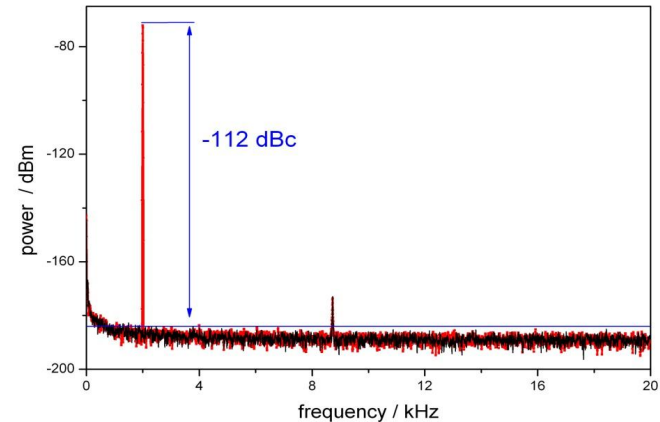
## Josephson Arbitrary Waveform Synthesizer

$f_p(t)$


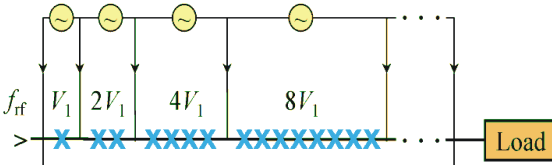
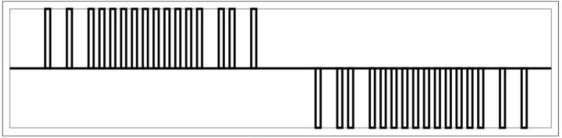
pulse operation



pulse repetition frequency



# PJVS and JAWS : basic principle

 <b>AC-Programmable Josephson Voltage Standard</b>	<b>Josephson Arbitrary Waveform Synthesizer</b>
<p><b>70 GHz</b></p> <p><math>V_{AC}(t) = M \cdot N \cdot \Phi_0 \cdot f</math></p> <p><b>15 GHz</b></p> <p>binary</p>  <p><math>f_{ff}</math></p> <p><math>V_1</math> <math>2V_1</math> <math>4V_1</math> <math>8V_1</math></p> <p><math>&gt;</math> <math>x</math> <math>xx</math> <math>xxxx</math> <math>xxxxxxxx</math> ...</p> <p>Load</p> <p><math>M(t)</math></p>	<p><math>f_p(t)</math></p> <p>pulse operation</p> 
<p><b>number Josephson junctions</b></p> <p><b>output voltage : <math>20 V_p</math></b></p> <p><b>step approximated waveform</b></p> <p><b>spectrum : many harmonics</b></p> <p><b>not quantized between steps</b></p> <p><b>frequency range : DC... &lt; 10 kHz</b></p>	<p><b>pulse repetition frequency</b></p> <p><b>output voltage : <math>1 V_{RMS}</math></b></p> <p><b>real arbitrary waveform</b></p> <p><b>spectrum : no harmonics</b></p> <p><b>quantized at any time</b></p> <p><b>frequency range : DC...MHz</b></p>

# outline



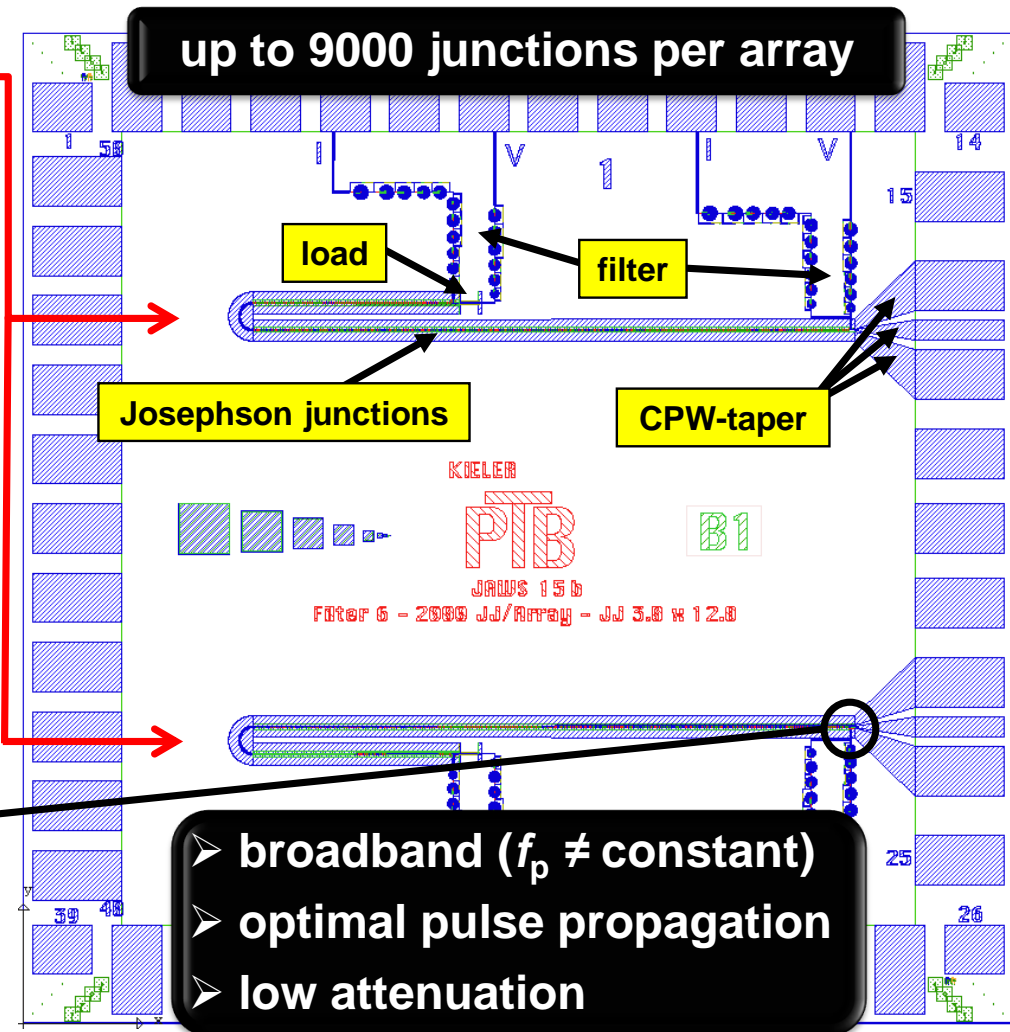
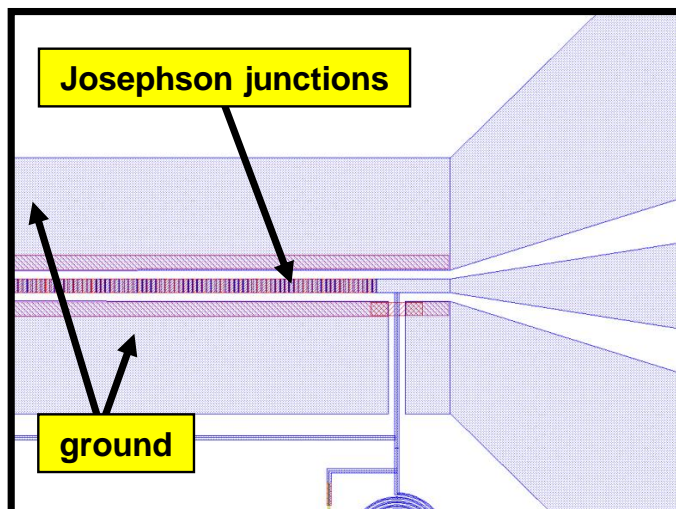
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# JAWS design : CPW



**2 arrays @ chip :**

- size : 10 mm x 10 mm
- coplanar waveguide (CPW)
- CPW : 50 Ohm-taper
- Load : 50 Ohm
- on-chip LCR-filter





# JAWS: major fabrication tools



***cluster sputter system***



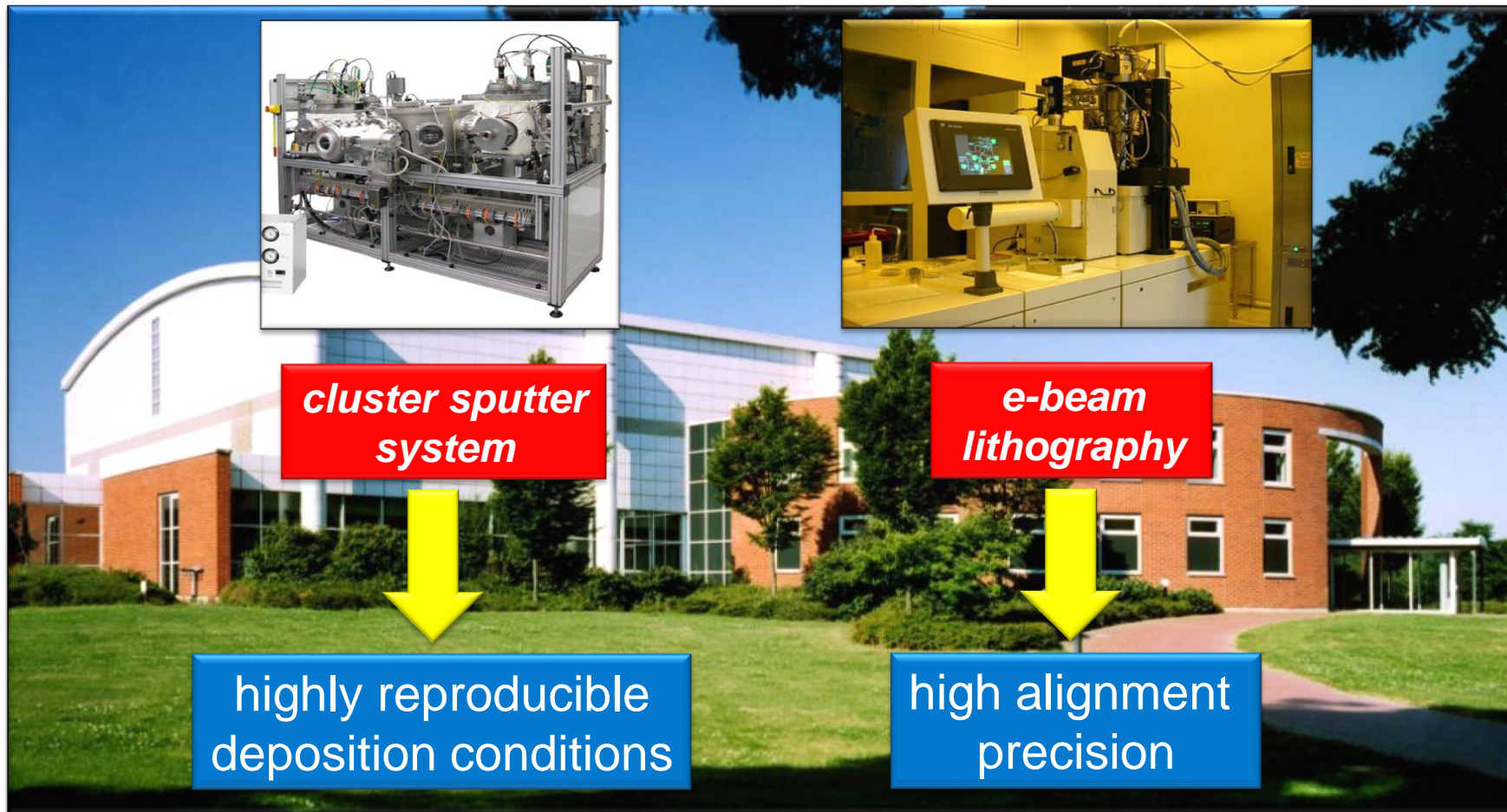
highly reproducible  
deposition conditions



***e-beam lithography***

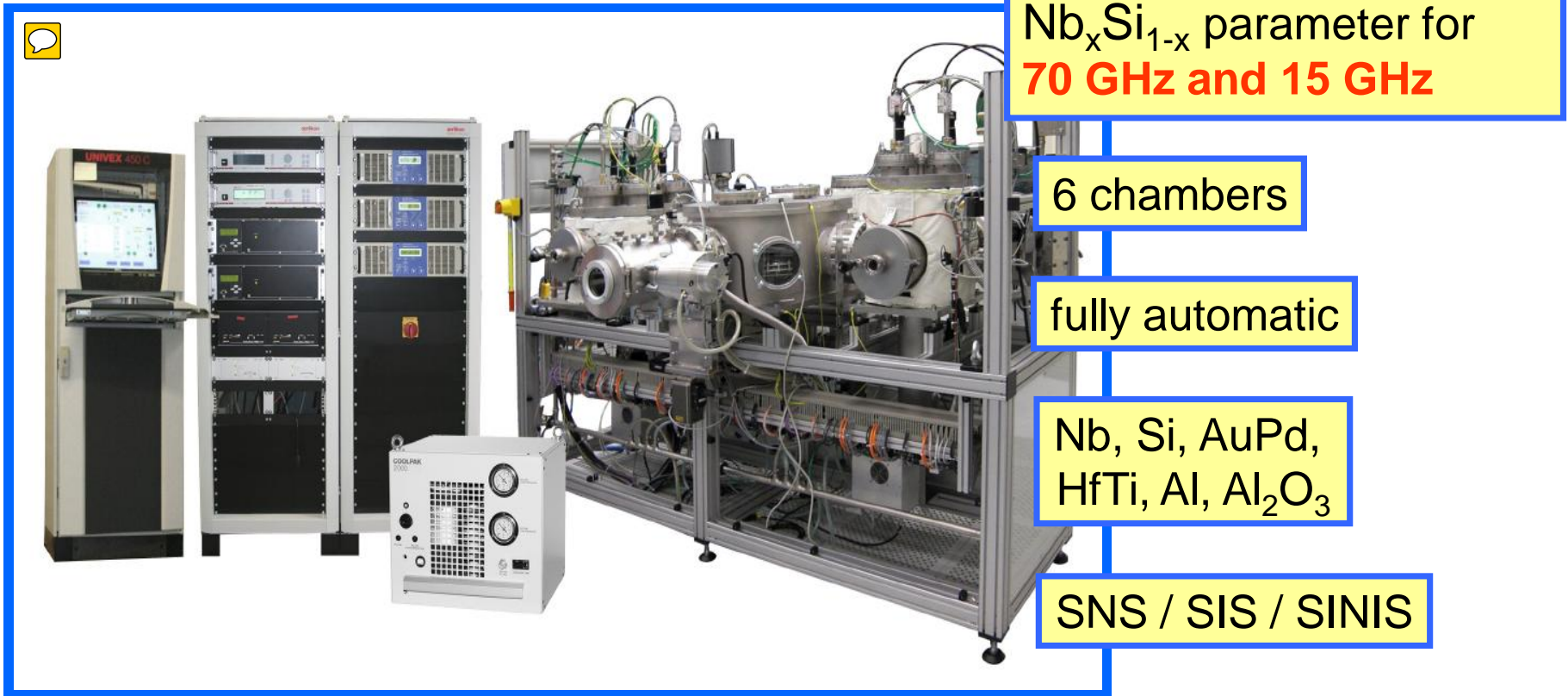


high alignment  
precision





# UNIVEX 450C – Cluster - Sputter - System



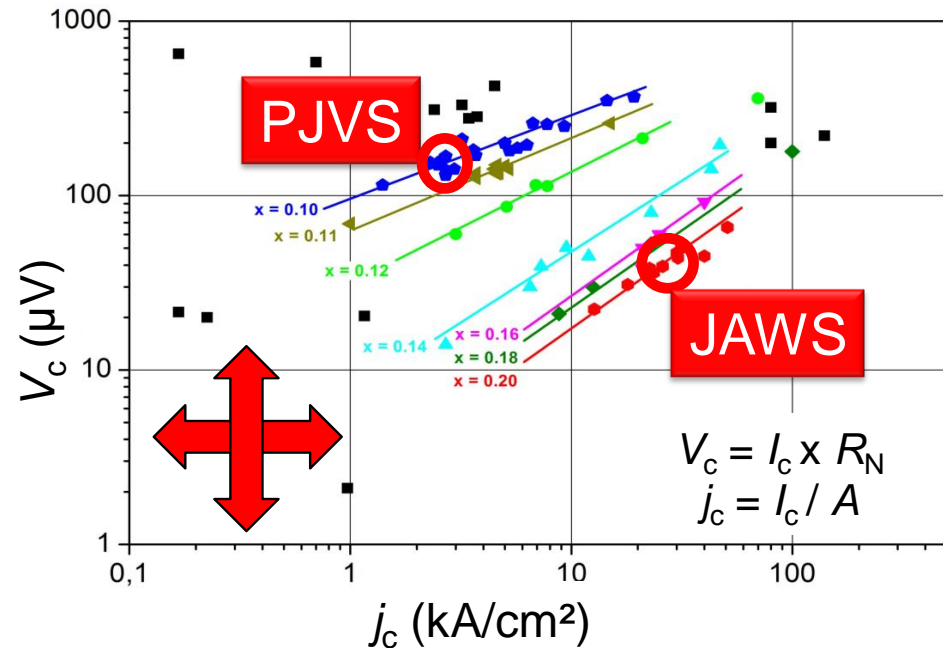
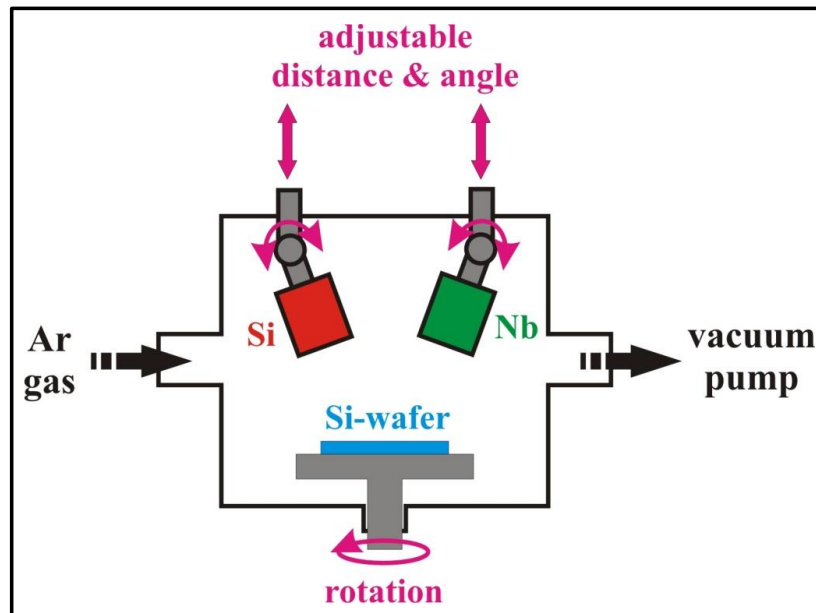
2 parameter to optimize :  
**JAWS** :  $x \approx 20\%$ ,  $d_{\text{NbSi}} \approx 30 \text{ nm @ 15 GHz}$

# SNS junctions : $Nb_xSi_{1-x}$



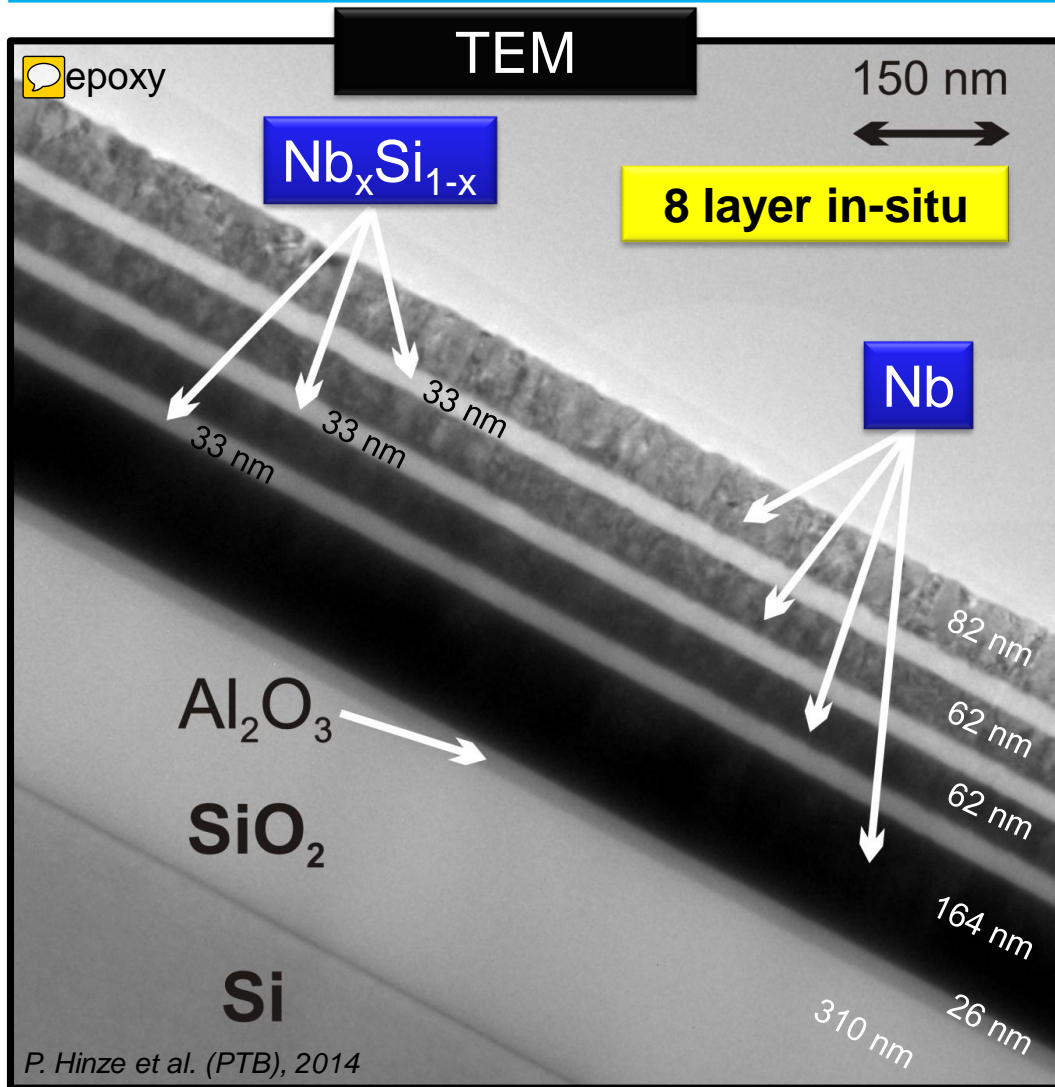
$Nb_xSi_{1-x}$  : co-sputter !

thickness  $d$  and Nb content  $x$



$j_c$  and  $V_c$  parameter adjustable  
in a **wide range** - **nearly independent**

# SNSNSNS : triple-stacked junctions



UNIVEX 450C - system



homogeneous & reproducible  
deposition conditions

for a given design :

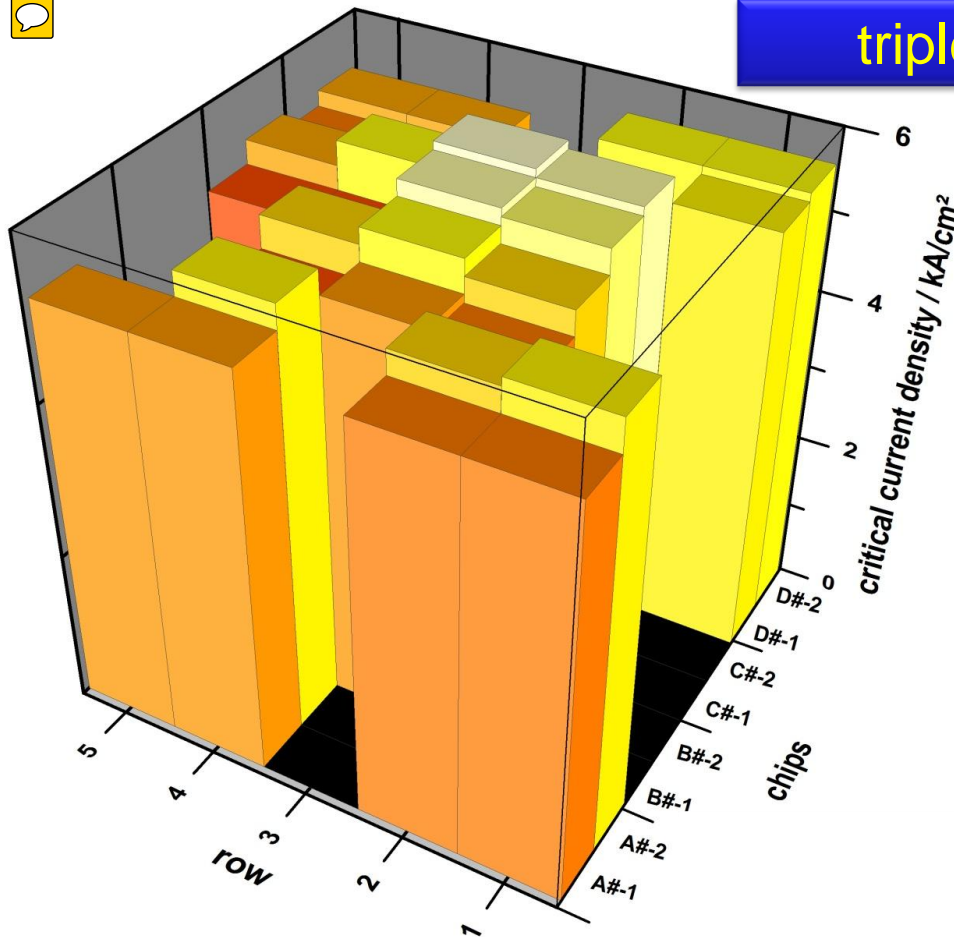
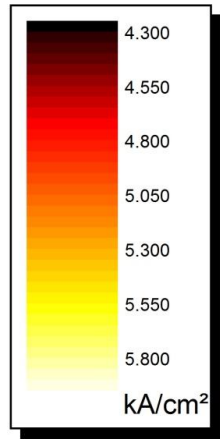
3 x junction number



3 x output voltage



# UNIVEX : low parameter spread



triple-stacked junctions

30 circuits  
measured (from 40)

228 000 junctions :  
9 defect only



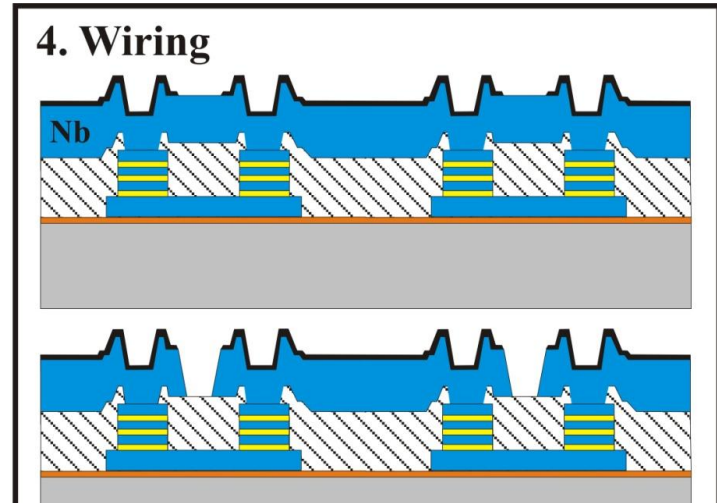
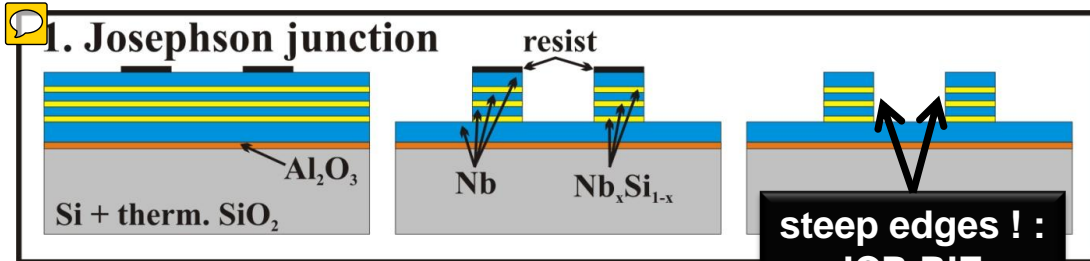
junction - yield :  
99.996 %

current density distribution @ wafer :



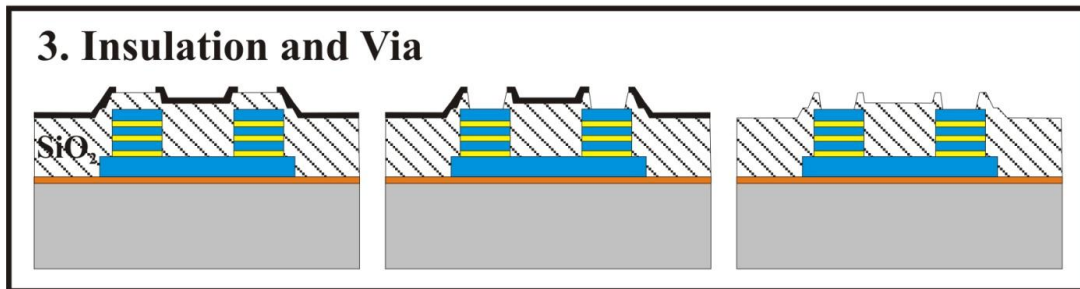
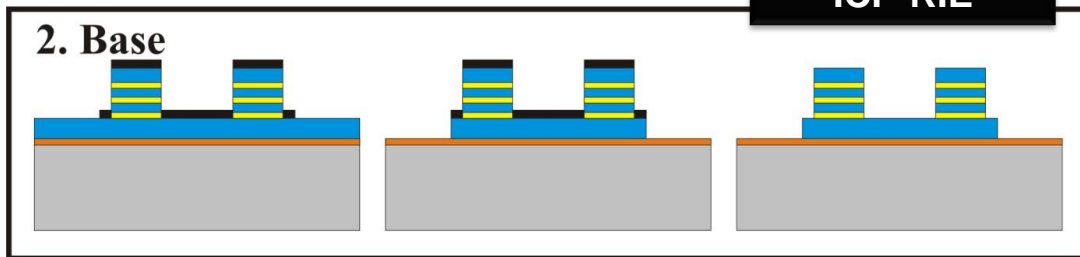
deviation from  
mean value :  
4.6 %

# Window-process : JJ : SNSNSNS



**3D fabrication :**

- junction multilayer : 550 nm
- SiO<sub>2</sub> : 600 nm
- Nb wiring : 750 nm
- AuPd : 300 nm
- : Σ = 2,2 μm

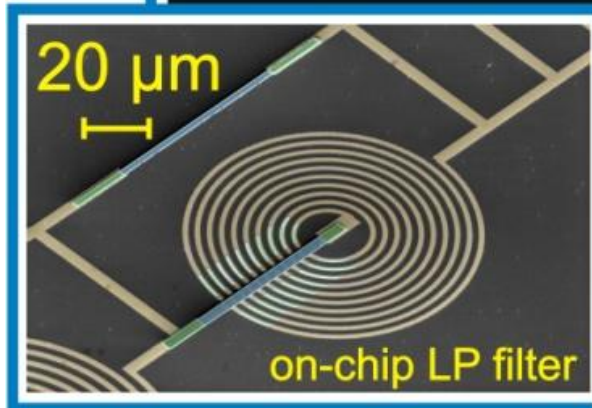
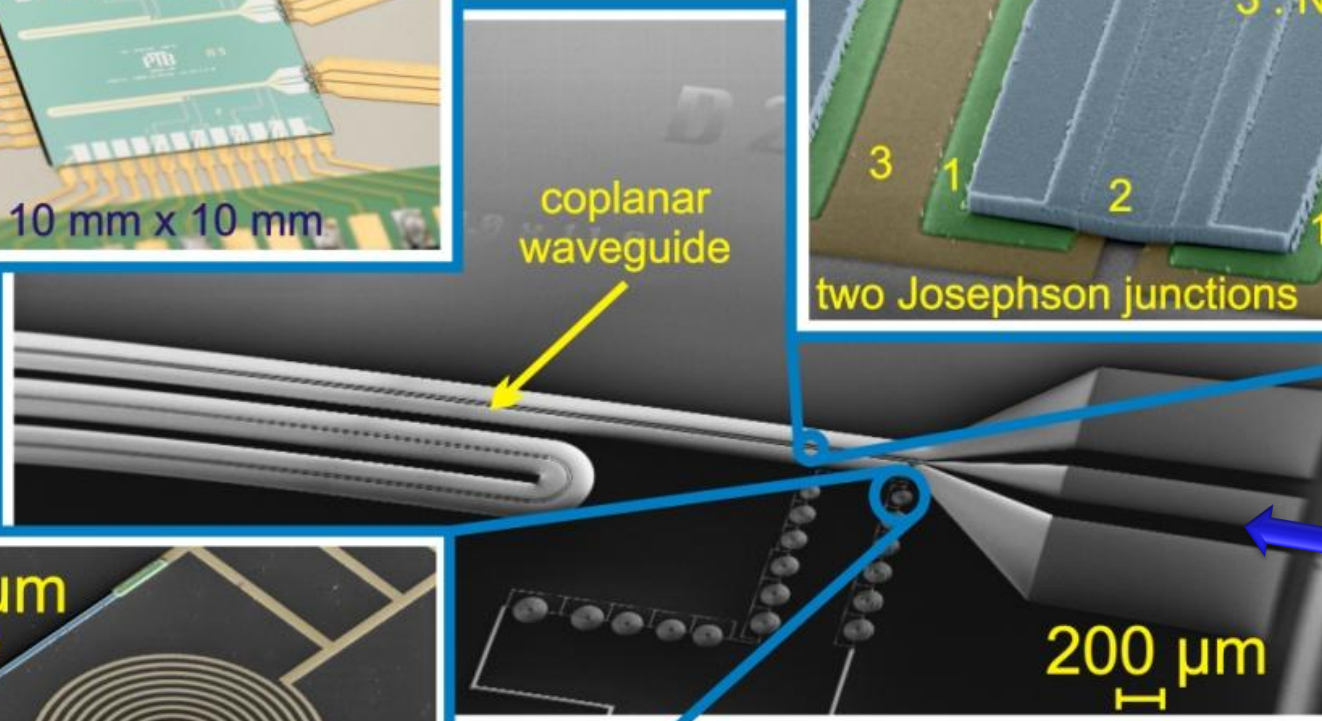
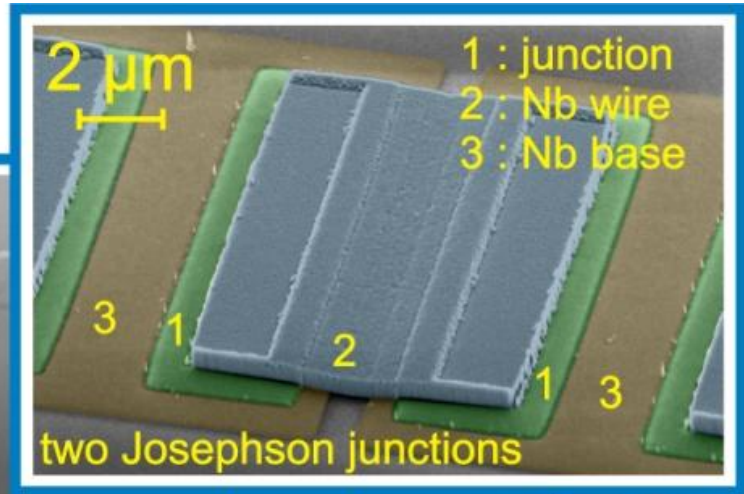
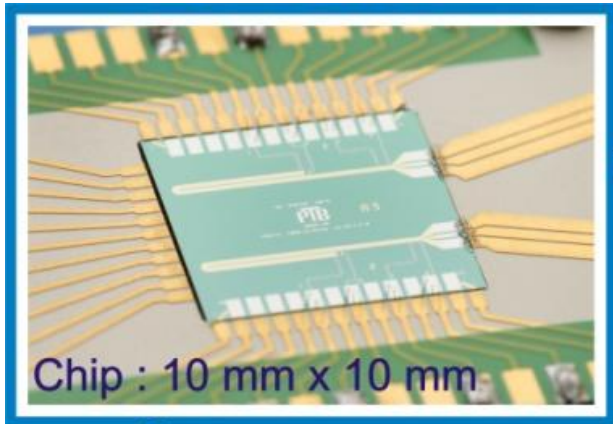


**5. Load : AuPd resistors by lift-off; 6. Pads : remove SiO<sub>2</sub> by wet-etching**

**5 x deposition, 5 x etching, 5 x e-beam, 1 x lift off, 1 x opt. lithography**

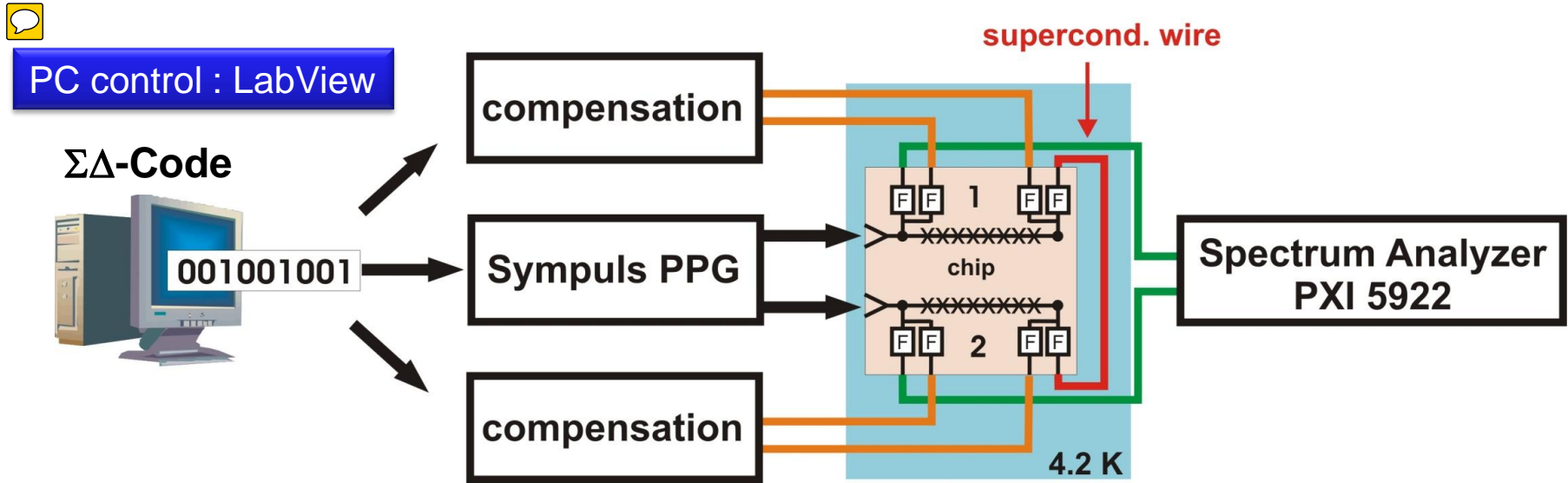
**fabrication of large arrays with high yield !**

# Technology : large circuits



2 x 9000 JJ : triple-stacked  
JJ-size : 4.0  $\mu\text{m}$  x 11.0  $\mu\text{m}$

# setup : 2 arrays in series @ 1 chip



## Sympuls PPG :

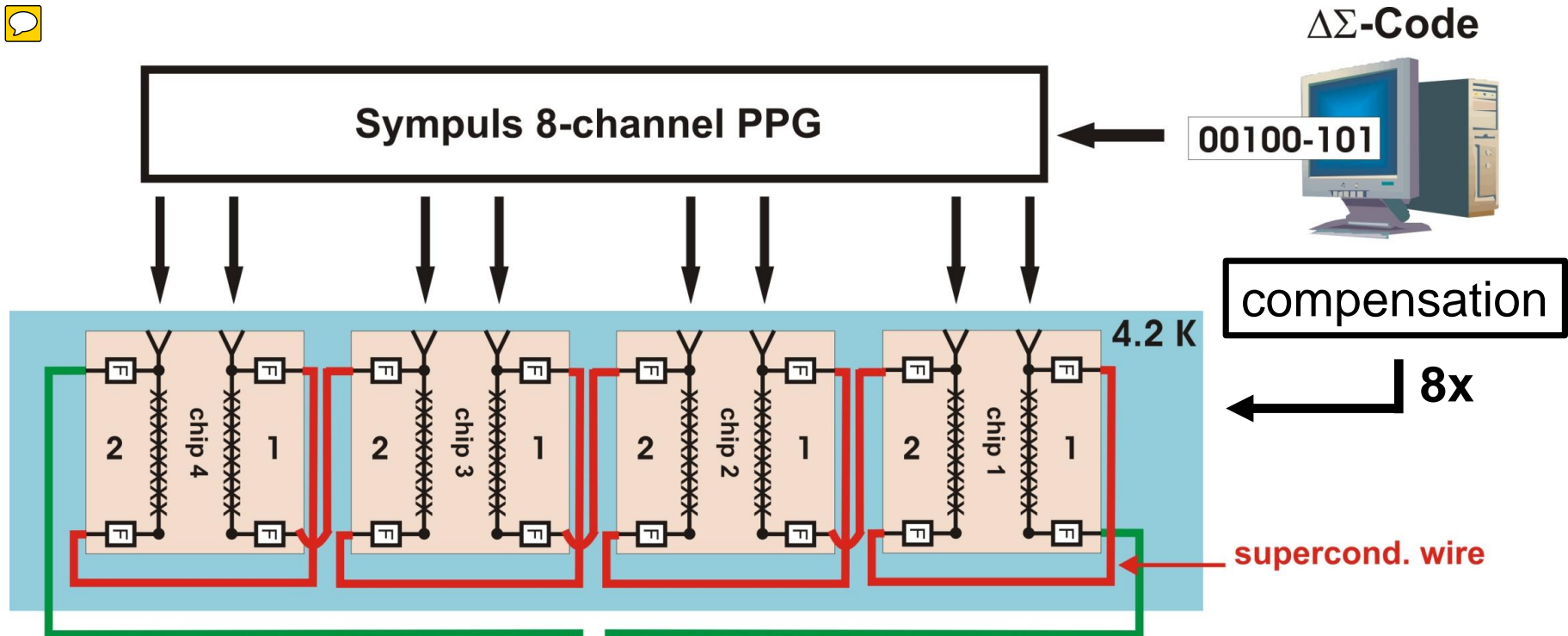
- ternary pulses : -1 / 0 / +1
- 2 output channels
- max. clock-frequency : 15 GHz
- max. code-memory : 256 Mbit

## „pure“ spectra, if optimized :

- $\Sigma\Delta$ -codes
- experimental setup
- broadband Josephson arrays

2 JAWS systems operational @ PTB

# 1 V-JAWS : 8 arrays @ 4 chips



junctions :  
chip 1 : 18 000  
chip 2 : 18 000  
chip 3 : 15 000  
chip 4 : 12 000

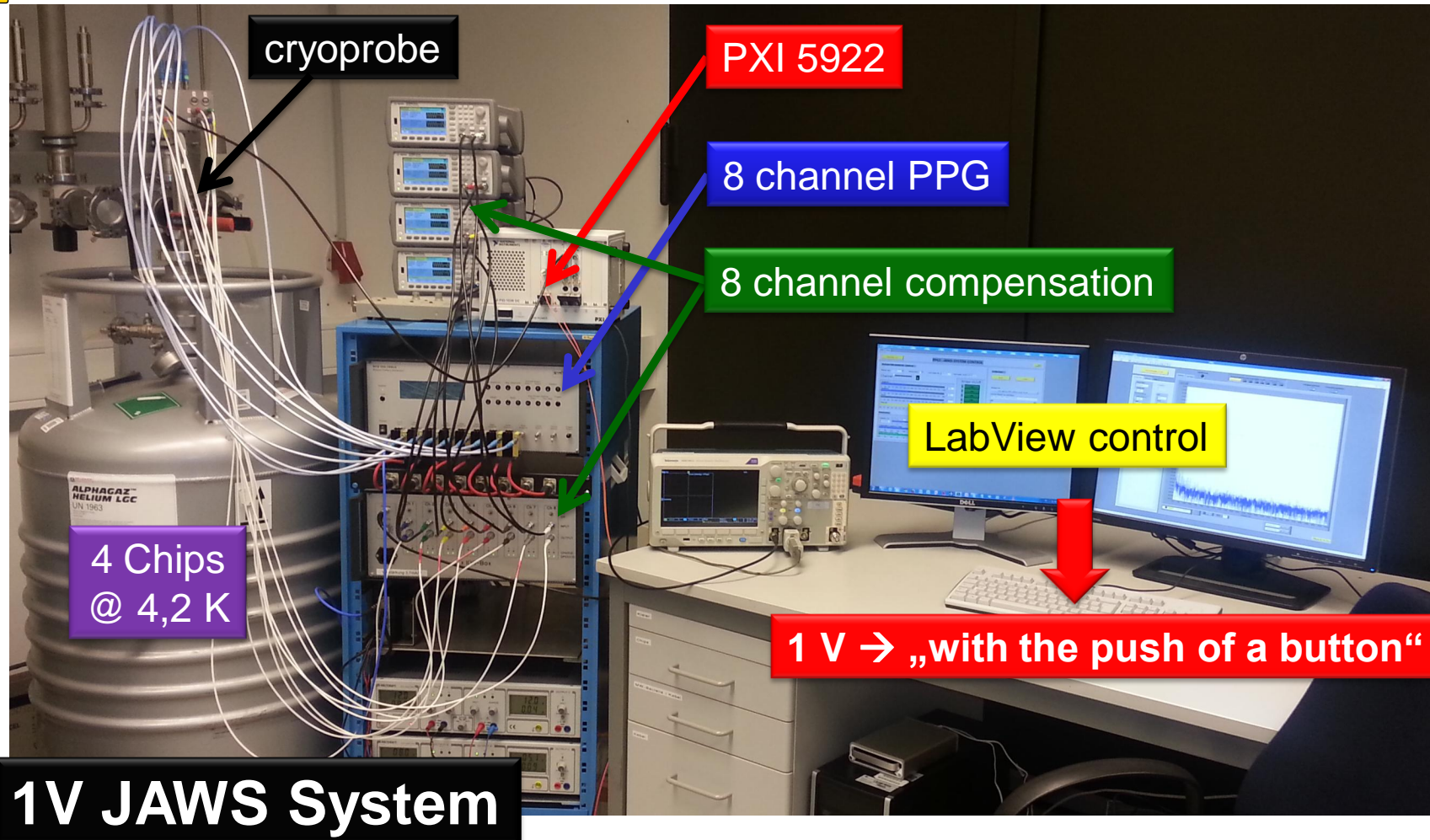
**Spectrum Analyzer  
PXI 5922**

**presented @ ASC 2014**

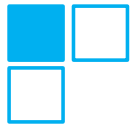
Sympuls PPG :  
- 8 output channels  
- ternary pulses : -1 / 0 / +1  
- max. clock-frequency : 15 GHz  
- max. code-memory : 256 Mbit  
- bit multiply-function



# optimized setup: 1V JAWS



**1V JAWS System**

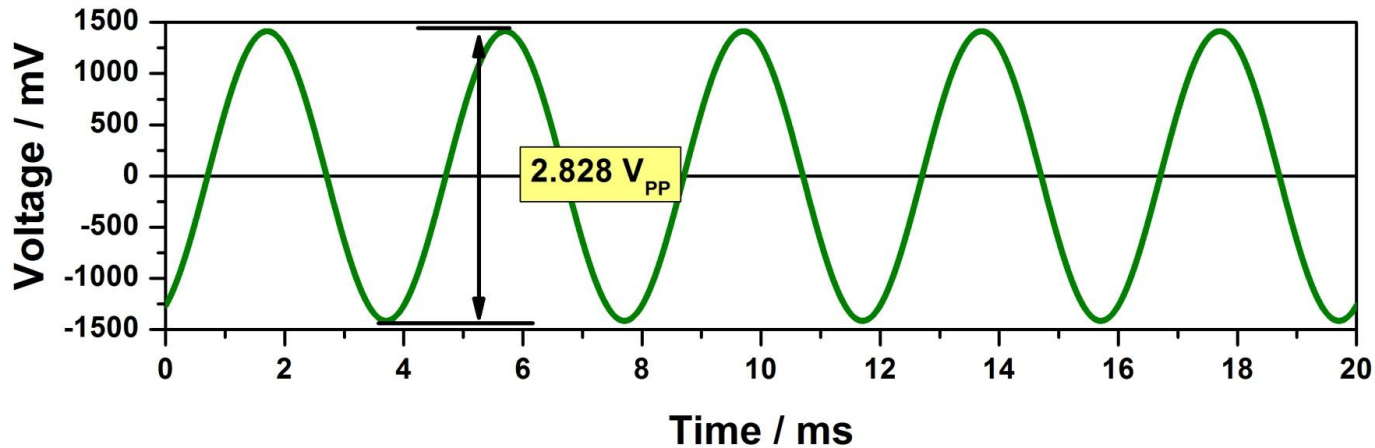
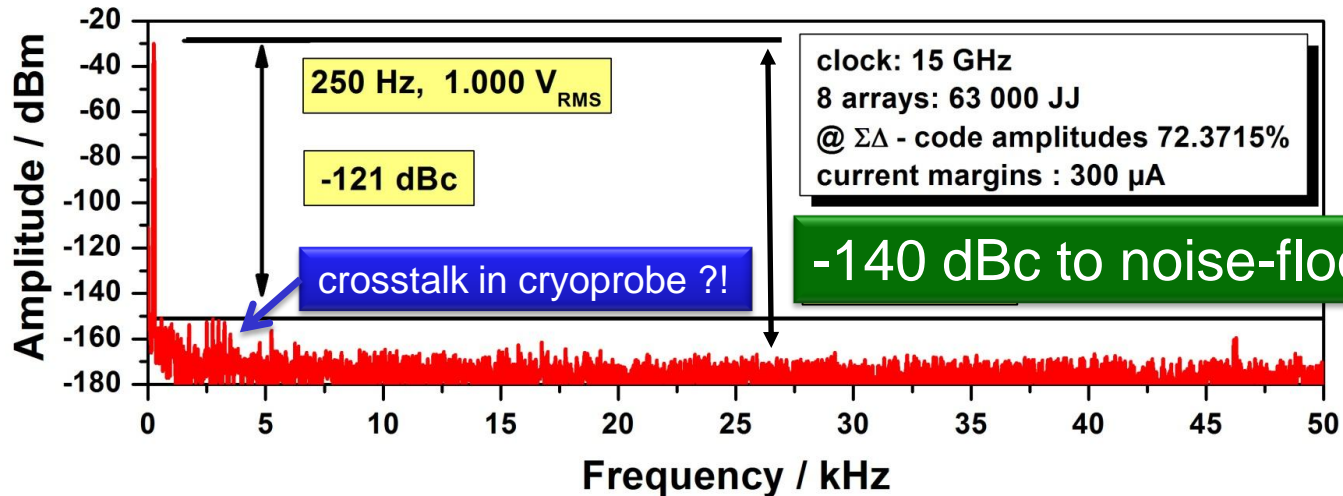


# triple-stacked junctions : 8 array @ 4 chips



➤ spectra up to voltages of  $1.0 V_{RMS}$  ( $2.8 V_{pp}$ ) with 63 000 junctions

stable  
operation  
margins  
 $300 \mu A$



## JAWS : features



- **spectrally pure waveforms**
- **arbitrary waveforms**
- **large frequency bandwidth**
- **operation in cryocooler**
- **high time stability**
- **high precision**
- **3 JAWS systems @ PTB**
- **first applications**

**already achieved !**



## JAWS : features



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- **arbitrary waveforms**
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- **3 JAWS systems @ PTB**
- **first applications**

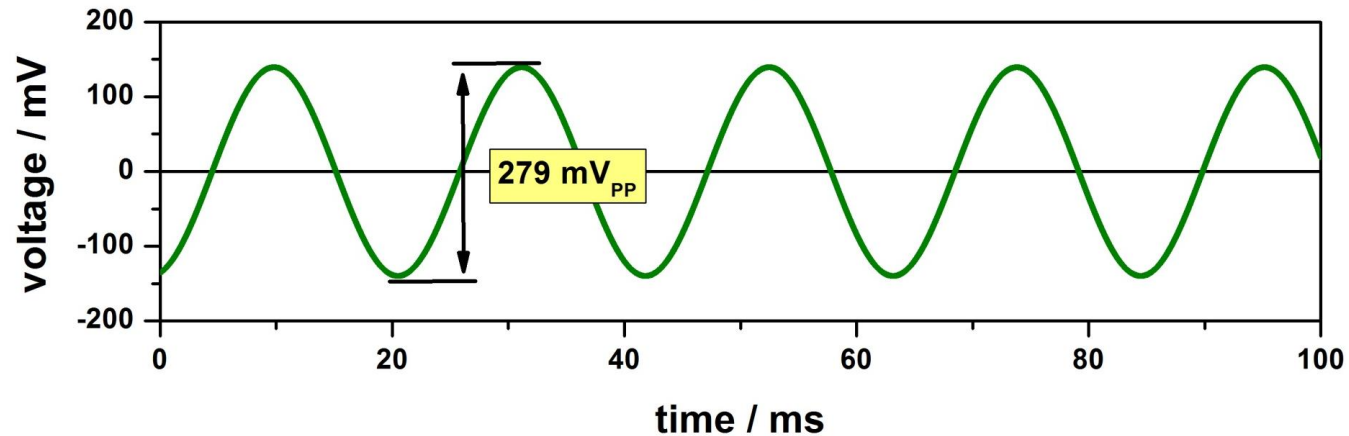
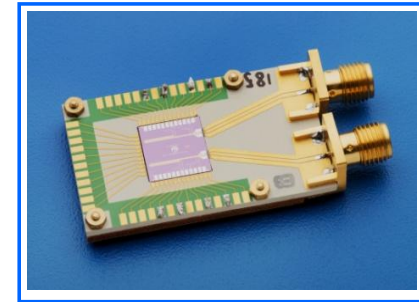
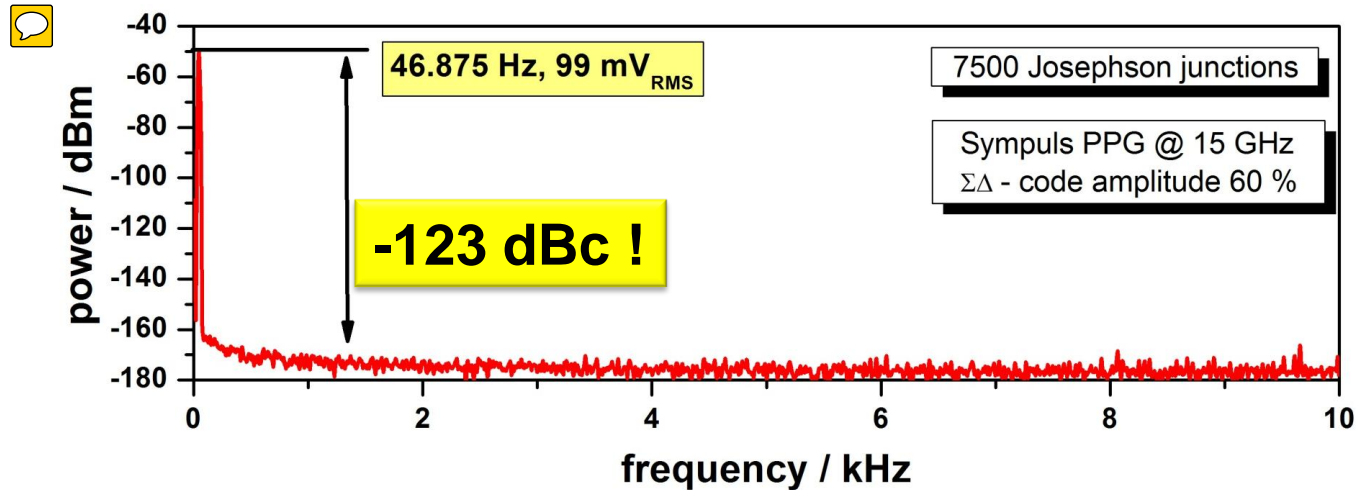
**examples**

**already achieved !**

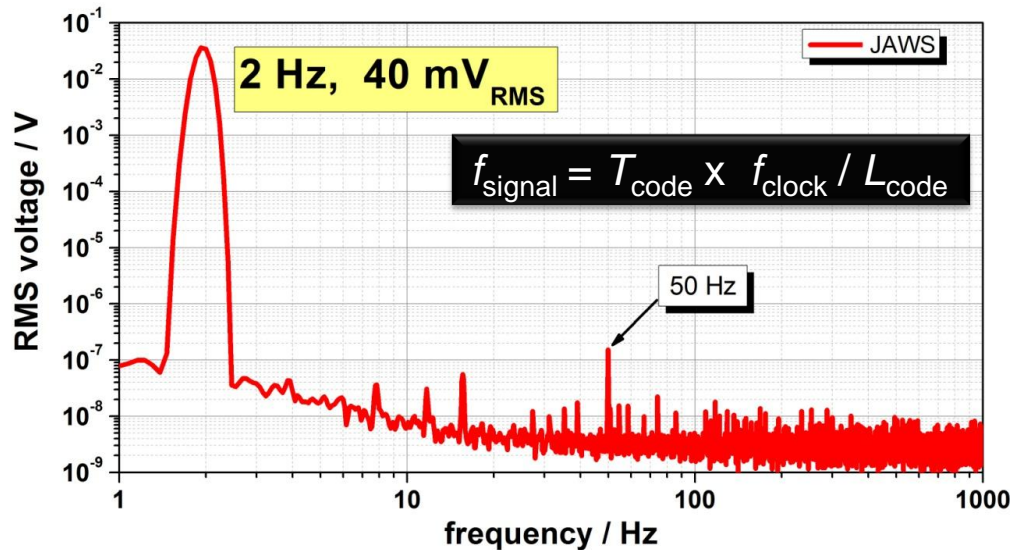
# JAWS : spectrally pure waveforms !



➤ spectra up to voltages of  $279 \text{ mV}_{pp}$  with 7 500 junctions with SNR of  $-123 \text{ dBc}$

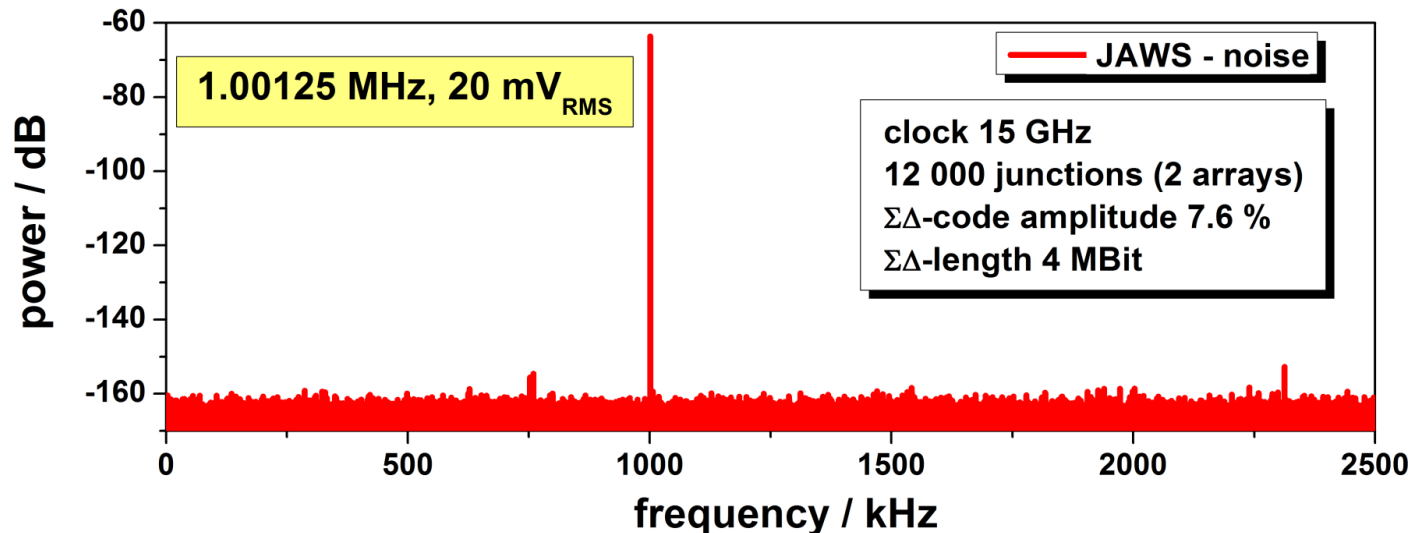


# JAWS : large frequency range



bit-multiply option :  
virtually increase  
of  $\Sigma\Delta$ -code memory  
(up to 32 x 256 Mbit)

frequency range :  
DC, 2 Hz ... 1 MHz

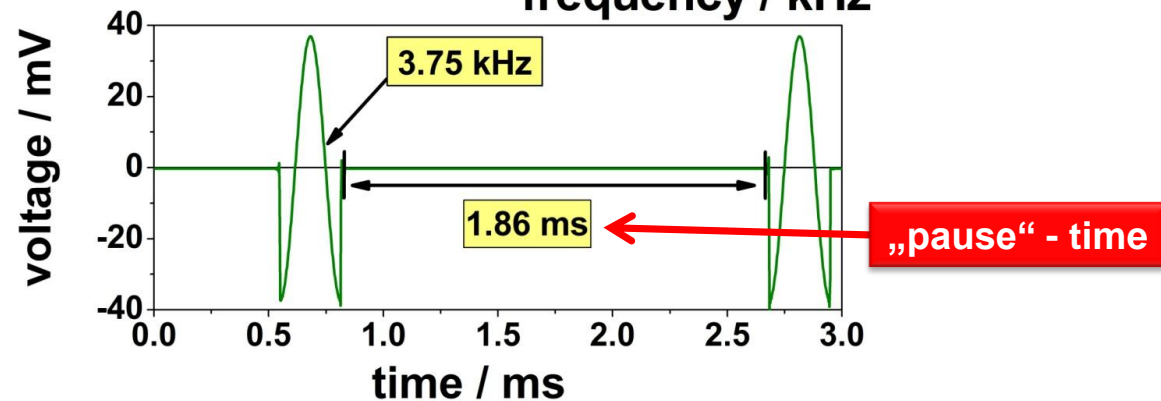
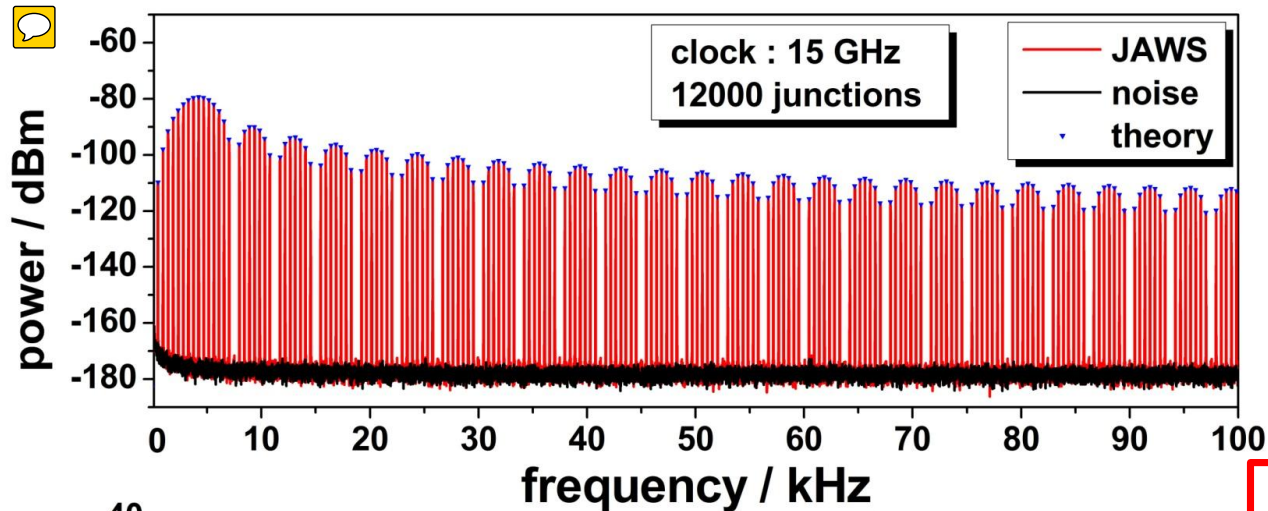


# JAWS : arbitrary waveforms



application : characterization AD-converter (e.g. „single-shot“)

➤ non-continuous waveform : cosines with „pause“- time

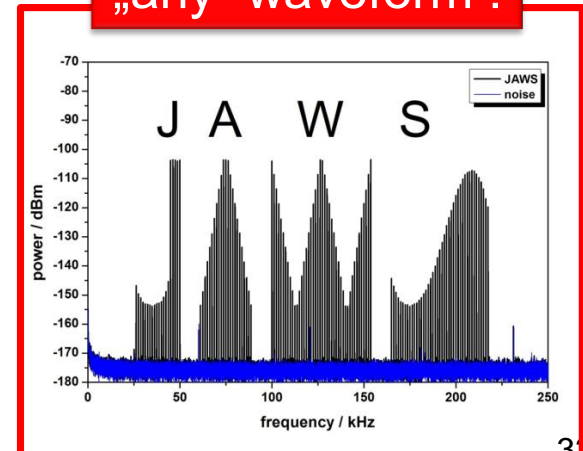


complex frequency comb



JAWS : most suitable

„any“ waveform !

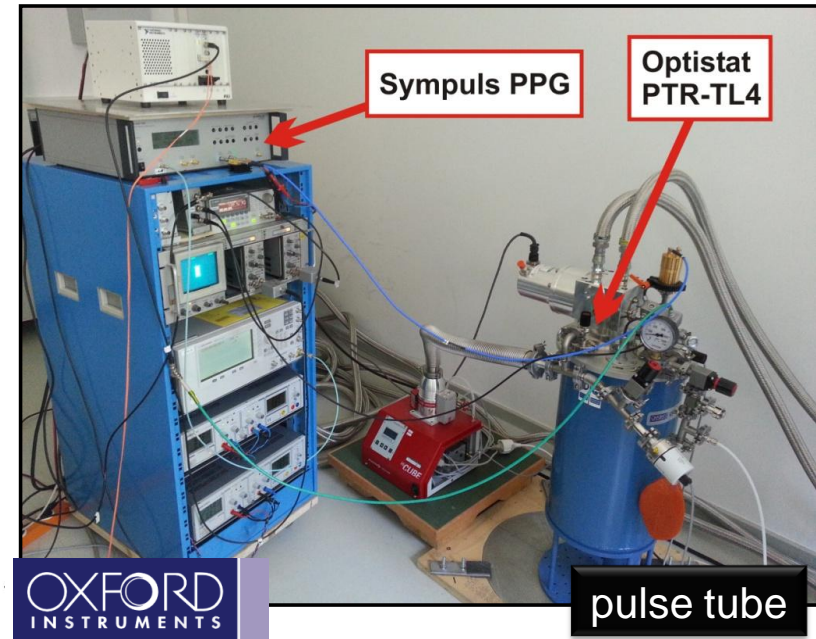
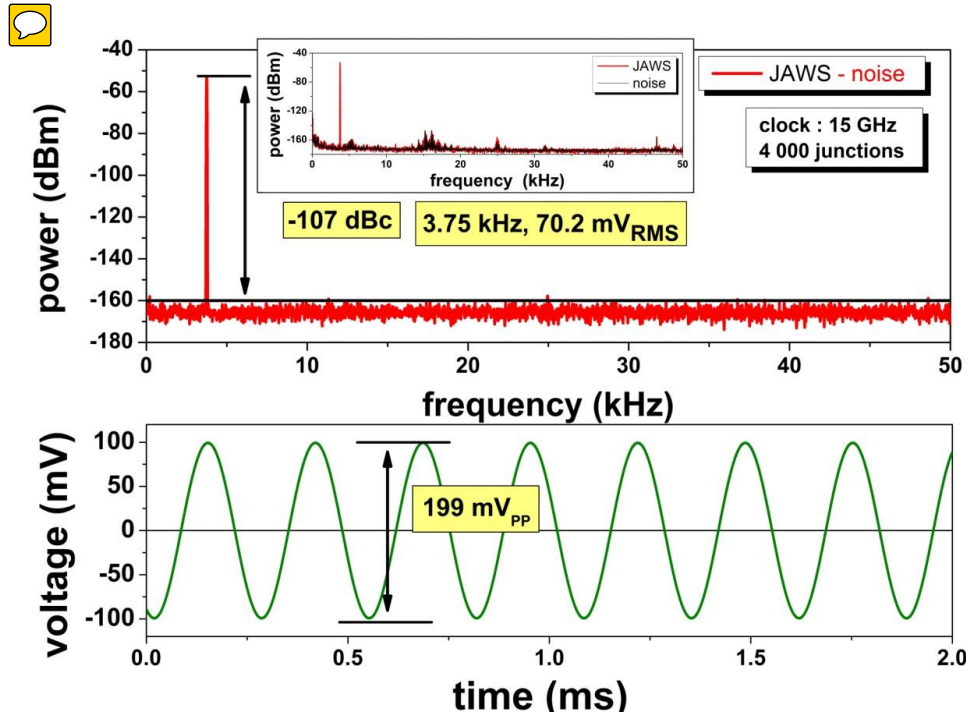


# JAWS : cryocooler operation



➤ spectra up to voltages of  $\approx 200 \text{ mV}_{pp}$  with 4 000 junctions

➤ temperature range : 4.2 K to 5.6 K



successful operation of JAWS in cryocooler

AIST :  
2.6 mV<sub>pp</sub> with 100 junctions,  
SNR -80 dBc

Urano, et al., *SUST* 22, 2009

Kieler, et al., *W. Journal Cond. Matter Physics* 3, 2013

# outline



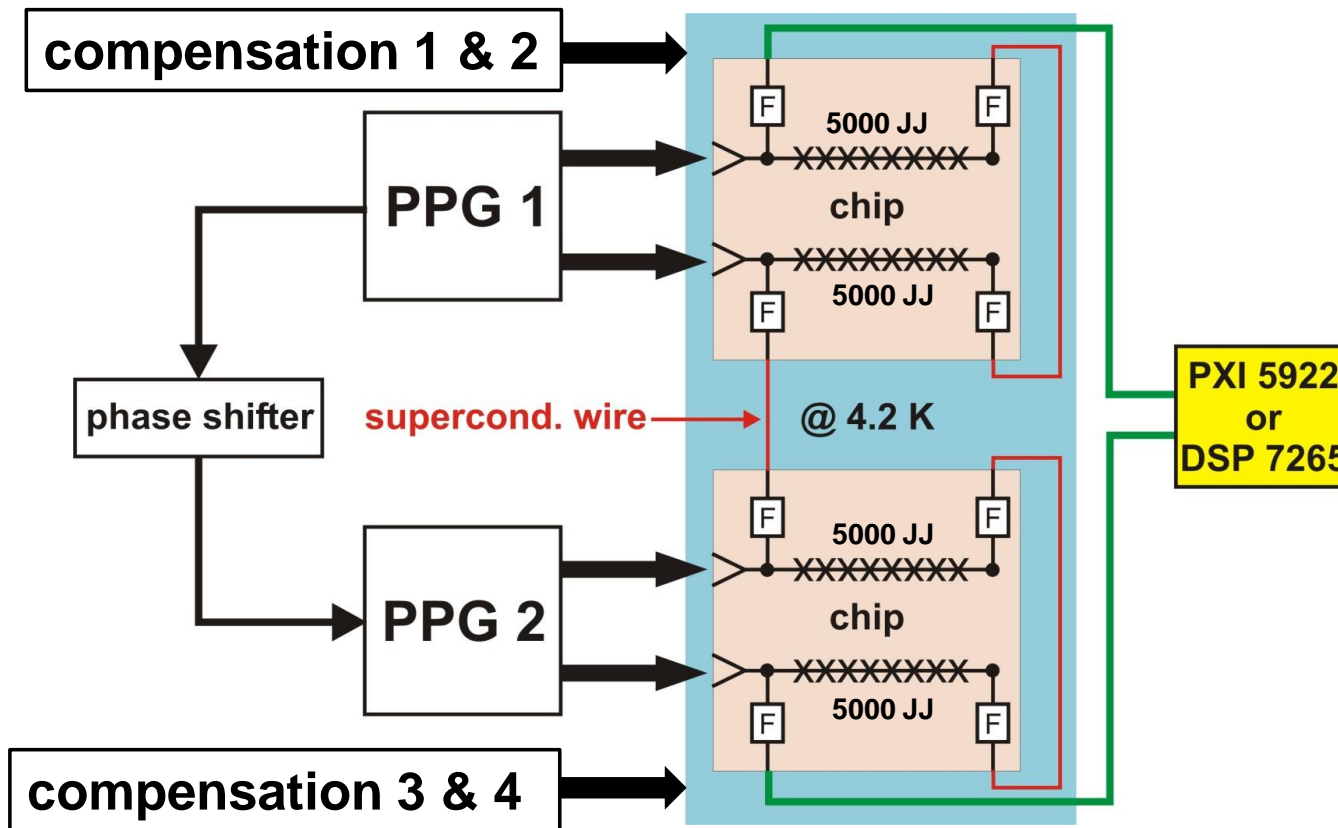
- 1. Principle PJVS and JAWS**
- 2. 1 V JAWS @ PTB**
  - a) design**
  - b) fabrication**
  - c) setup**
  - d) overview : features**
- 3. Precision of JAWS**
  - a) comparison JAWS vs. JAWS**
  - b) comparison JAWS vs. QVM**
- 4. Summary**



# direct comparison : JAWS vs. JAWS (I)



comparison : 10 000 junctions vs. 10 000 junctions



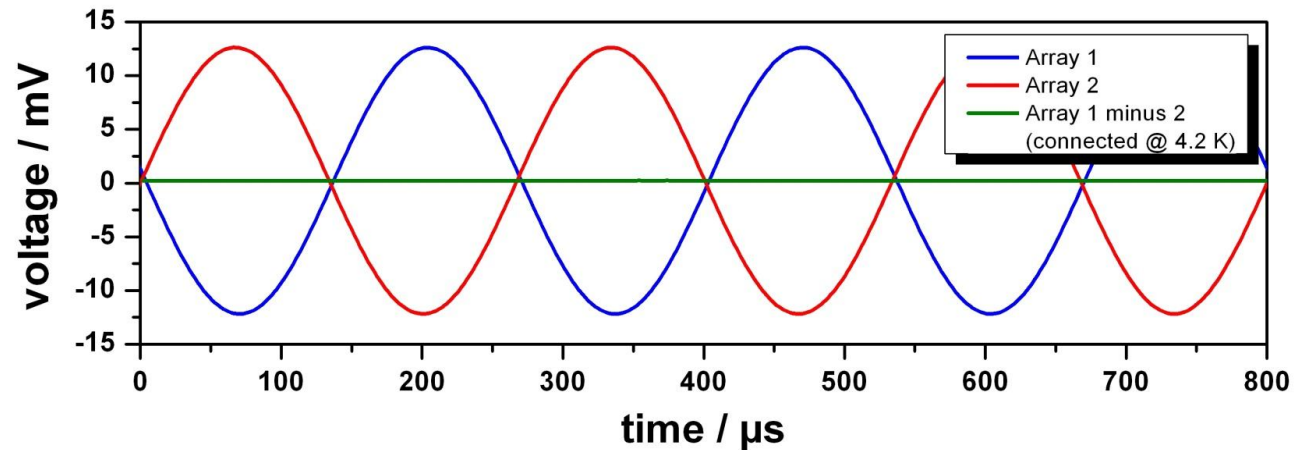
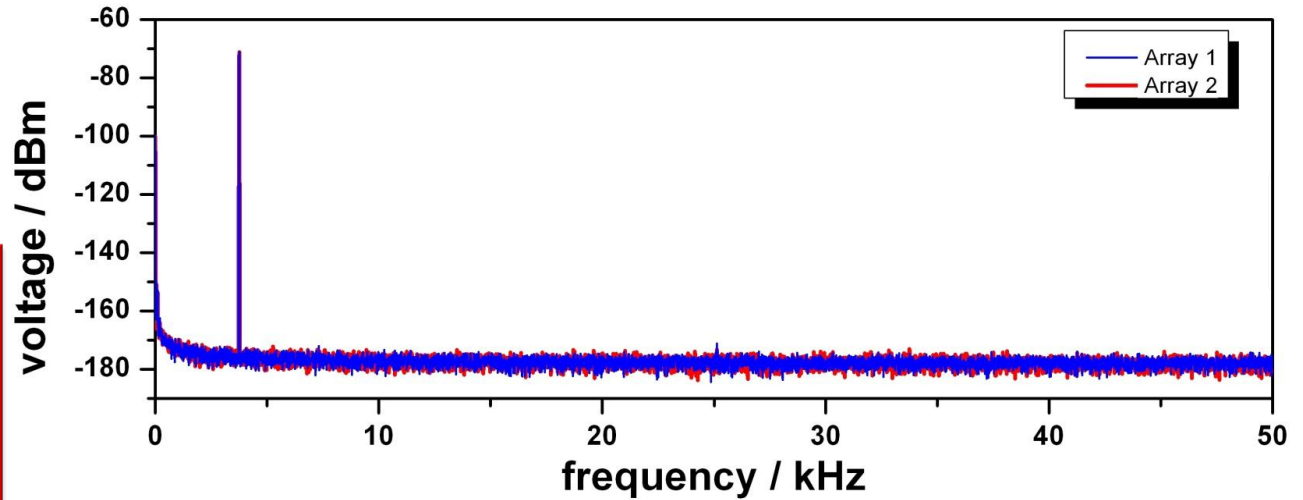
# direct comparison : JAWS vs. JAWS (II)



if only **one** array  
switched on



PXI 5922 :  
voltage difference  
already only  
 $53 \text{ nV}_{\text{RMS}}$





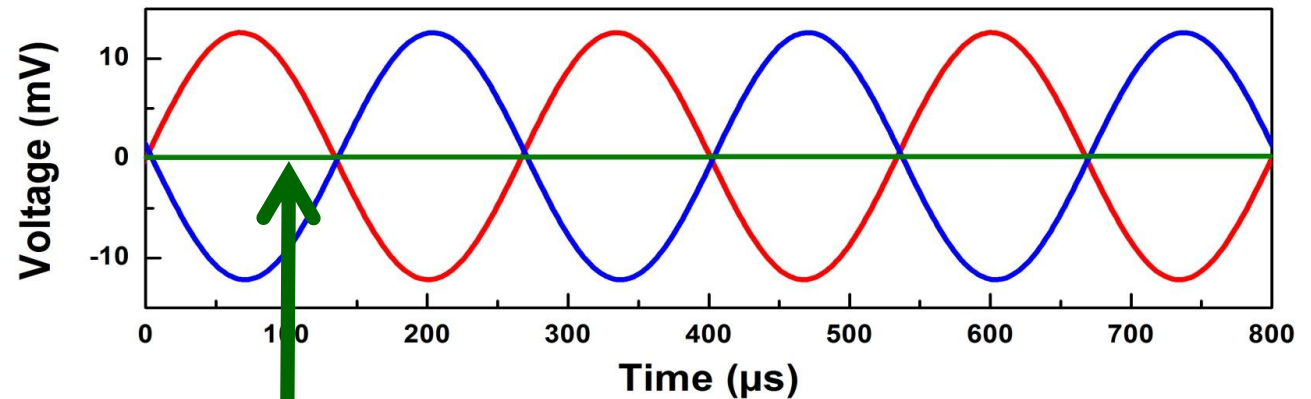
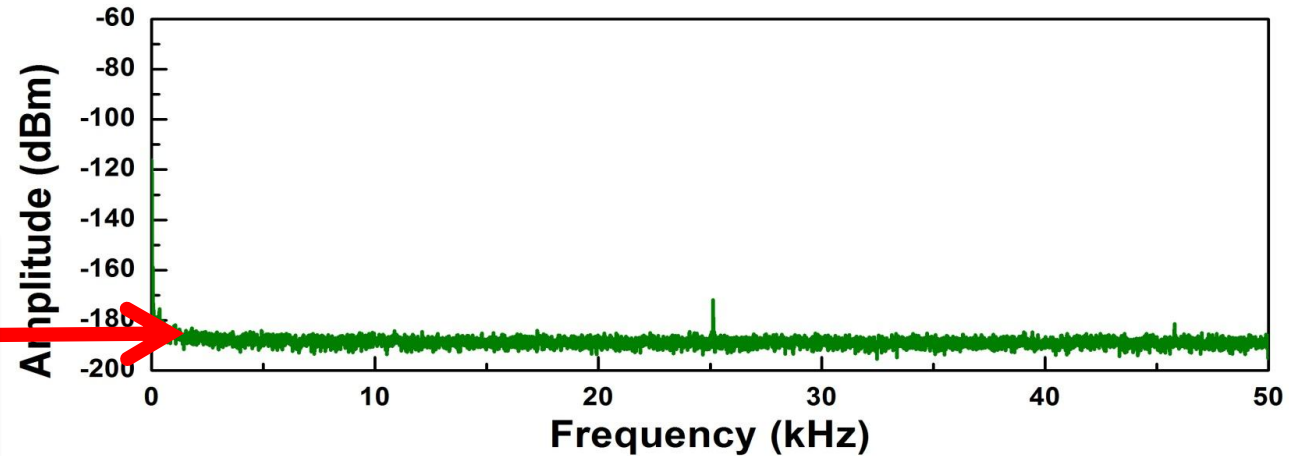
# direct comparison : JAWS vs. JAWS (III)



both arrays  
switched on

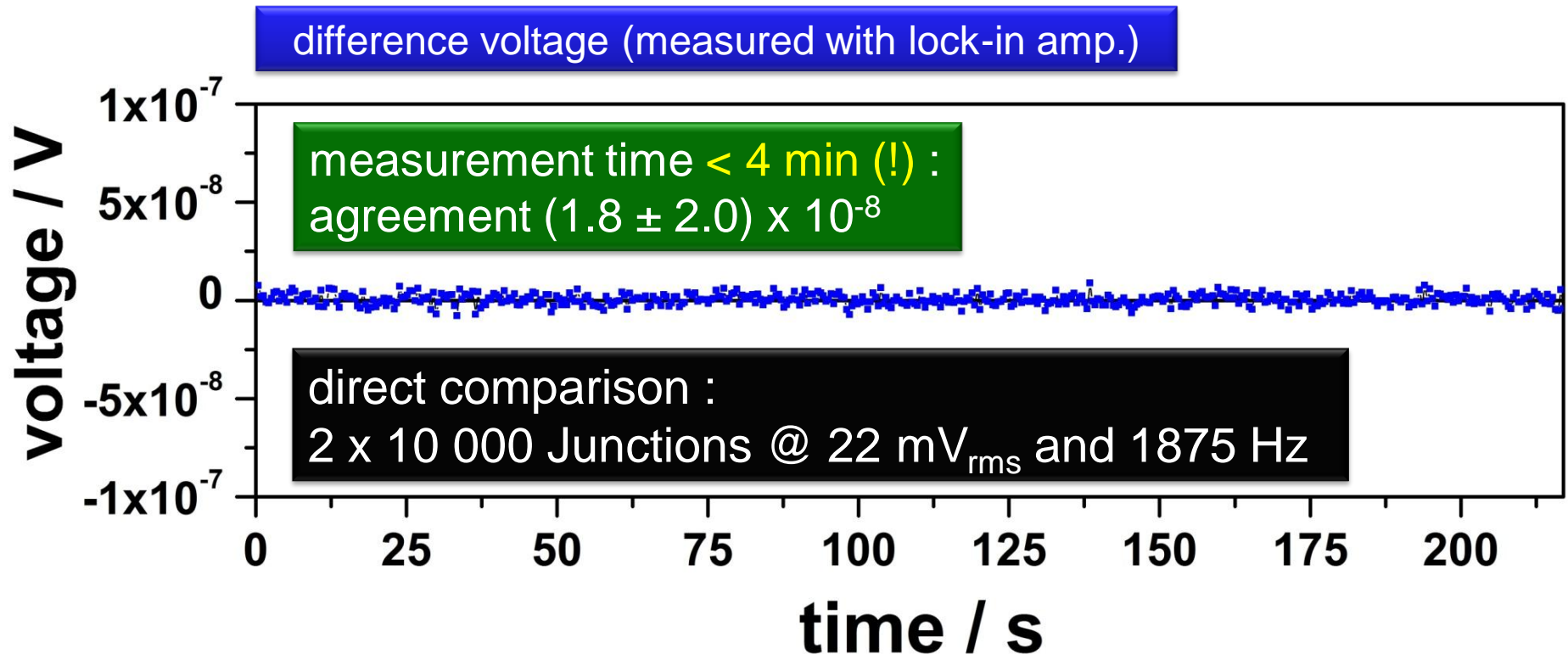


PXI 5922 :  
voltage difference  
below noise floor  
 $< 9 \text{ nV}_{\text{RMS}}$



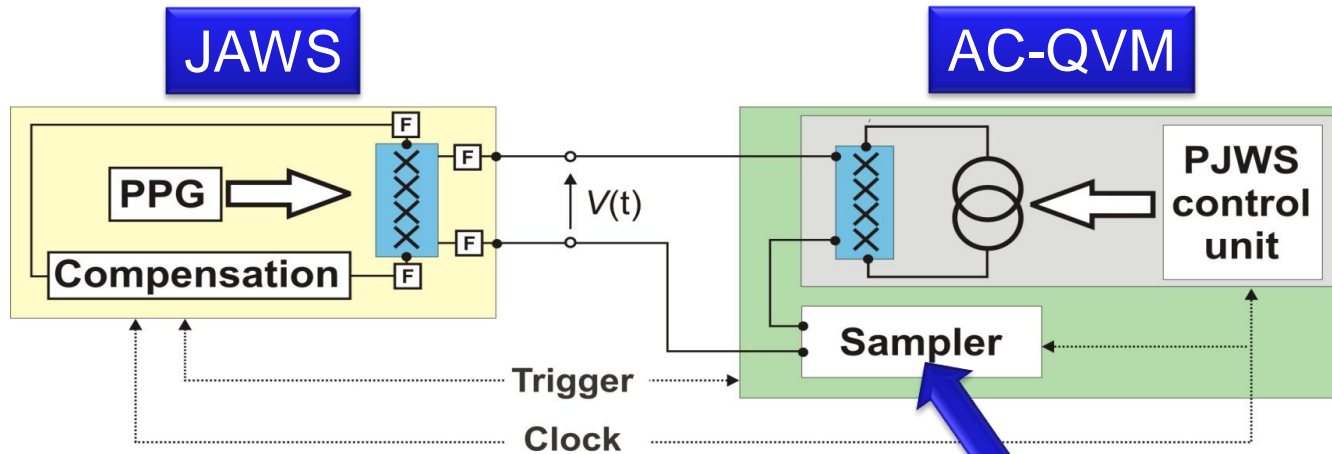
cancellation of waveform, when both arrays are switched on

# direct comparison : JAWS vs. JAWS (IV)




**high precision of JAWS !**

## direct comparison : JAWS vs. QVM



➤ **problem :**  
no second 1 V-JAWS available

➤ **solution :**   
QVM demonstrated :  $2 \times 10^{-8}$   
(J. Lee, CPEM 2014)

PXI 5922  
(National Instruments)

direct comparison @ 1 V level  
possible now !

# JAWS vs. QVM : QVM with PXI 5922

 PXI 5922 gain & offset are “not” stable

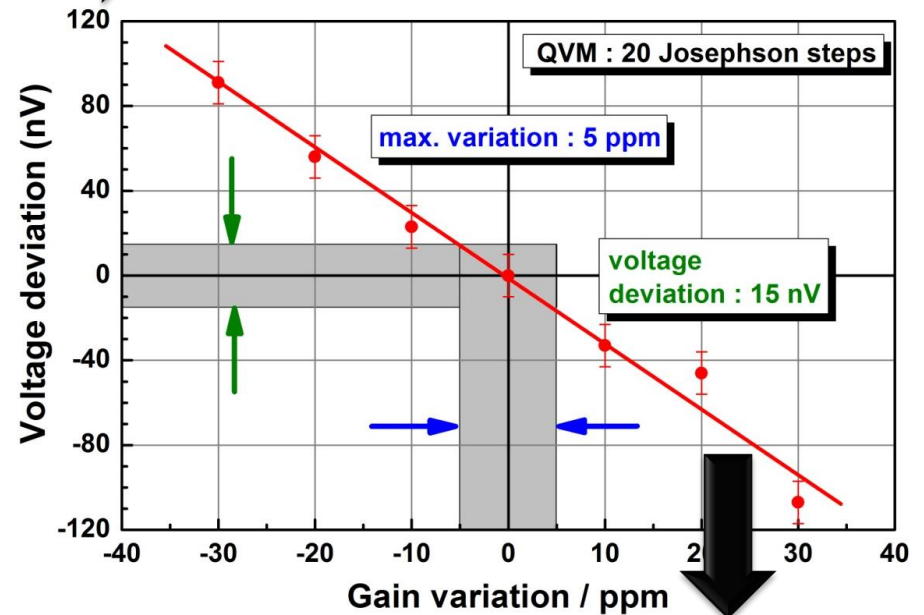
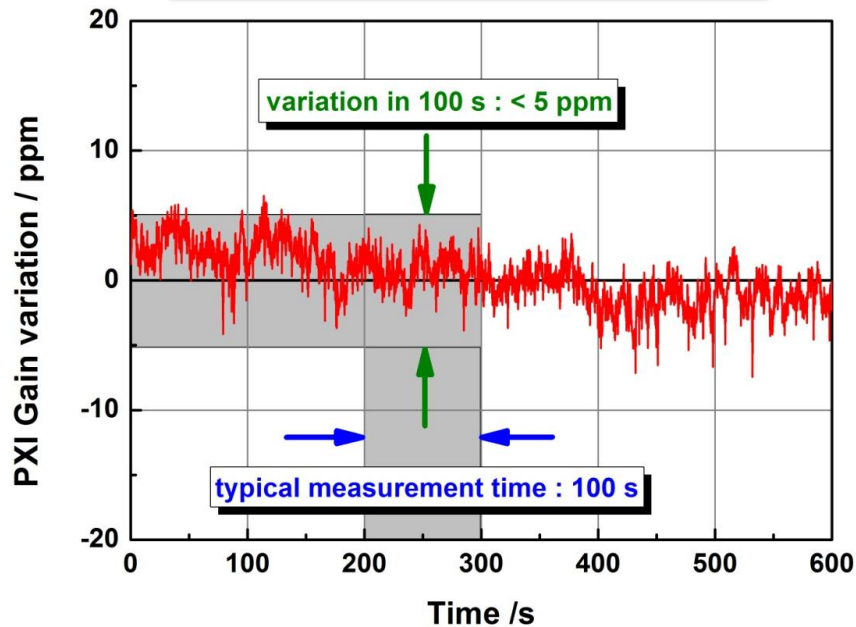
PXI 5922 : @ fixed sample rate of 4 MS/s or 10 MS/s

QVM : @ 150 mV<sub>p</sub> for evaluation of gain/offset

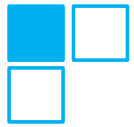
gain error is small ! 

time window → gain variation

gain window → voltage variation



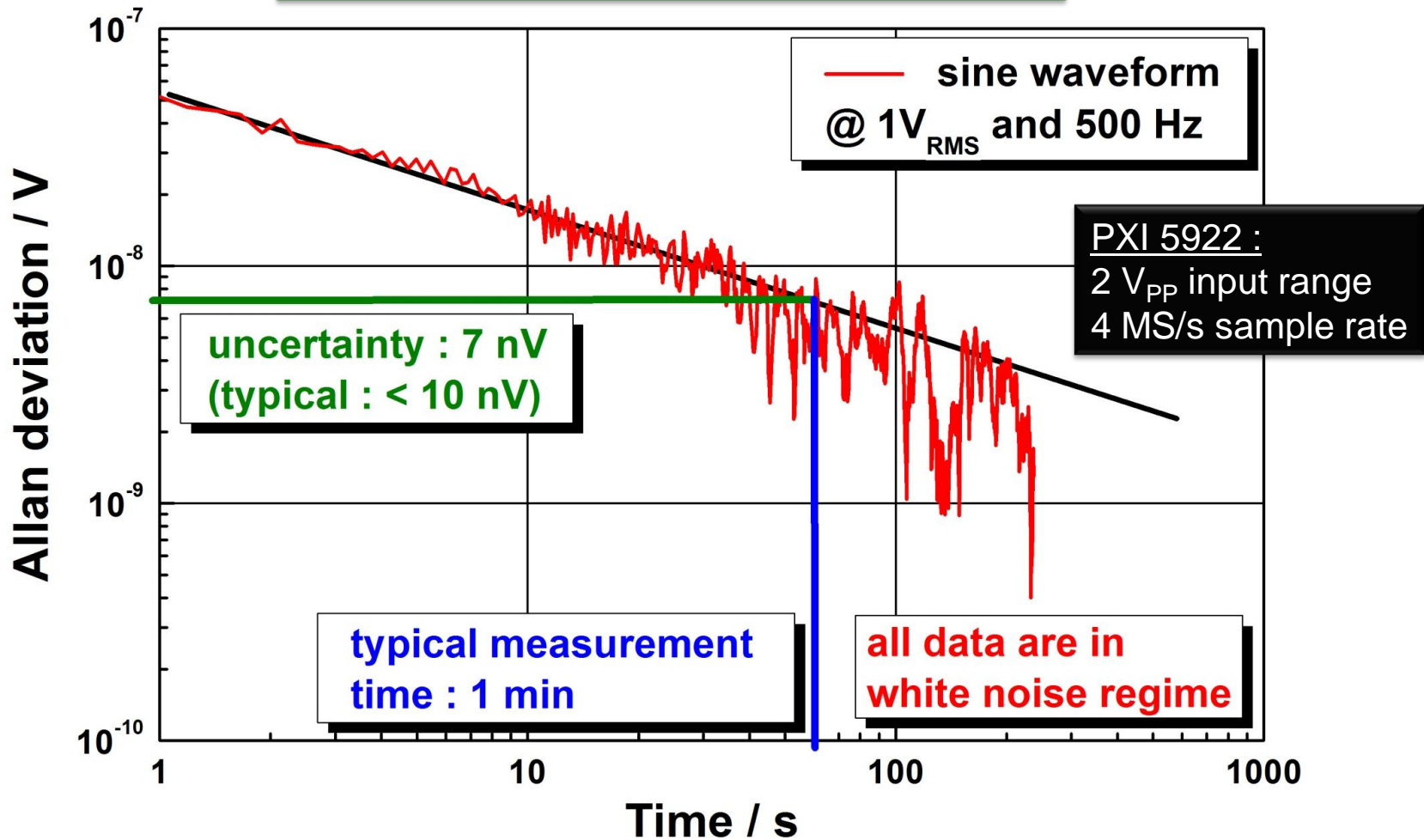
type-B uncertainty < 9 nV



# JAWS vs. QVM : measurement time



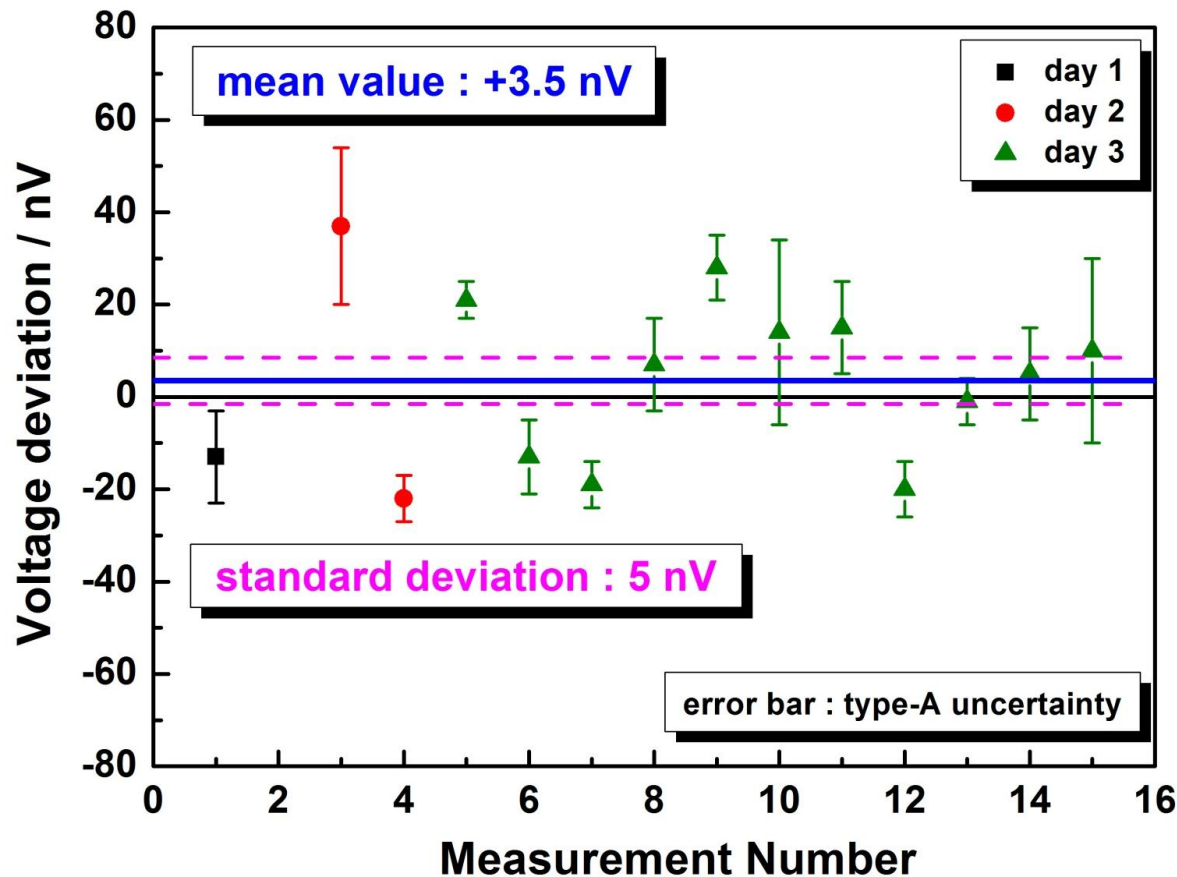
**excellent Allan deviation !**



# JAWS vs. QVM : comparison @ 250 Hz



$$V_{\text{JAWS}} - V_{\text{QVM}} = +3.5 \text{ nV} \pm 12 \text{ nV} @ 250 \text{ Hz}$$



comparison  
@ 1 V<sub>RMS</sub>



excellent  
ppb  
agreement



# outline



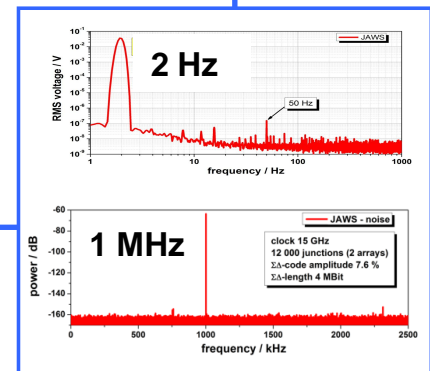
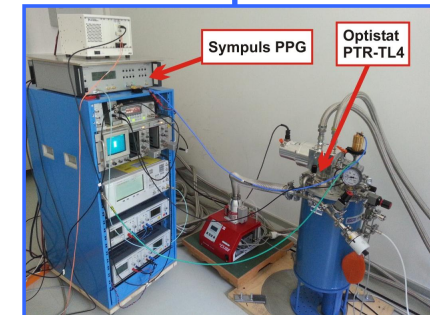
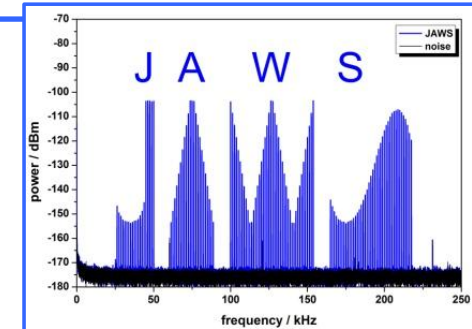
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# Summary (I)



## high-quality AC-waveforms

- $\text{Nb}_x\text{Si}_{1-x}$ - arrays with **triple-stacked** junctions
- up to **8 arrays** in series : **63 000 junctions**
- output voltage up to **1 V<sub>RMS</sub> (2.83 V<sub>PP</sub>)**
- high spectral purity : SNR better than **-120 dBc**
- high frequency range : **DC, 2 Hz ... 1 MHz**
- high **time stability** : **low noise** and **no drift**
- **arbitrary** waveforms demonstrated
- **JAWS** successfully operated in **cryocooler**

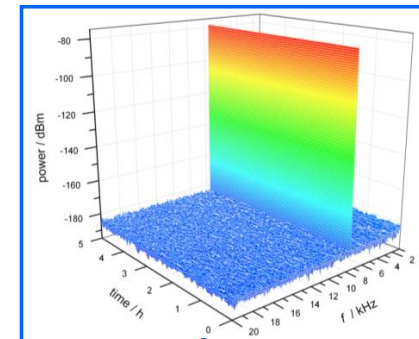


## Summary (II)

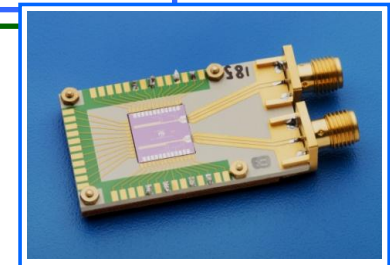


### high-quality AC-waveforms

- **3 JAWS systems operational :**
  - **JAWS 1 :  $1 V_{RMS}$**
  - **JAWS 2 : Impedance bridge with  $2 \times 100 mV_{RMS}$**
  - **JAWS 3 : PJVS + JAWS :  $1.18 V$  with SNR  $-125 dBc$**
- **first applications :** e.g. characterization of HF devices
- **direct comparison JAWS - JAWS :  $(1.8 \pm 2.0) \times 10^{-8}$  @ 1875 Hz**
- **direct comparison JAWS - PJVS :  $(3.5 \pm 11.7) \times 10^{-9}$  @ 250 Hz &  $1 V_{RMS}$**



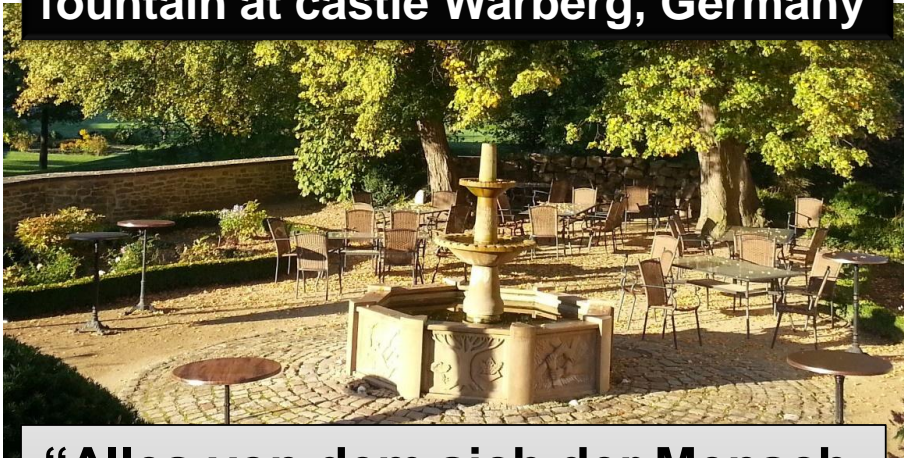
- **next steps :**
  - further reduction of crosstalk → new cryoprobe
  - more junctions per chip → less than 4 chips for 1 V



# 1 V JAWS: impact

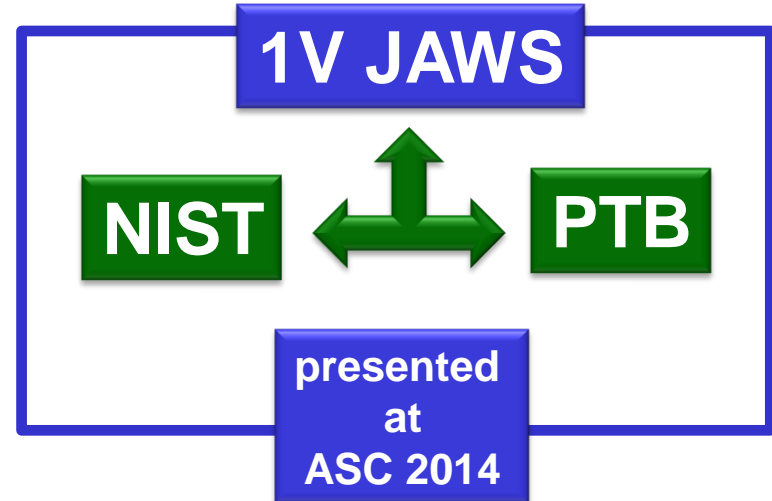


fountain at castle Warberg, Germany

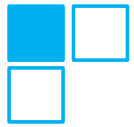


“Alles von dem sich der Mensch  
eine Vorstellung machen kann,  
ist machbar...”  
(W.v.B.)

“all what a man can imagine,  
is possible...”  
(W.v.B.)



„voltage source for arbitrary waveforms at the 1 V level  
with quantum precision and spectral purity“



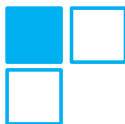
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# Thank you very much for your attention!



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