



Quantum sensing with superconducting flux qubits

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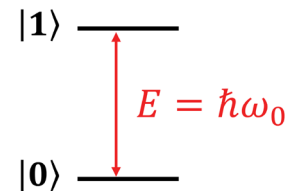


Quantum Sensing

1. Use of two-level nature

Energy levels are sensitive to external fields

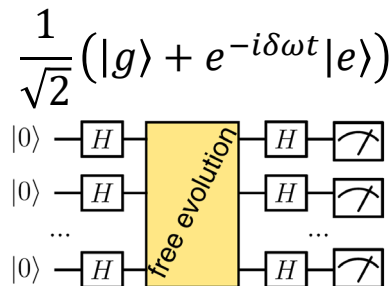
- Sensitivity $\propto (\# \text{ of qubits})^{1/2}$



2. Use of quantum coherence

Phase accumulation during free evolution of superposition states

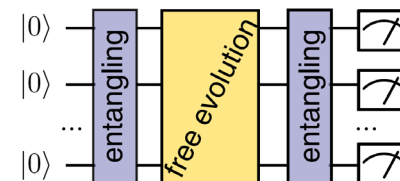
- Filter functions can be applied. (Frequency selectivity, DC or AC)
- Sensitivity $\propto (\# \text{ of qubits})^{1/2}$



3. Use of quantum entanglement

Phase accumulation during free evolution of entangled states

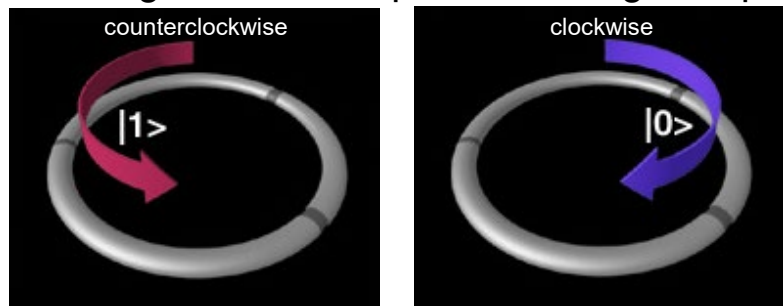
- Sensitivity $\propto (\# \text{ of qubits})^1$ (Heisenberg limit)



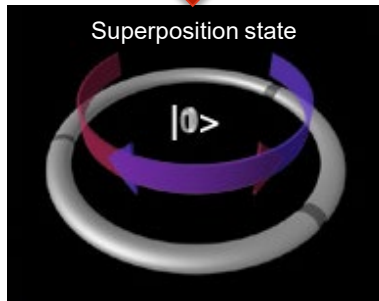
Superconducting flux qubit



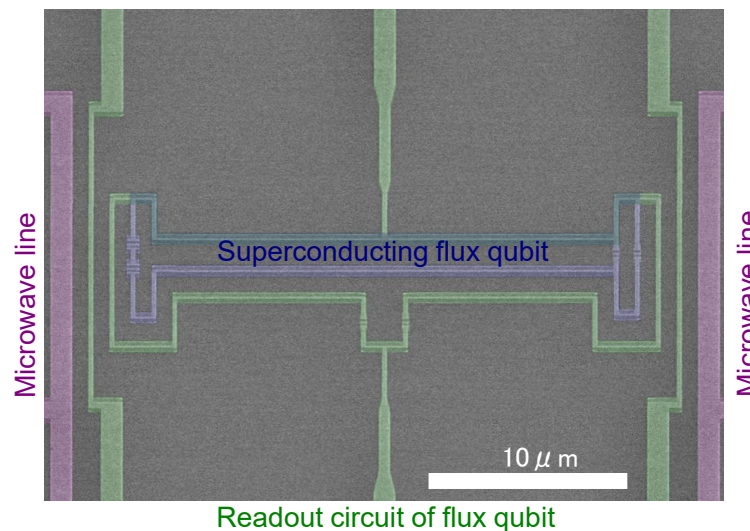
Circulating current in superconducting flux qubit



Superconductor ring
+ 3 Josephson junctions



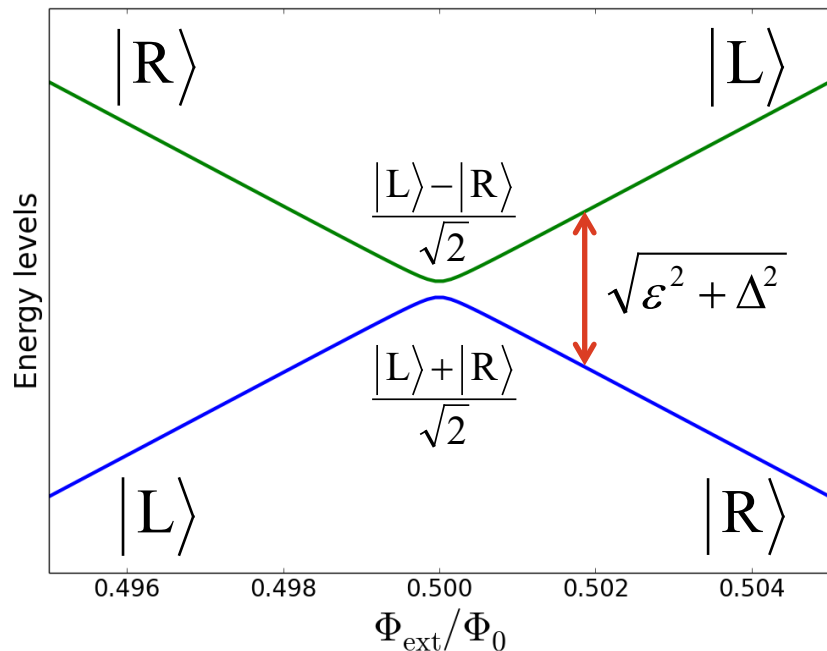
SEM picture of superconducting flux qubit



Mooij *et al.*, *Science* **285**, 1036 (1999)

Interaction between the circulating current and magnetic field is large.
→ Sensitive magnetic field detection is possible.

Superconducting flux qubit



$$\hat{H} = \frac{1}{2} (\epsilon \hat{\sigma}_z + \Delta \hat{\sigma}_x)$$

$$= \frac{\sqrt{\epsilon^2 + \Delta^2}}{2} \hat{\sigma}'_z$$

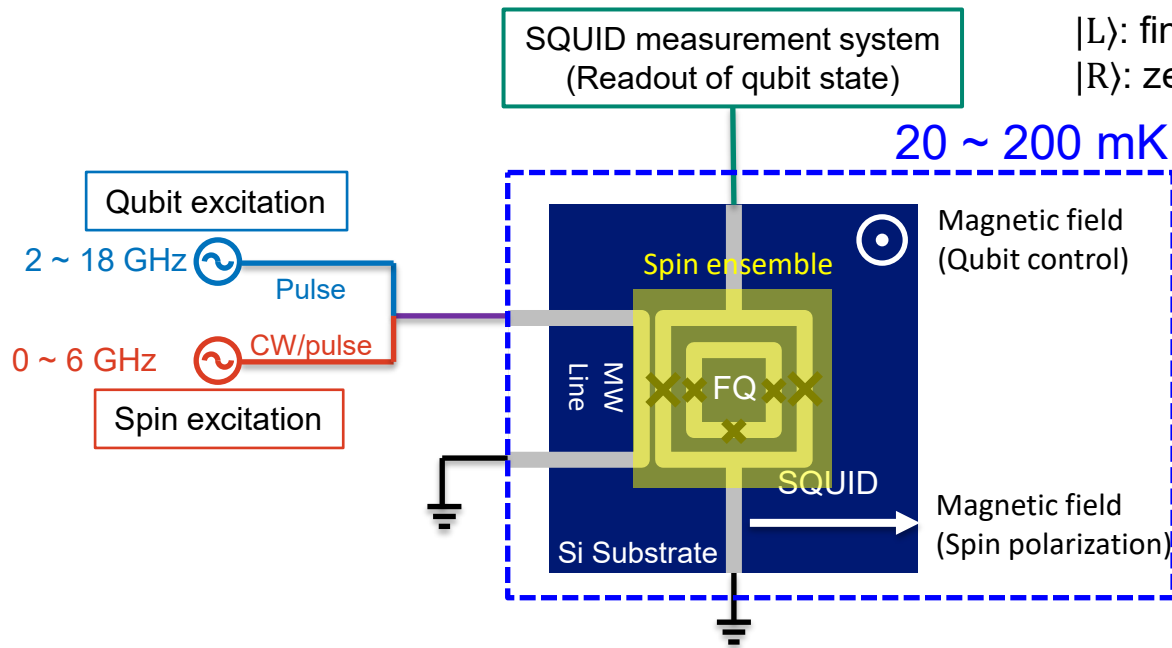
Magnetic field dependence



$$\begin{cases} \epsilon = 2I_p (\Phi_{\text{ext}} - \Phi_0/2) \\ I_p : \text{Persistent current (const.)} \\ \Delta : \text{Tunnel energy (const.)} \\ \hat{\sigma}_z, \hat{\sigma}_x : \text{Pauli matrix} \end{cases}$$

- The energy eigenstate is linear combination of $|L\rangle$ and $|R\rangle$.
- Transition frequency has dependence on the magnetic flux
→ Sensitive to magnetic field.
- Large persistent current I_p is desired. ($I_p \sim 300$ nA in design)

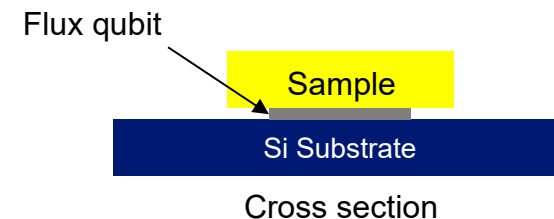
Spin detection using a flux qubit



Example:

$|L\rangle$: finite voltage output

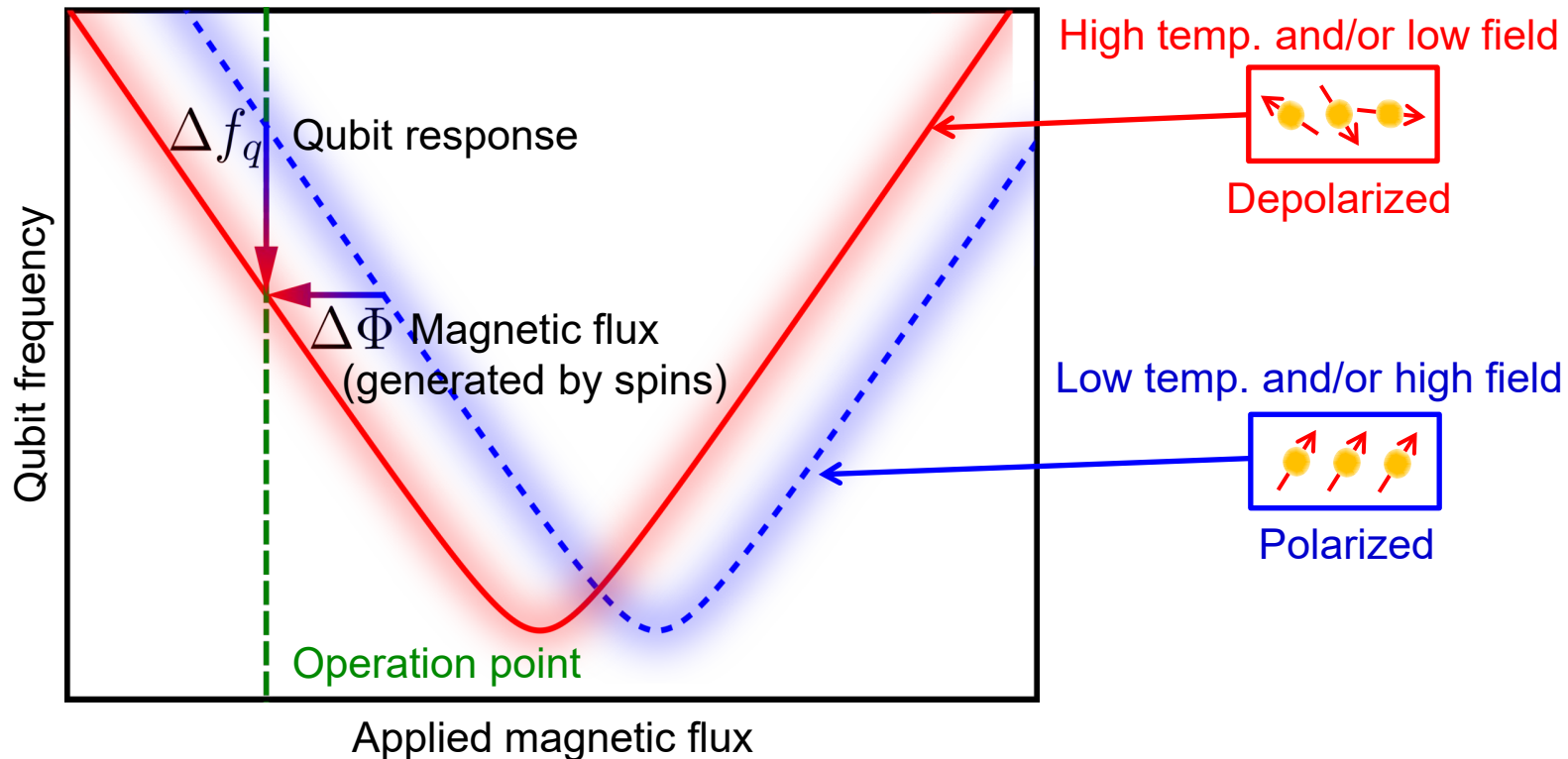
$|R\rangle$: zero voltage output



In-plane field and temperature dependence → Magnetometry

In-plane field and frequency dependence → Electron spin resonance

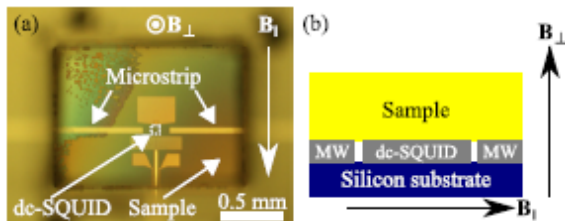
Spin detection using a flux qubit



Spin polarization is converted to qubit frequency

Electron spin detection using SC magnetometers

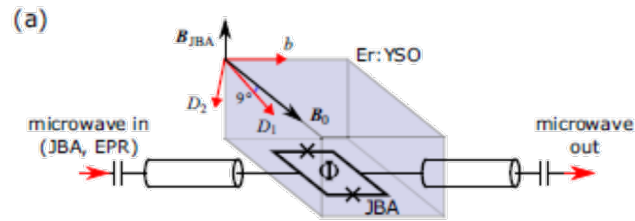
SQUID



10^6 spins/ $\sqrt{\text{Hz}}$

Toida *et al.*, 2016 APL

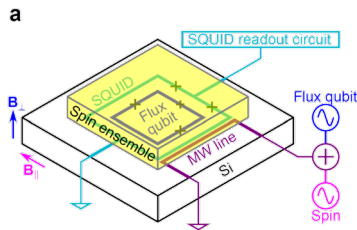
Josephson bifurcation amplifier (JBA)



Fast readout \rightarrow 15,000 spins/ $\sqrt{\text{Hz}}$

Budoyo *et al.*, 2018 PRMaterials

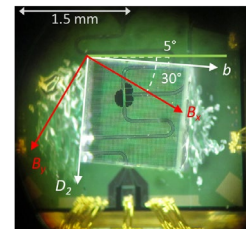
Flux qubit (SQUID readout)



Sensitive magnetometer \rightarrow 400 spins/ $\sqrt{\text{Hz}}$

Toida *et al.*, 2019 Commun. Phys.

Flux qubit (JBA readout)

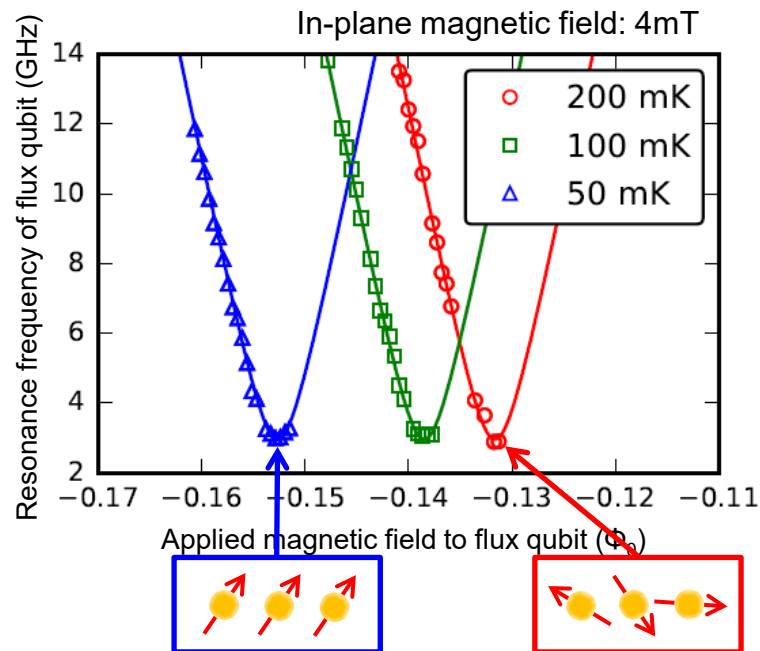
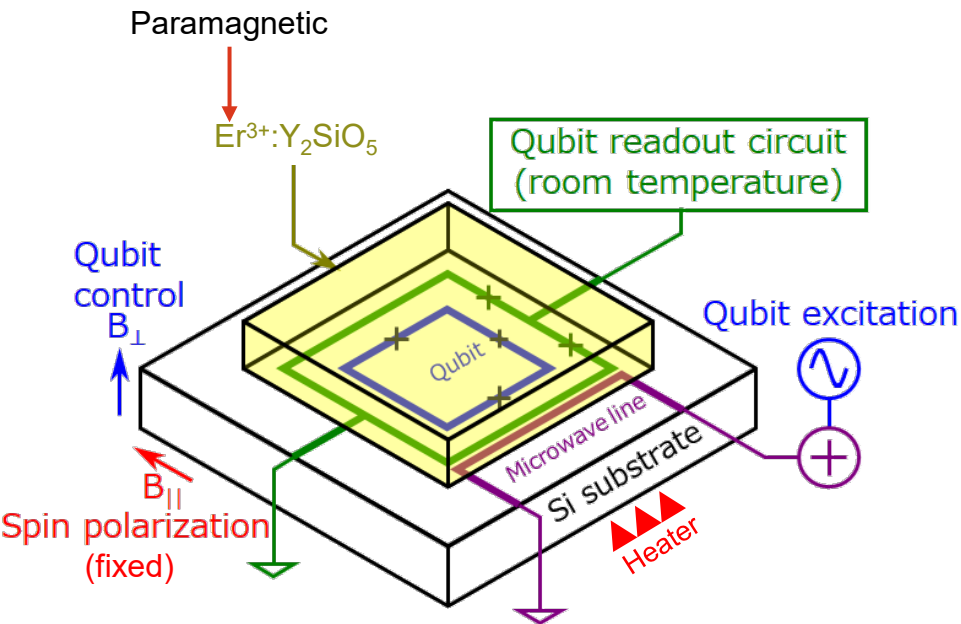


20 spins/ $\sqrt{\text{Hz}}$

Budoyo *et al.*, 2020 APL

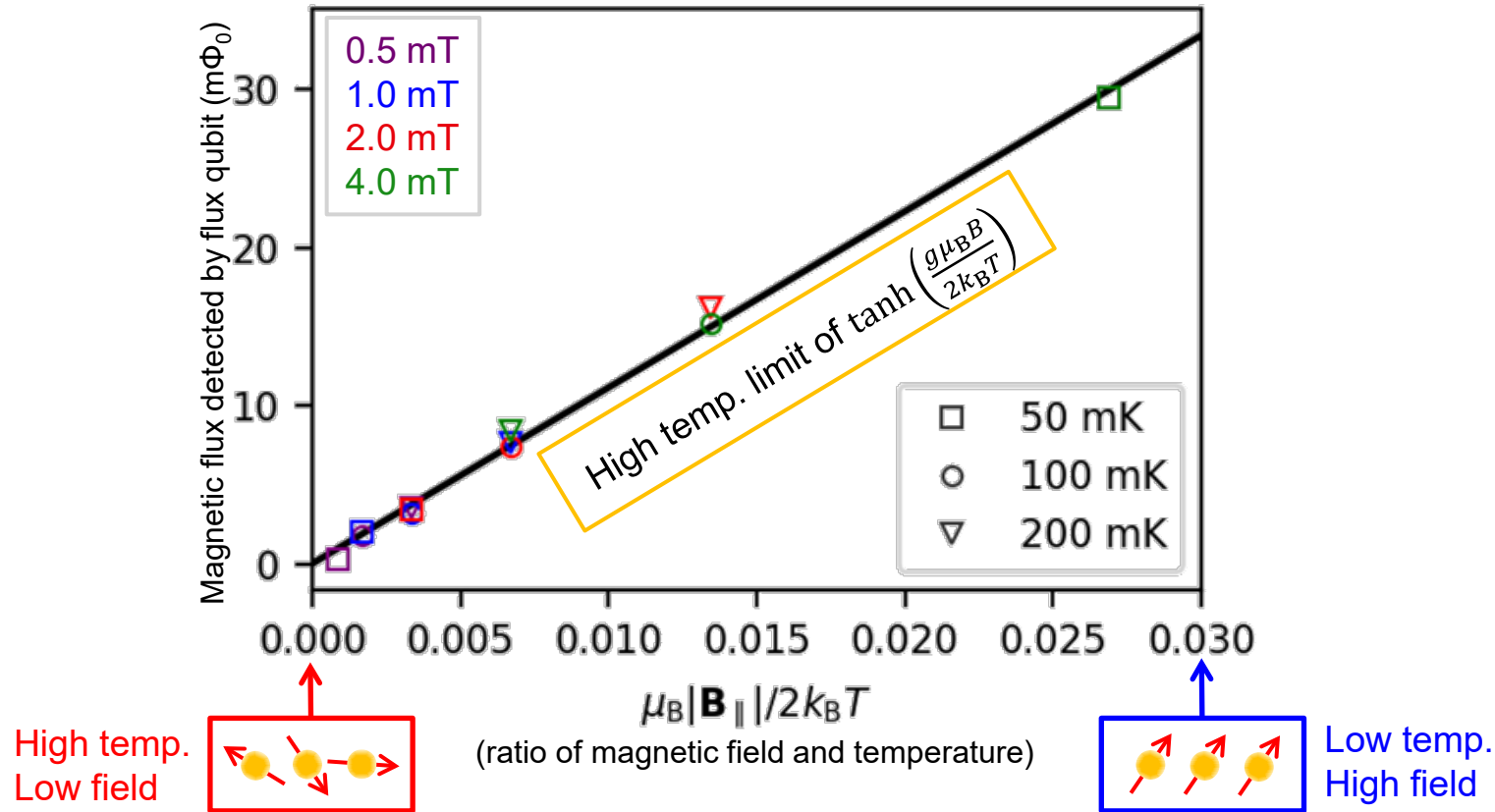
Sensitive spin detection is realized using SC spin detectors. (Now 12 spins/ $\sqrt{\text{Hz}}$)

Spin detection of $\text{Er}^{3+}:\text{Y}_2\text{SiO}_5$



Magnetization from electron spins is detected by a flux qubit

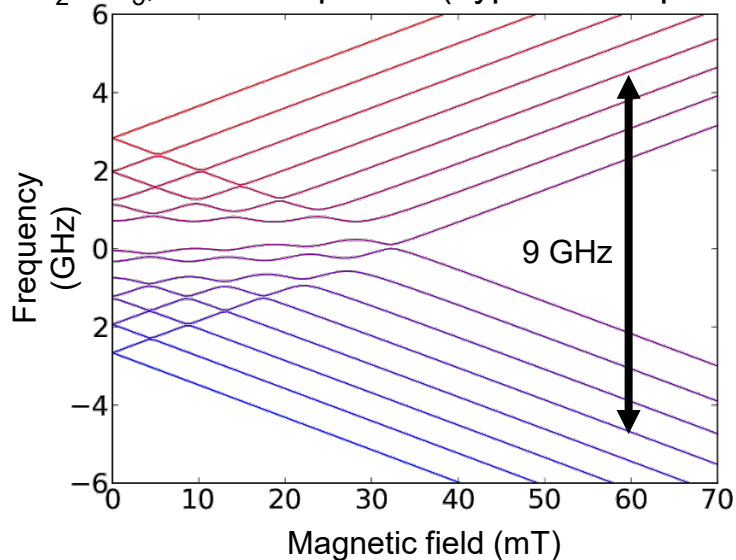
Spin detection of $\text{Er}^{3+}:\text{Y}_2\text{SiO}_5$



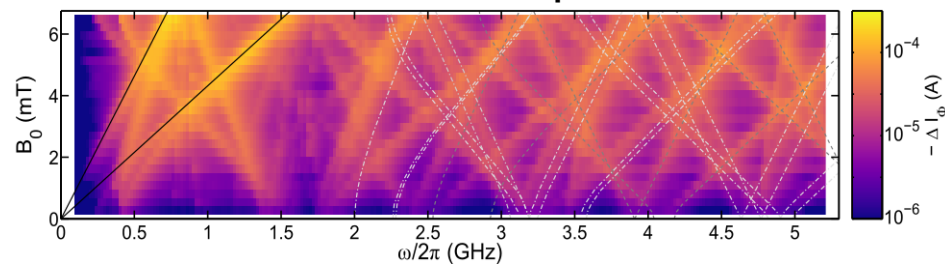
Curie's law in the high temperature limit is confirmed.

Application to material parameter estimation

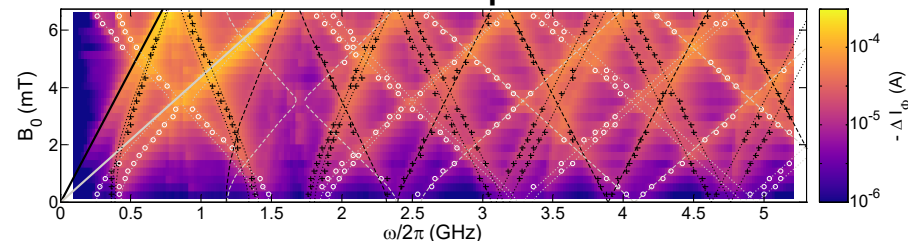
$\text{Er}^{3+}:\text{Y}_2\text{SiO}_5$, nuclear spin 7/2 (hyperfine + quadrupole)



Parameters from X band ESR spectrum



Parameters from our ESR spectrum



Standard ESR spectrometer
 → 0 – 0.3 T, X band ~9 GHz

ESR spectrometer using magnetometer
 → 0 - 6.5 mT, 0 - 5.2 GHz

Effect of hyperfine and quadruple interaction is small in the high field region
 → parameter estimation is not trivial

Effect of hyperfine and quadruple interaction is large in the small field region
 → suitable for parameter estimation

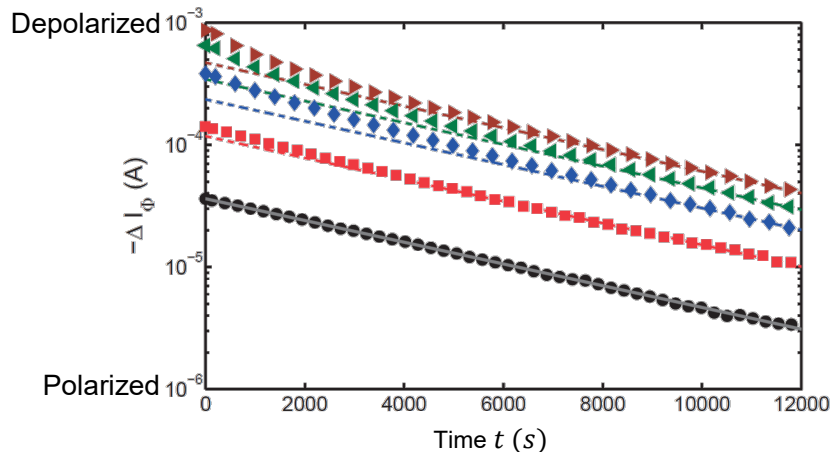
Measurement of spin relaxation time



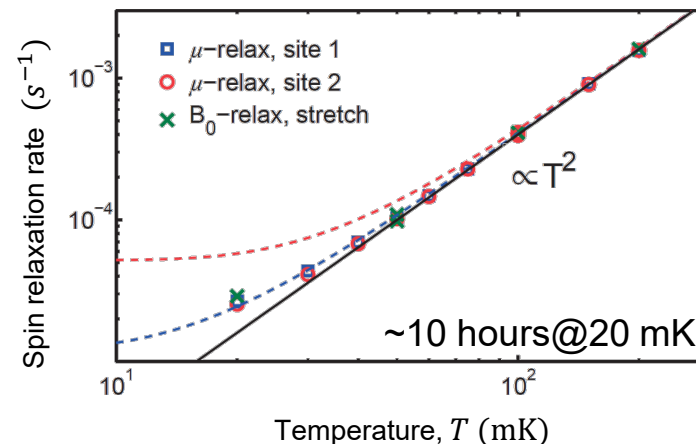
Usual relaxation

Sometimes limit the relaxation

→ Phonon bottleneck effect



→ non-exponential decay curve

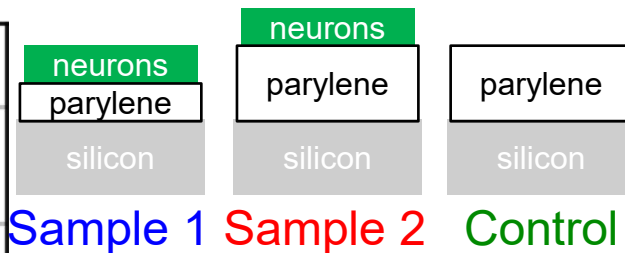
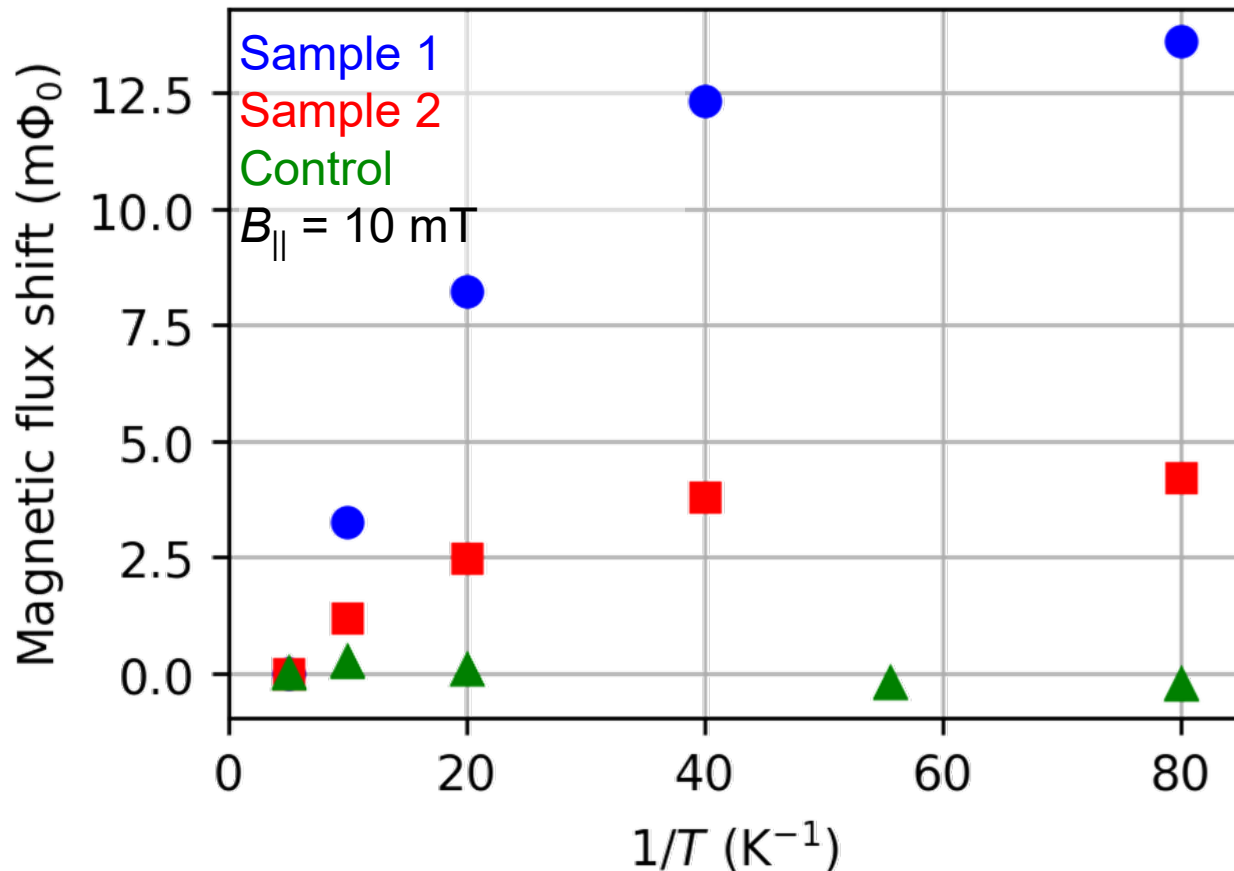


→ spin relaxation rate $\propto T^2$

Phonon bottleneck effect is suggested.

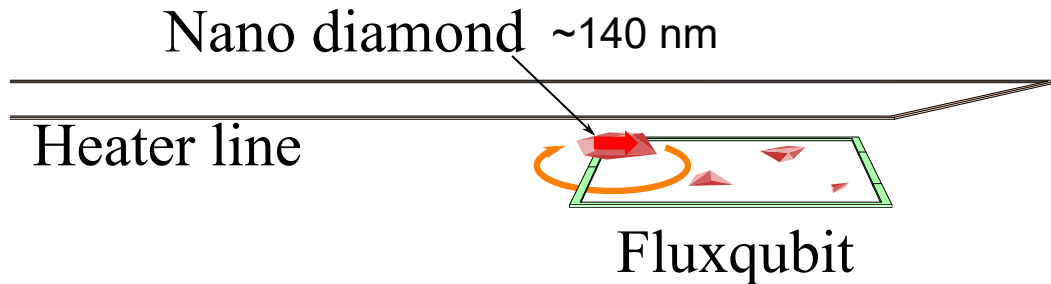
(Our ESR is suitable to observe the effect because no energy is transferred to measurement system)

Magnetometry of neurons

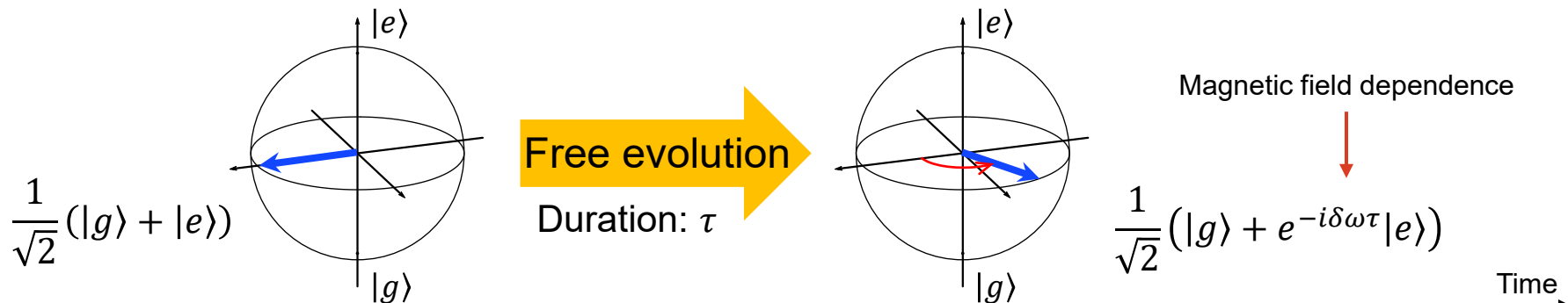


- Control experiment shows **smaller** magnetization.
- Sample with thinner insulator shows larger signal.
- Spins in **neurons** are observed.
- Spins are identified as Fe^{3+} ions. (Details are not discussed here.)

Thermometry using Ramsey oscillations

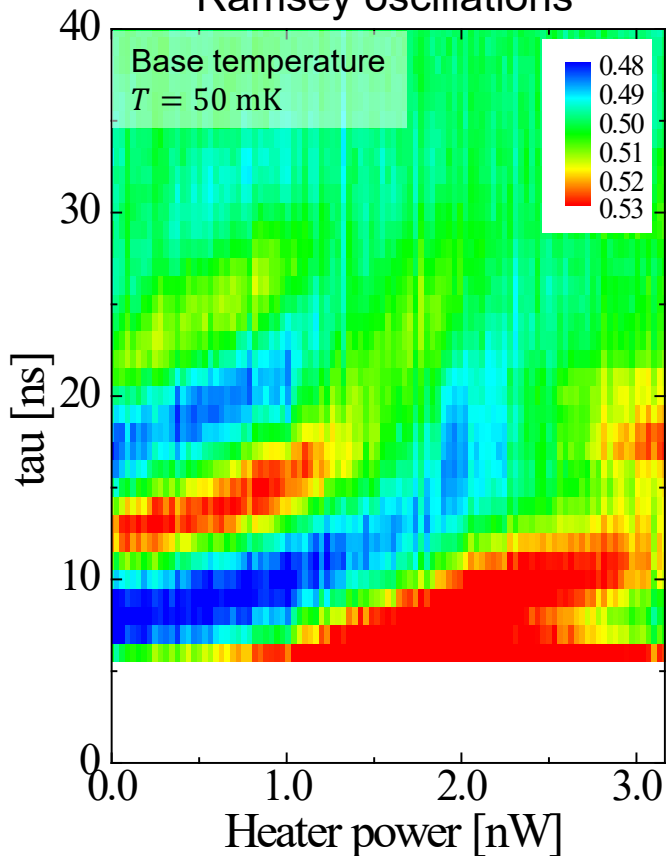


1. The temperature of nano diamond is controlled by heater power.
2. The magnetization of nano diamond changes as a function of the temperature.
3. The magnetic field (magnetization) changes Ramsey frequency of the qubit.



Thermometry using Ramsey oscillations

Ramsey oscillations

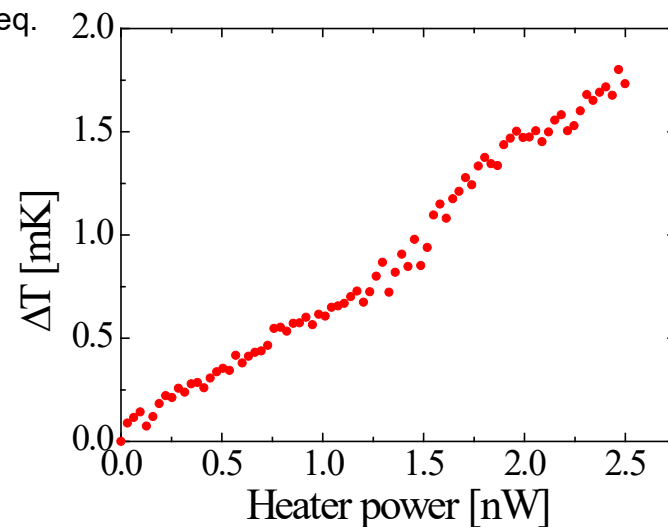


Ramsey frequency:

$$\delta\omega = \sqrt{\Delta^2 + \varepsilon(B)^2} - \omega_0$$

Calibration constants

Temperature difference



Sensitivity: $1.3 \mu\text{K}/\sqrt{\text{Hz}}$ @ 9.1 mK

Estimation of the sensitivity of FQ ESR

Noise in qubit measurement
(e.g., Variation in switching probability)

$$\sigma P_{sw}$$

×

$$\frac{\partial f_q}{\partial P_{sw}}$$

×

$$\frac{\partial \Phi}{\partial f_q}$$

×

$$\frac{\partial N}{\partial \Phi}$$

(Slope of qubit spectrum)⁻¹

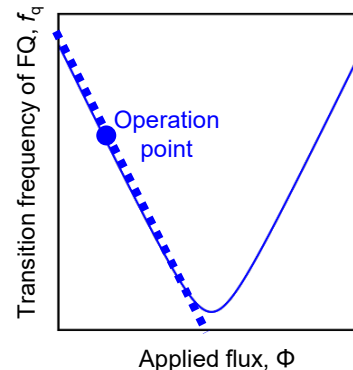
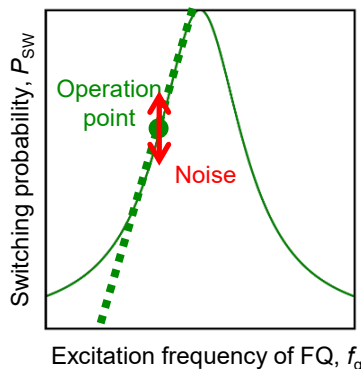
Linewidth of FQ

(magnetic flux generated by single spin)⁻¹

Narrow linewidth / small slope



Wide linewidth / large slope

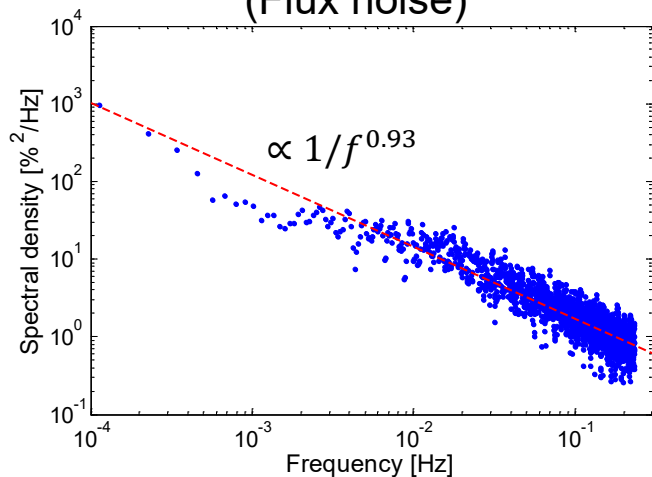


Our best sensitivity ~ 12 spins/√Hz

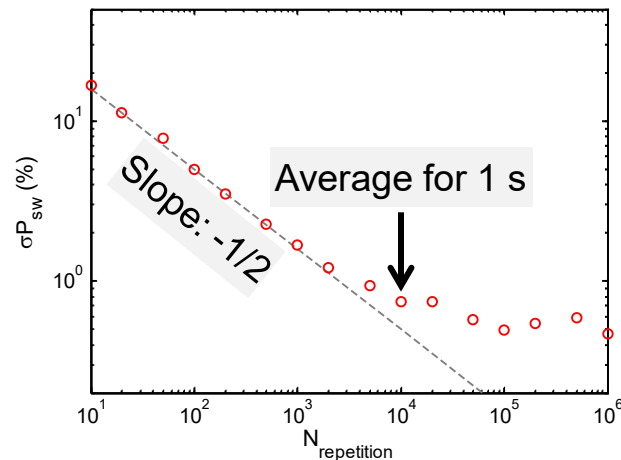
1/f noise of qubit readout devices (SQUID)



Power spectrum density
(Flux noise)



Readout noise vs. averaging



- Averaging is less effective for long integration time due to $1/f$ flux noise
 - $1/f$ flux noise also limits the coherence time (linewidth) of the flux qubit
- limitation factor of the sensitivity

Our Team



Quantum Sensing (Theory)



Dr. Munro
(→ OIST)



Dr. Matsuzaki
(→ Chuo Univ.)

Biomaterial

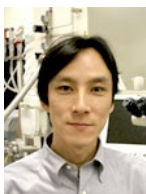


Dr. Teshima

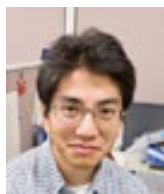


Dr. Sakai

Superconducting Circuits



Dr. Saito



Dr. Kakuyanagi



Dr. Mahboob



Dr. Toida



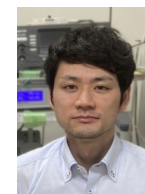
Dr. Budoyo

NTT

ESR Spectroscopy



Prof. Ono



Prof. Hori

Shizuoka University

Summary

Sensitive spin detection using flux qubits is realized

- Sensitivity: 12 spins/ $\sqrt{\text{Hz}}$, Spatial resolution: $\sim \mu\text{m}$
- Magnetometry, electron spin resonance, thermometry
- Application: solid state material, biomaterial, etc.

Future works

- Single spin detection
- Spin imaging
 - › Qubit array
 - › Scanning qubit
 - › Microwave interference
- Entanglement sensor using multiple flux qubits