



Aalto University
School of Science

Govenius et al., PRL 117, 030802 (2016)



Detecting zJ microwave pulses

– using calorimetry and electrothermal feedback

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Motivation

Lack of an efficient photodetector
for itinerant microwave photons

But there's progress!
e.g., Inomata et al., Nature
Comm. 7, 12303 (2016)



Applications:

- quantum computing/communication protocols
Examples: Govenius et al., PRA **92**, 042305 (2015)
& references therein.
- quantum thermodynamics
J. P. Pekola, Nature Phys. **11**, 118 (2015).
- photon correlation measurements
da Silva et al. PRA **82**, 043804 (2010).
Bozyigit et al., Nat. Phys. **7**, 154 (2011).

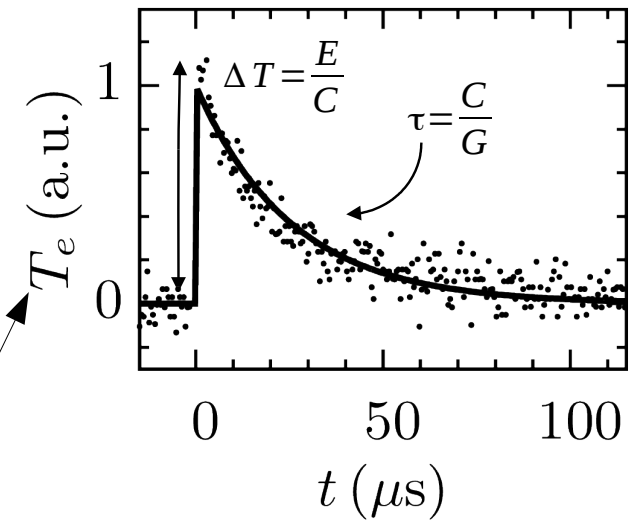
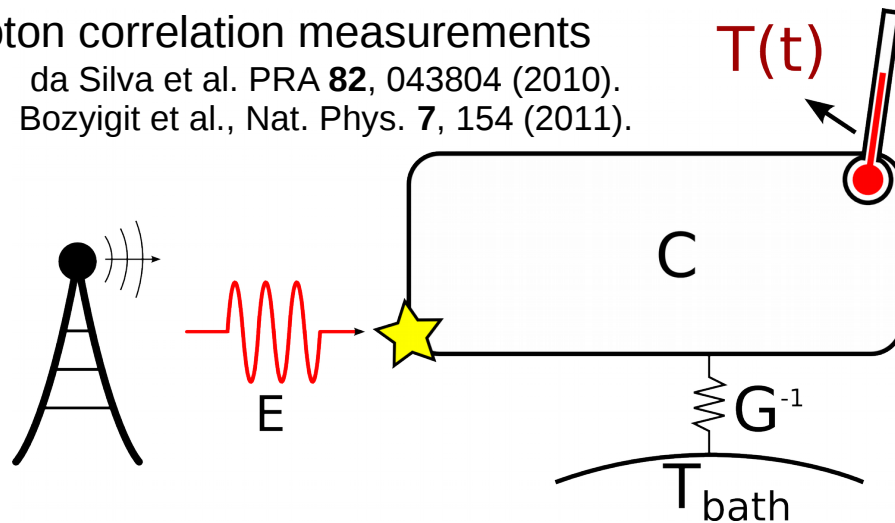
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Can we use calorimetry?

Good review on THz calorimeters:
 B. Karasik et al.,
 IEEE Trans. Terahertz Sci. **1**, 97 (2011)

$$\Delta E = h \times 23 \text{ THz} = 15 \text{ zJ}$$

in

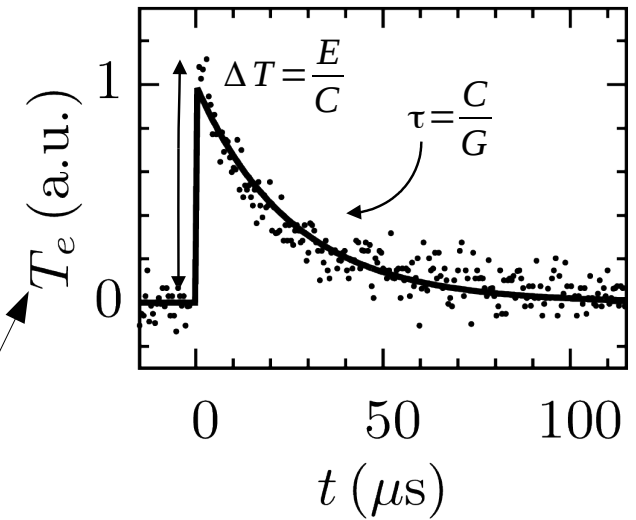
Santavicca et al., APL **96**, 083505 (2010).
 Karasik et al., APL **101**, 052601 (2012).

Ours: $200 \times h \times 8.4 \text{ GHz} = 1.1 \text{ zJ}$

= -110 dBm x 100 ns

Outline

- Principle of operation (“linear response”)
- Electrothermal nonlinearity
- Detection of zJ pulses
- (Noise equivalent power)



Can we use **calorimetry**?

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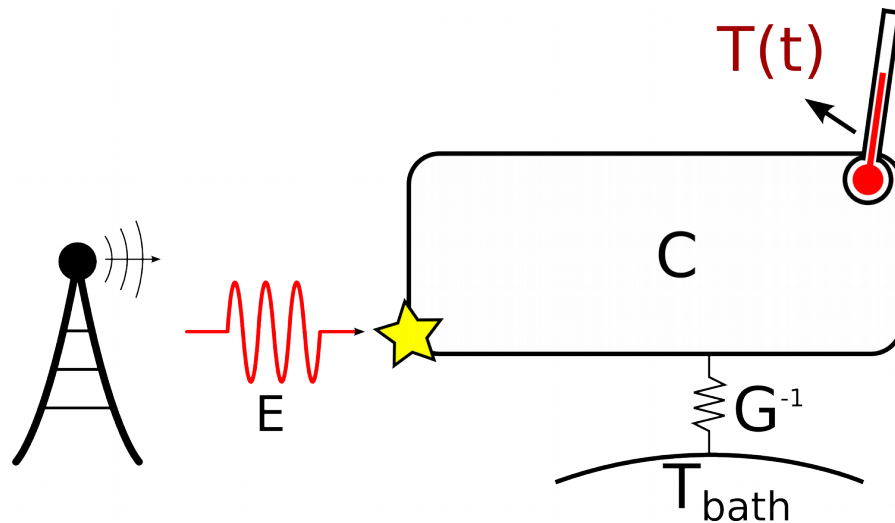
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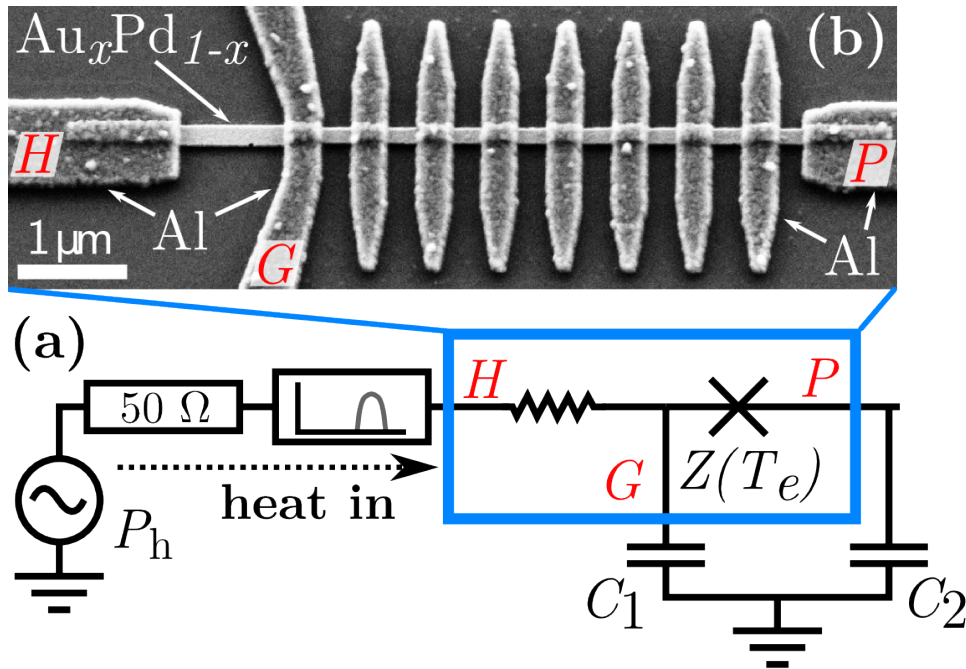
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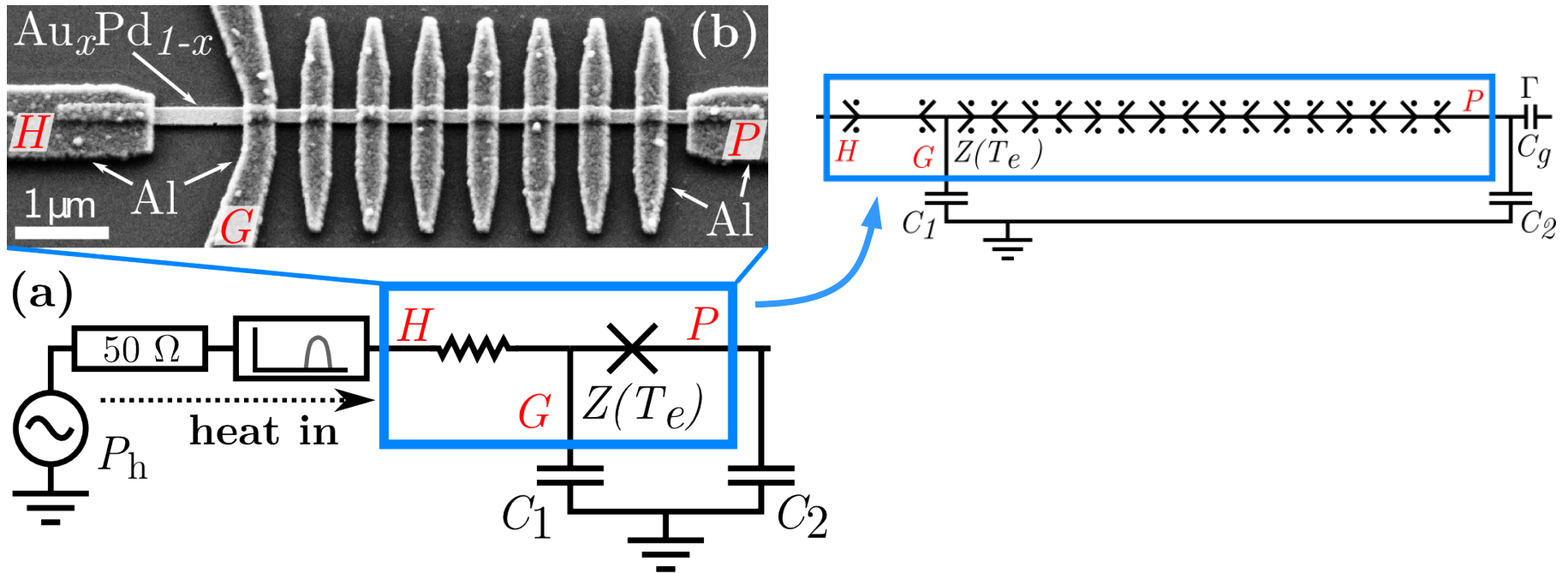
Principle of operation

8 GHz microwave power $\rightarrow T_e \rightarrow$ 750 MHz electrical output



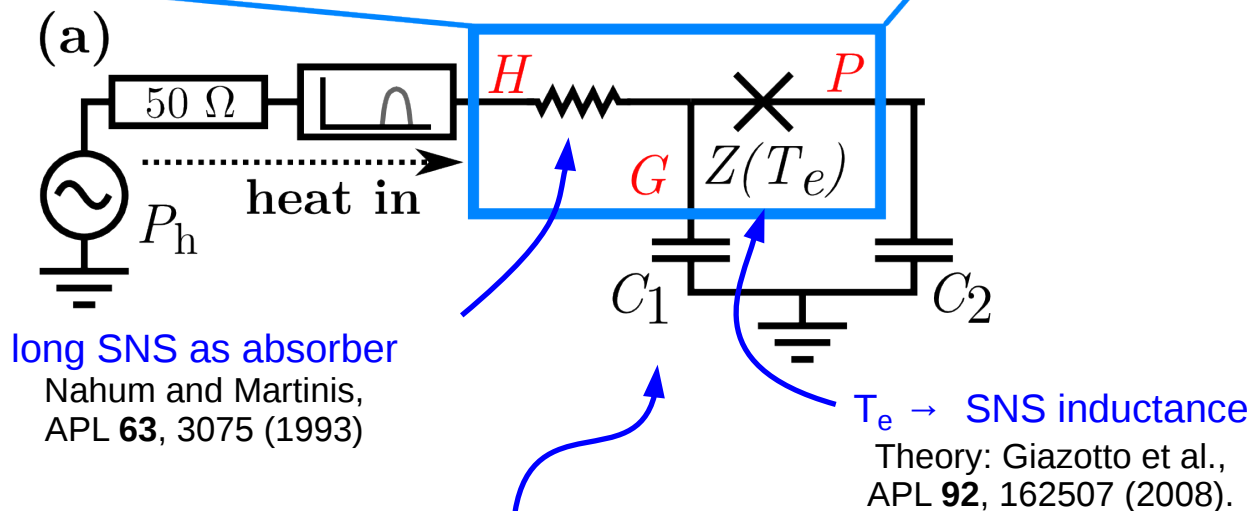
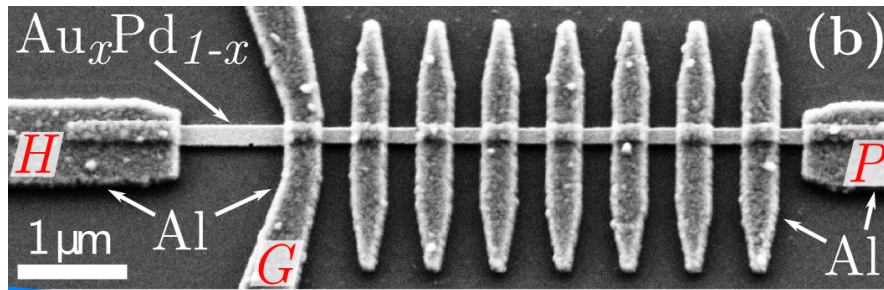
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Principle of operation

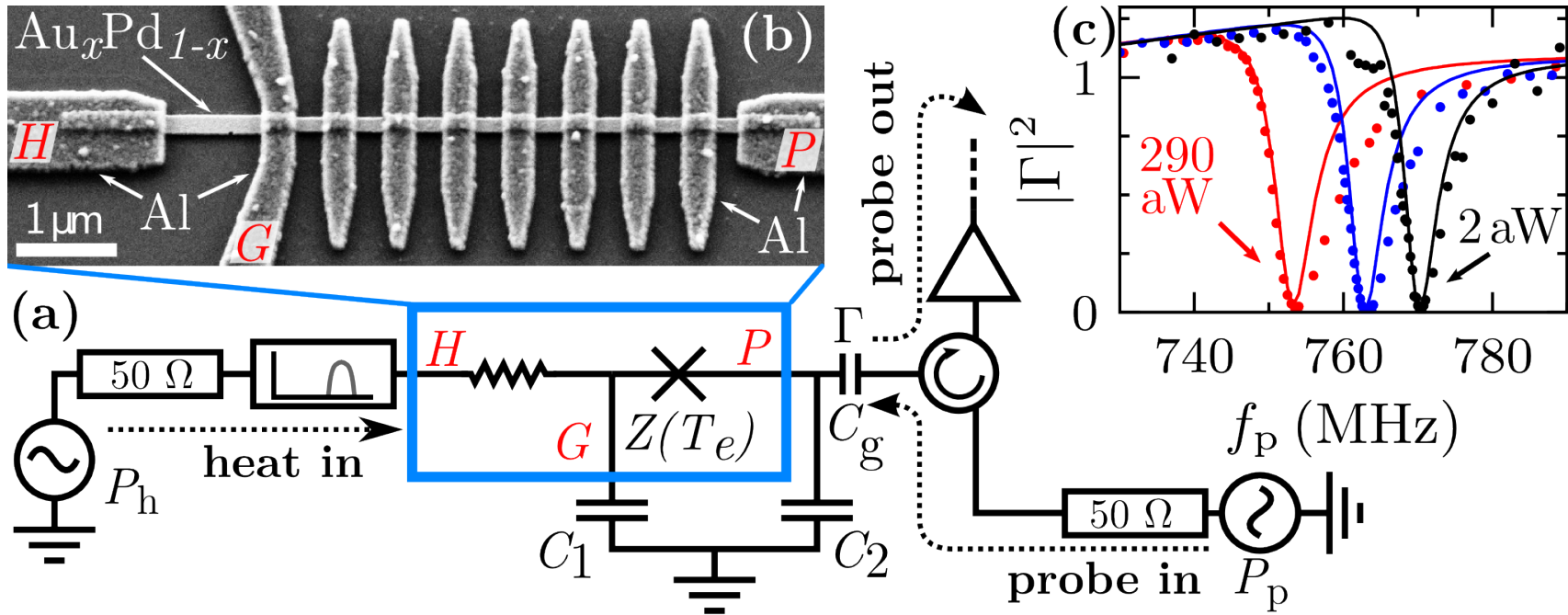
8 GHz microwave power $\rightarrow T_e \rightarrow$ 750 MHz electrical output

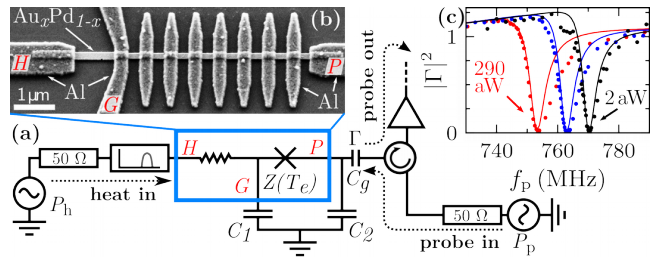


Alternative: $T_e \rightarrow$ SIN resistance + RF readout
Schmidt, Yung and Cleland, APL **83**, 1002 (2003).
Gasparinetti et al., Phys. Rev. Appl. **3**, 014007 (2015)

Principle of operation

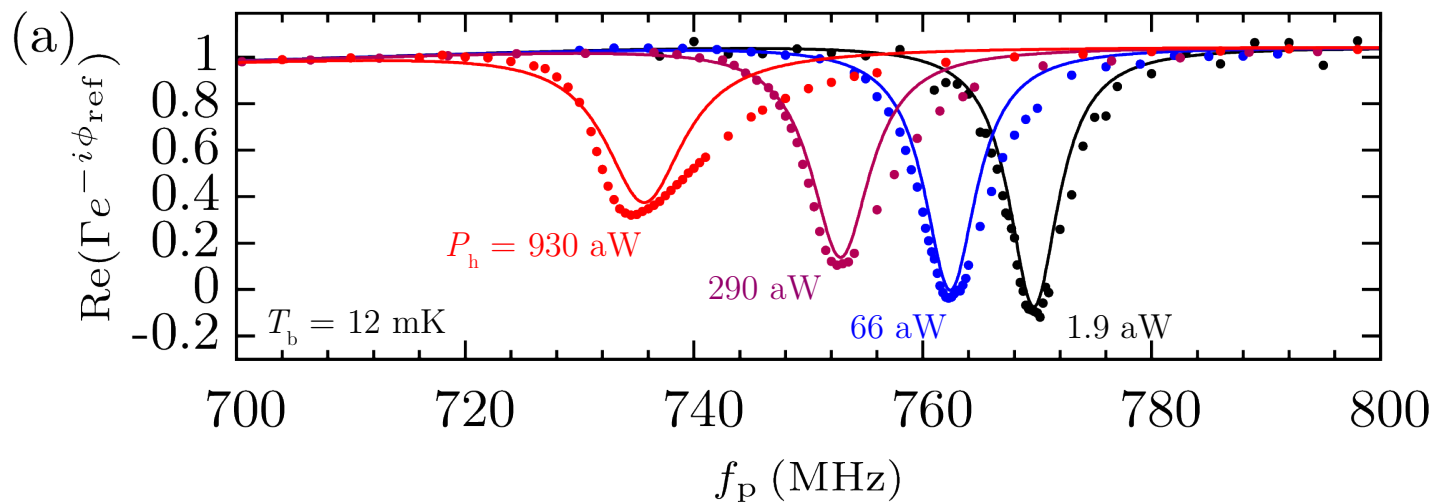
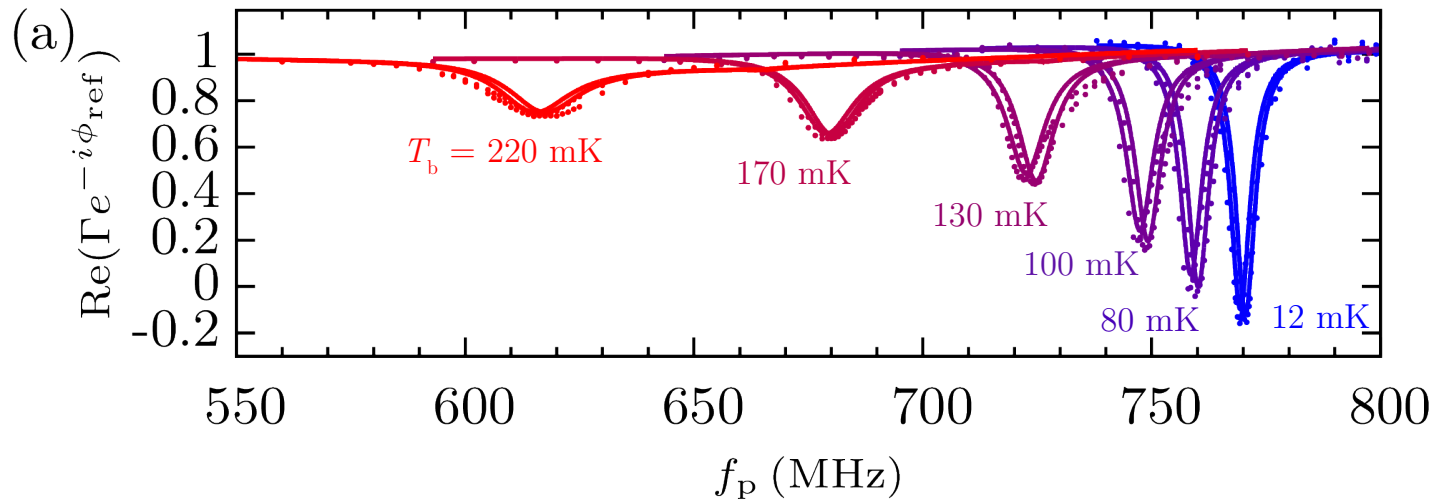
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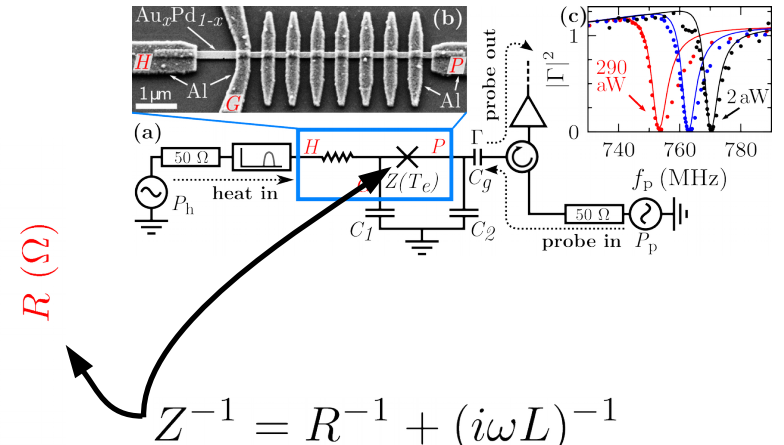
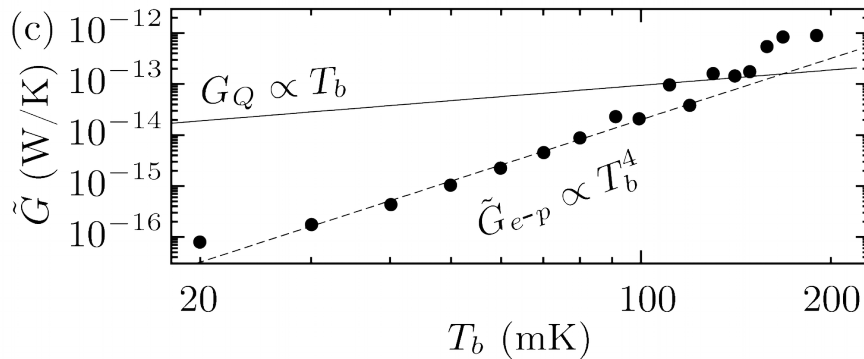
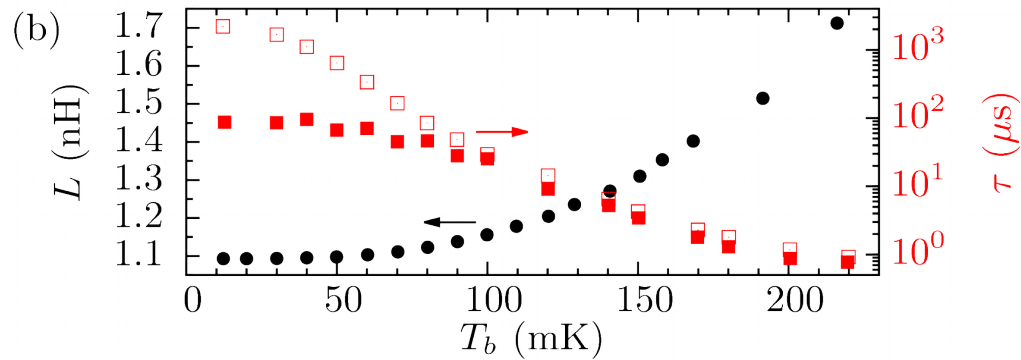
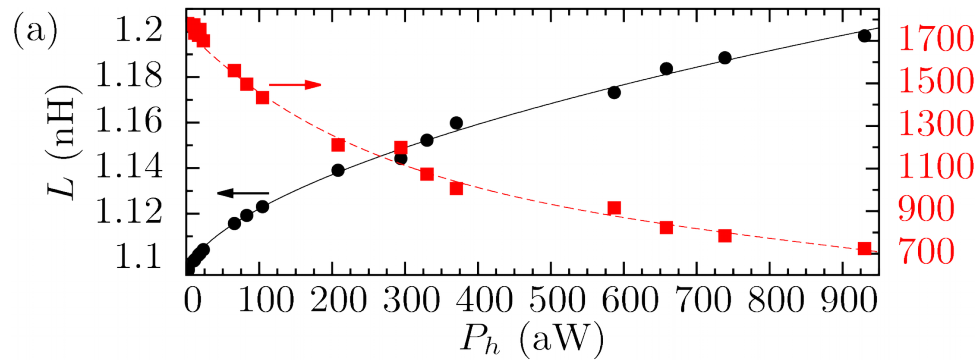


Effect of T_b and P_h

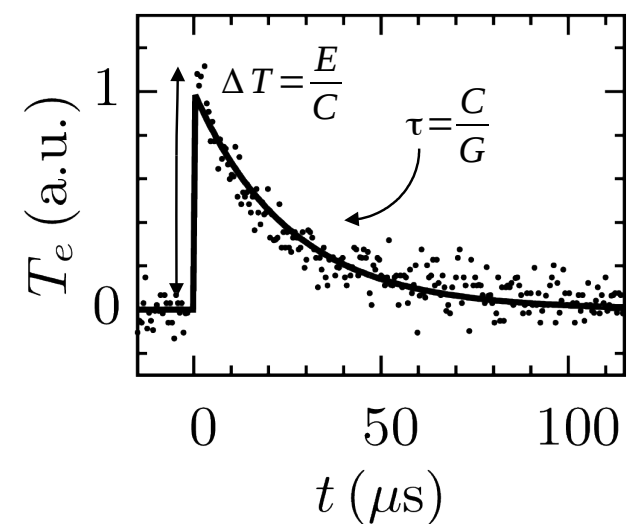
- linear response



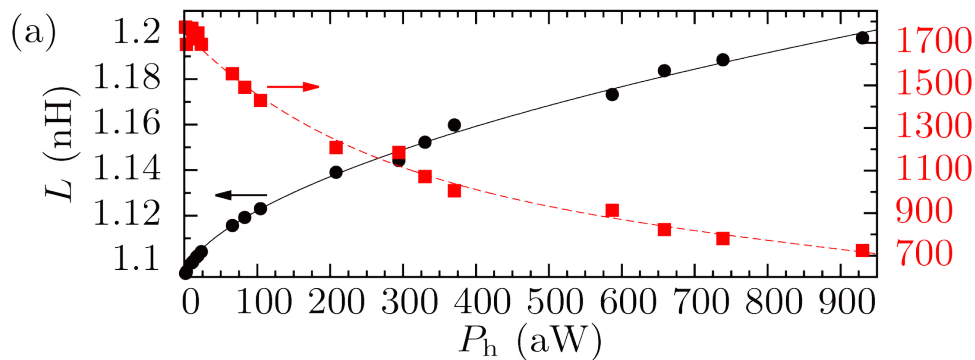
Linear response



$$Z^{-1} = R^{-1} + (i\omega L)^{-1}$$



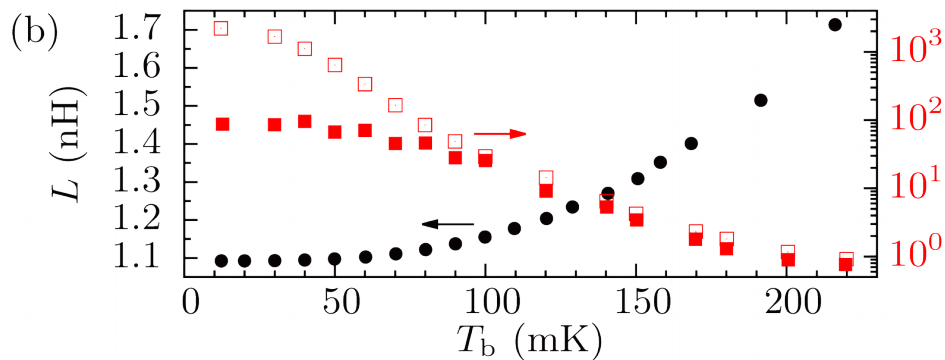
Linear response



1700
1500
1300
1100
900
700

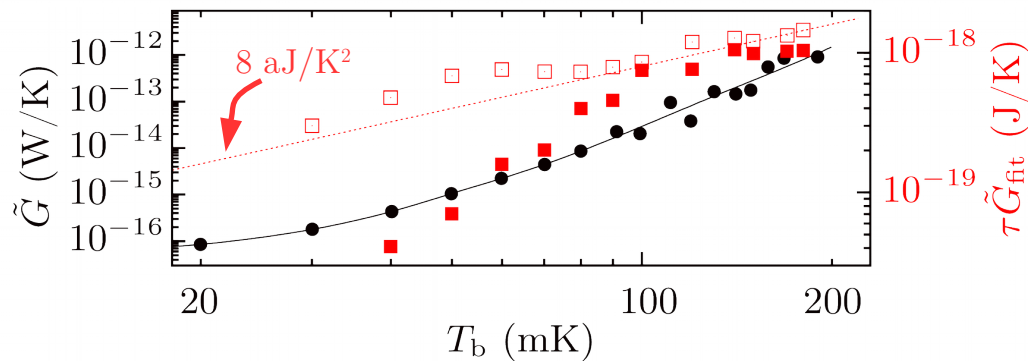
$R (\Omega)$

$$Z^{-1} = R^{-1} + (i\omega L)^{-1}$$



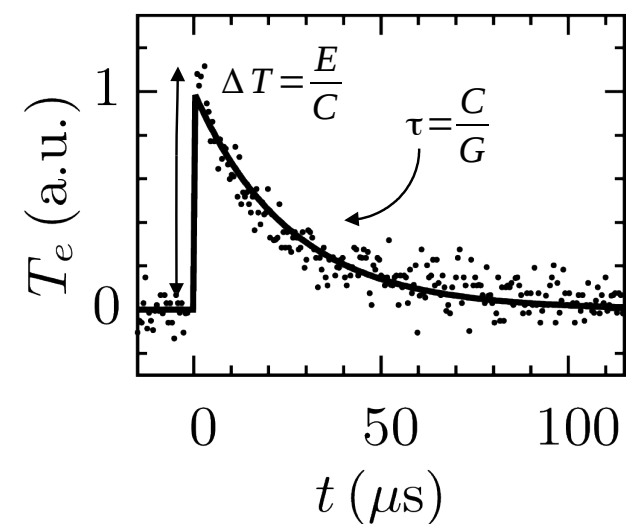
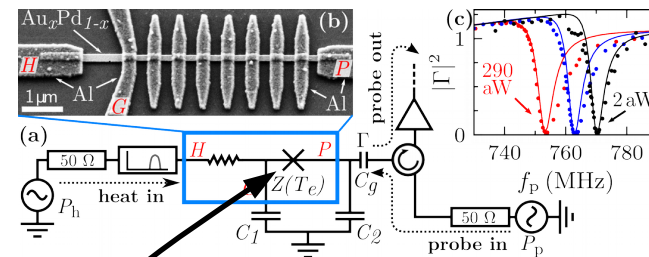
10^3
 10^2
 10^1
 10^0

$\tau (\mu s)$

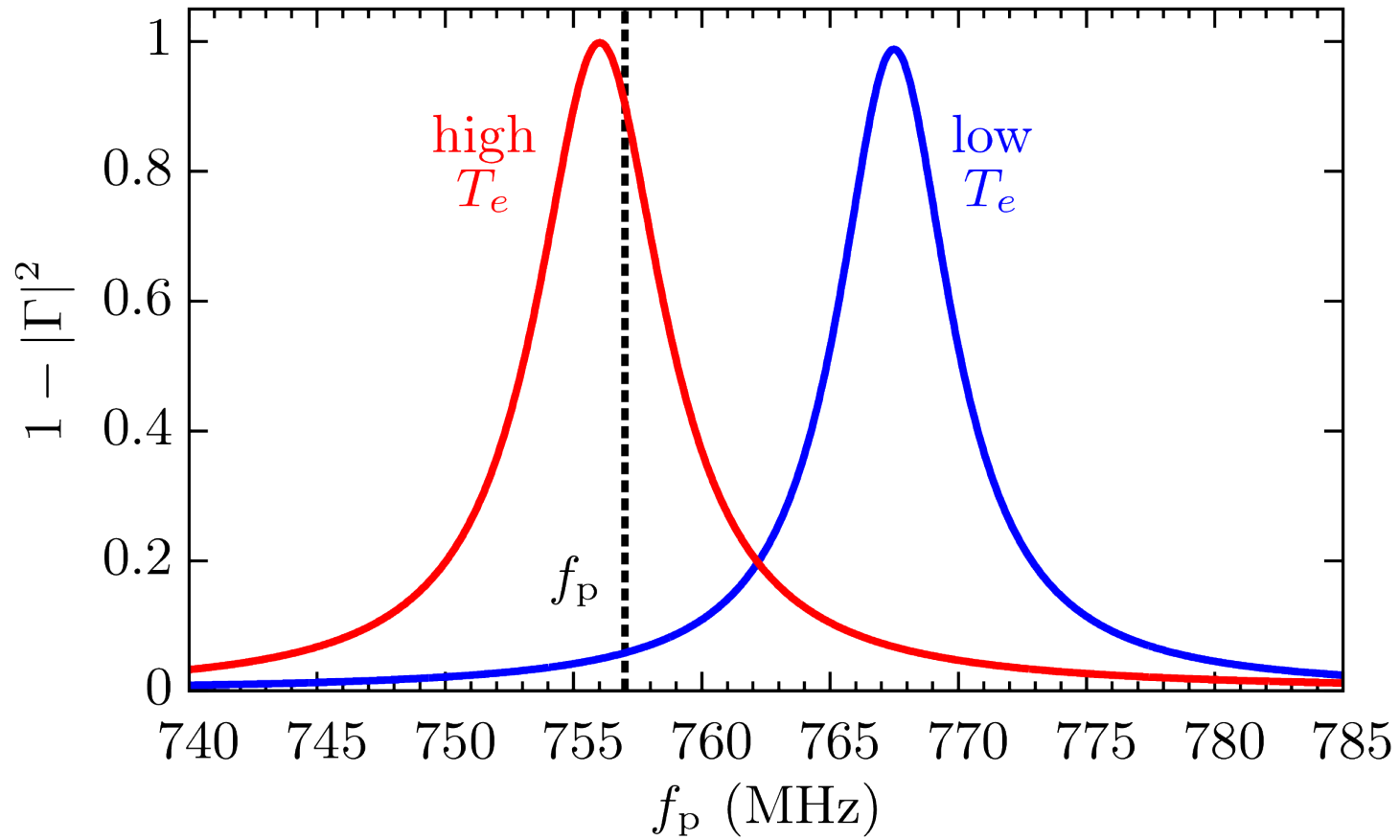
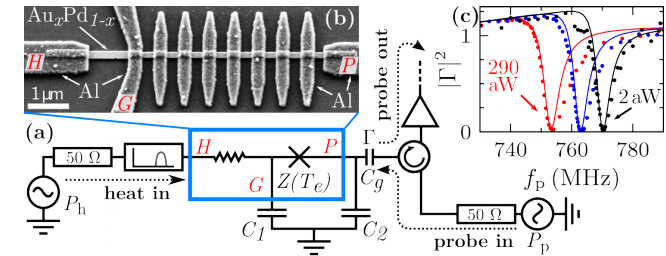


10^{-18}
 10^{-19}

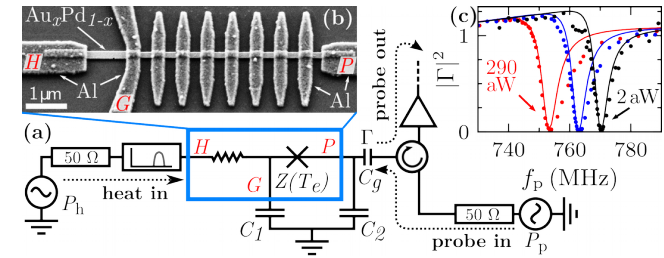
$\tau \tilde{G}_{fit} (J/K)$



Electrothermal non-linearity



Electrothermal non-linearity



“Thermal” power balance

$$C_e(T_e) \dot{T}_e = -P_{e-b}(T_e, T_b) + P_x + P_h + (1 - |\Gamma(T_e, \omega)|^2) P_p$$

heat flow to thermal bath

heater power

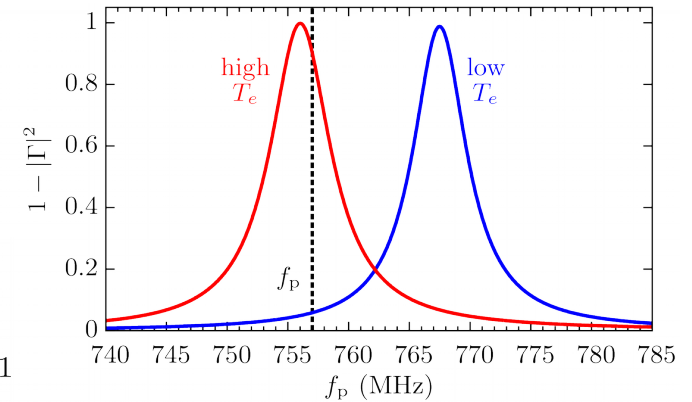
probe freq.

probe power

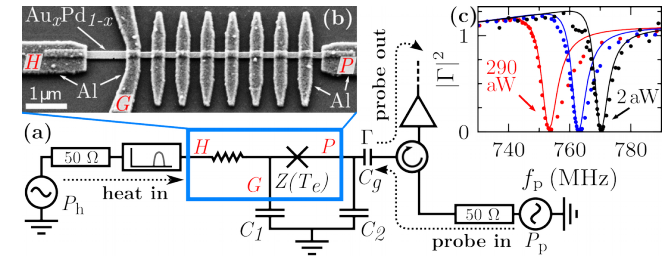
“Electrical” response

$$\Gamma(T_e, \omega) = \frac{Z_L(T_e) - Z_0}{Z_L(T_e) + Z_0},$$

$$\text{where } Z_L(T_e) = \frac{1}{i\omega C_g} + \left[i\omega C_2 + (Z^{-1}(T_e) + i\omega C_1)^{-1} \right]^{-1}$$



Electrothermal non-linearity



“Thermal” power balance

$$C_e(T_e) \dot{T}_e = -P_{e-b}(T_e, T_b) + P_x + P_h + (1 - |\Gamma(T_e, \omega)|^2) P_p$$

heat flow to thermal bath

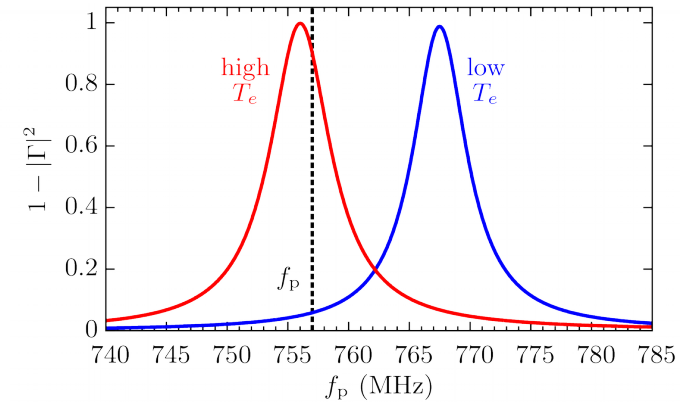
heater power

probe freq.

probe power

Change of variable from T_e to

$$\Delta(T_e) = P_{e-b}(T_e, T_b) - P_x$$



Electrothermal non-linearity

“Thermal” power balance

$$\rightarrow \tau(\Delta) \dot{\Delta} = -\Delta + P_h + (1 - |\Gamma(\Delta, \omega)|^2) P_p$$

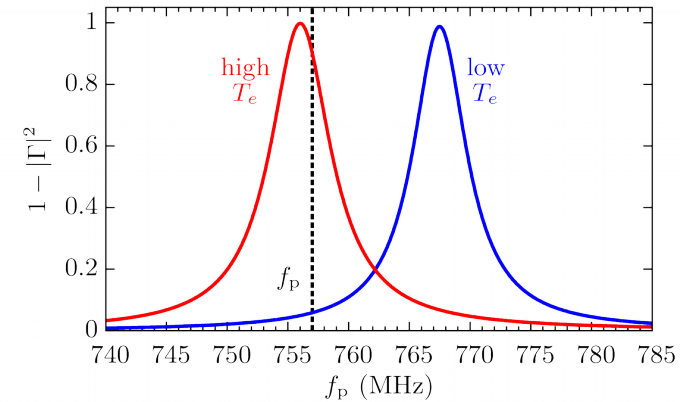
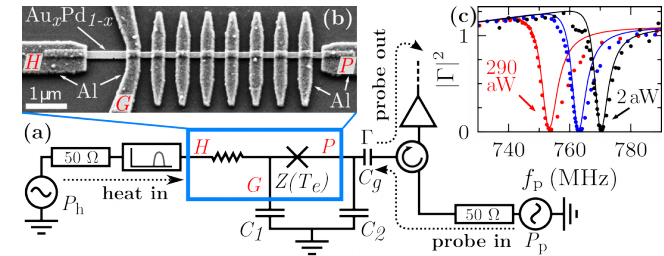
heater power

heat flow to thermal bath

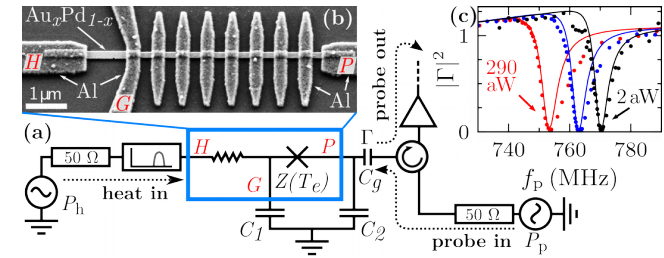
electrothermal nonlinearity

Change of variable from T_e to

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Electrothermal non-linearity



“Thermal” power balance

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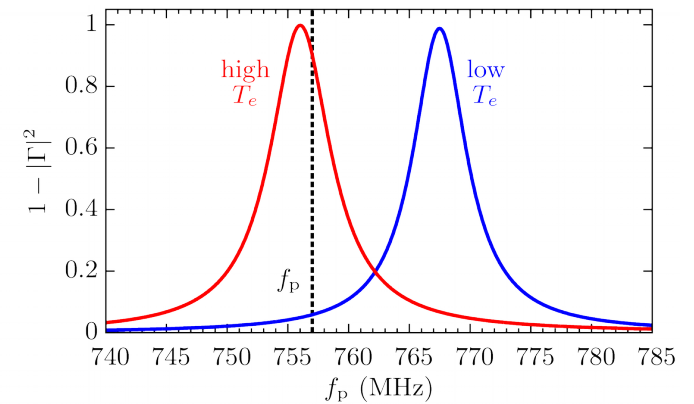
heater power

heat flow to thermal bath

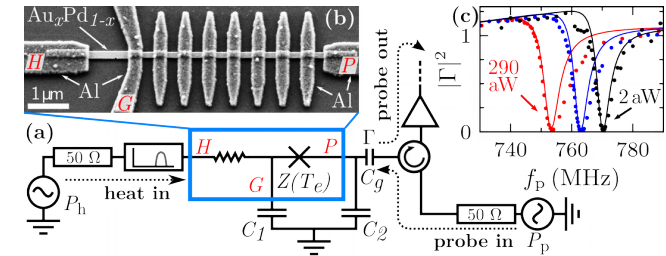
electrothermal nonlinearity

Susceptibility

$$\chi = \left. \frac{\partial \Delta}{\partial P_h} \right|_{\dot{\Delta}=0}$$



Electrothermal non-linearity



“Thermal” power balance

$$0 = -\Delta + P_h + (1 - |\Gamma(\Delta, \omega)|^2)P_p$$

heat flow
to thermal
bath

electrothermal
nonlinearity

heater
power

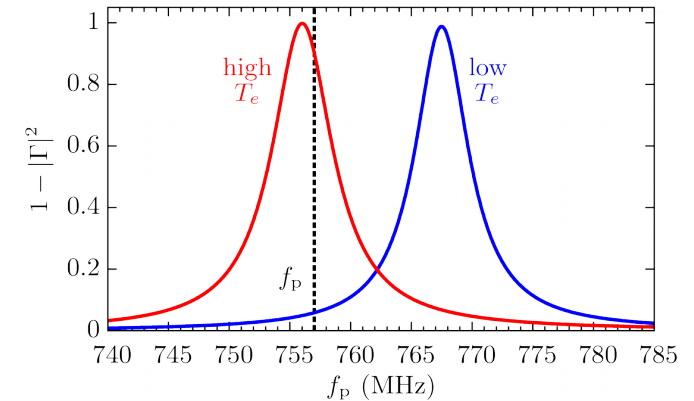
$$\frac{\partial}{\partial P_h}$$

Susceptibility

$$0 = 1 - \frac{\partial}{\partial P_h} |\Gamma(\Delta, \omega)|^2 P_p$$

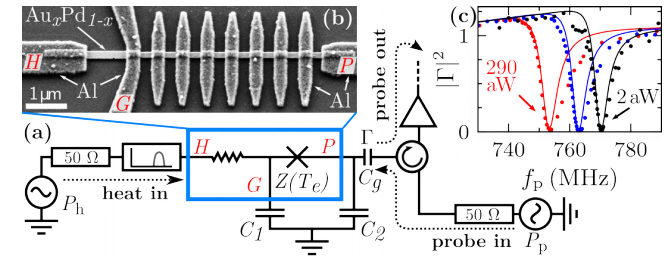
$$0 = 1 - P_p \frac{\partial \Delta}{\partial P_h} \frac{\partial |\Gamma(\Delta, \omega)|^2}{\partial \Delta}$$

$$\chi = \left(1 + P_p \frac{\partial |\Gamma(\Delta, \omega)|^2}{\partial \Delta} \right)^{-1}$$



$$\chi = \left. \frac{\partial \Delta}{\partial P_h} \right|_{\Delta=0}$$

Electrothermal non-linearity



“Thermal” power balance

$$0 = -\Delta + P_h + (1 - |\Gamma(\Delta, \omega)|^2)P_p$$

heater power

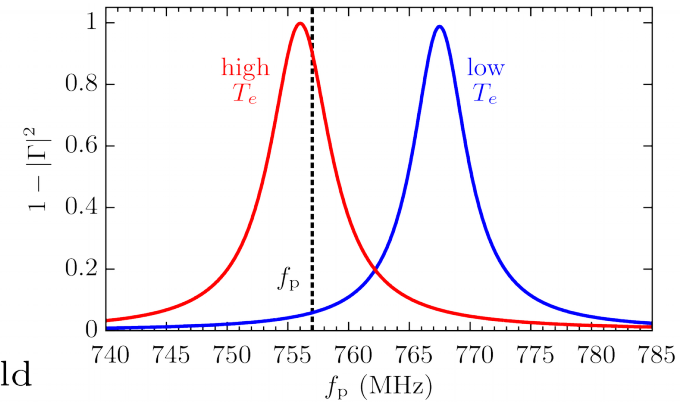
heat flow to thermal bath

electrothermal nonlinearity

Susceptibility

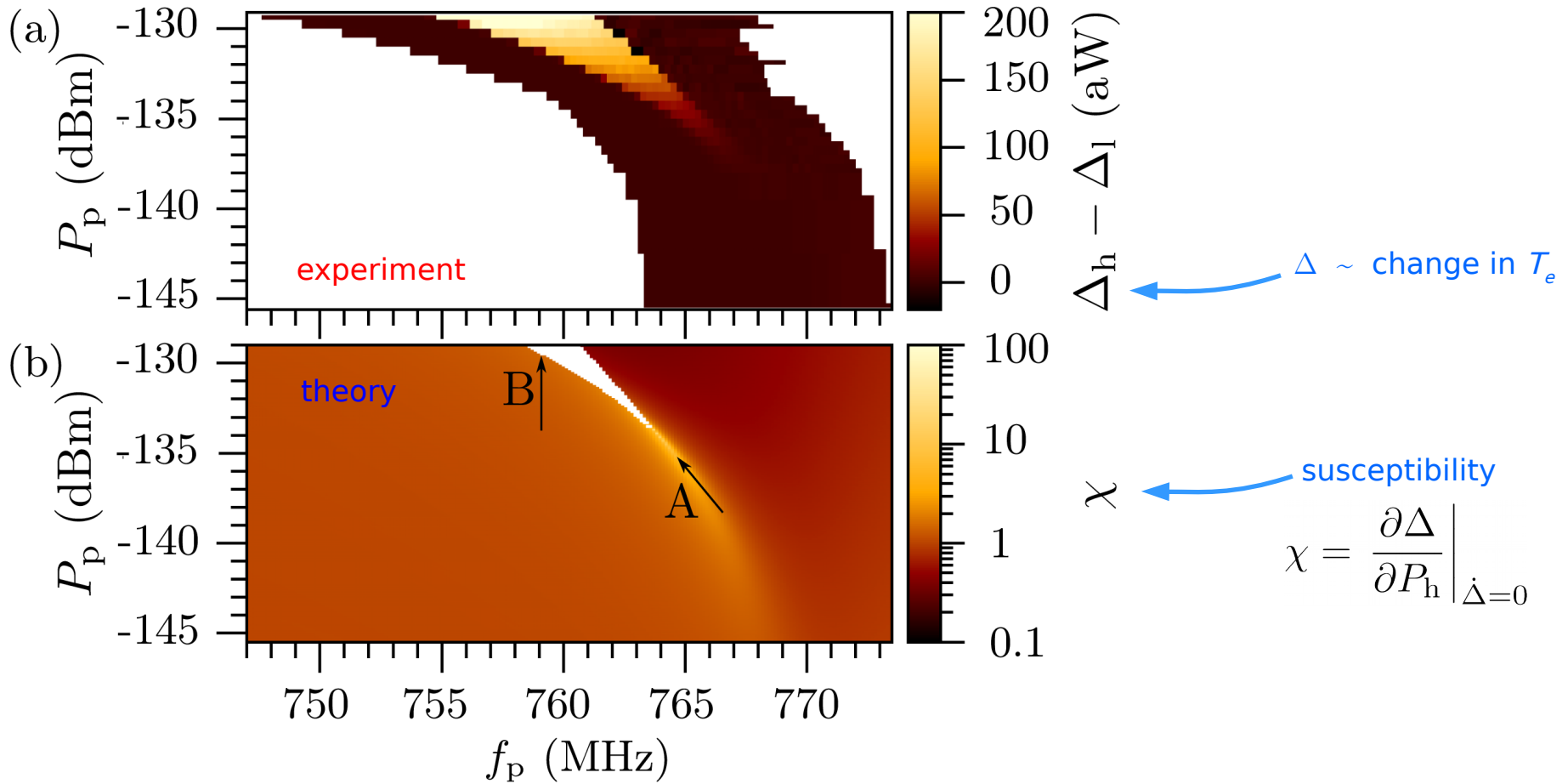
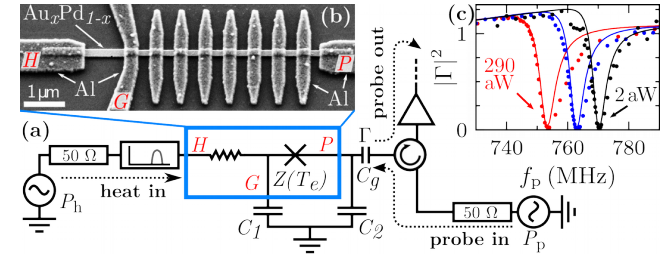
$$P_p \rightarrow - \left(\frac{\partial |\Gamma(\Delta, \omega)|^2}{\partial \Delta} \right)^{-1} \equiv P_{p, \text{threshold}}$$

$$\chi = \left(1 + P_p \frac{\partial |\Gamma(\Delta, \omega)|^2}{\partial \Delta} \right)^{-1}$$

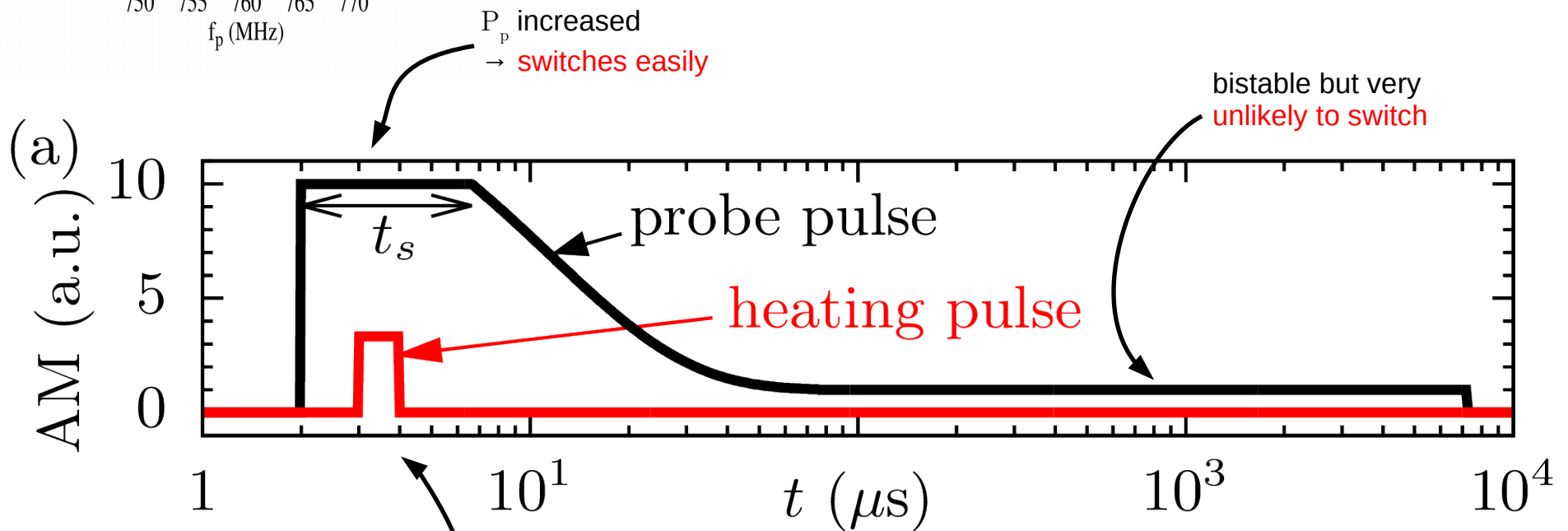
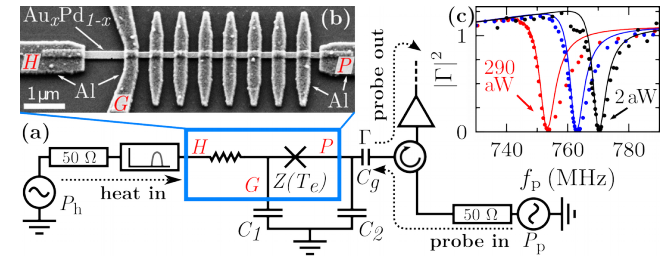
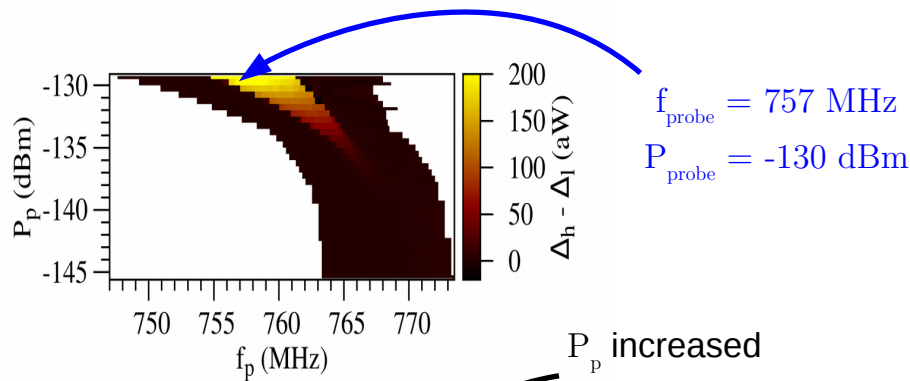


$$\chi = \left. \frac{\partial \Delta}{\partial P_h} \right|_{\Delta=0}$$

Electrothermal non-linearity – “phase diagram”

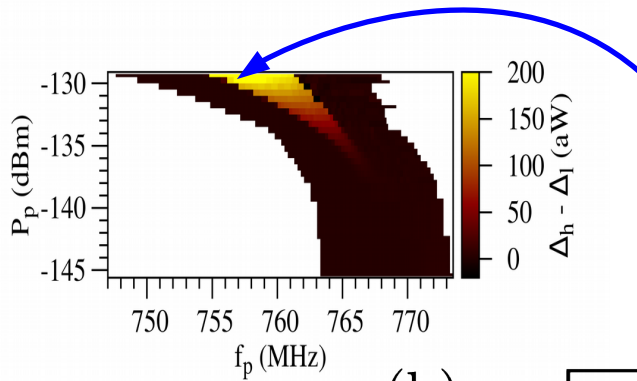


Threshold detection – pulse sequence

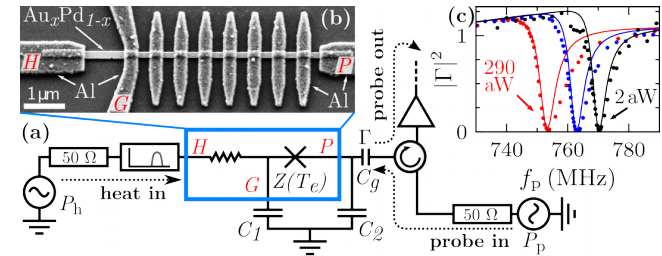


$P_{\text{heater}} = -120$ dBm for $1 \mu\text{s}$
 → $200 \times (h \times 8.4 \text{ GHz})$ of power

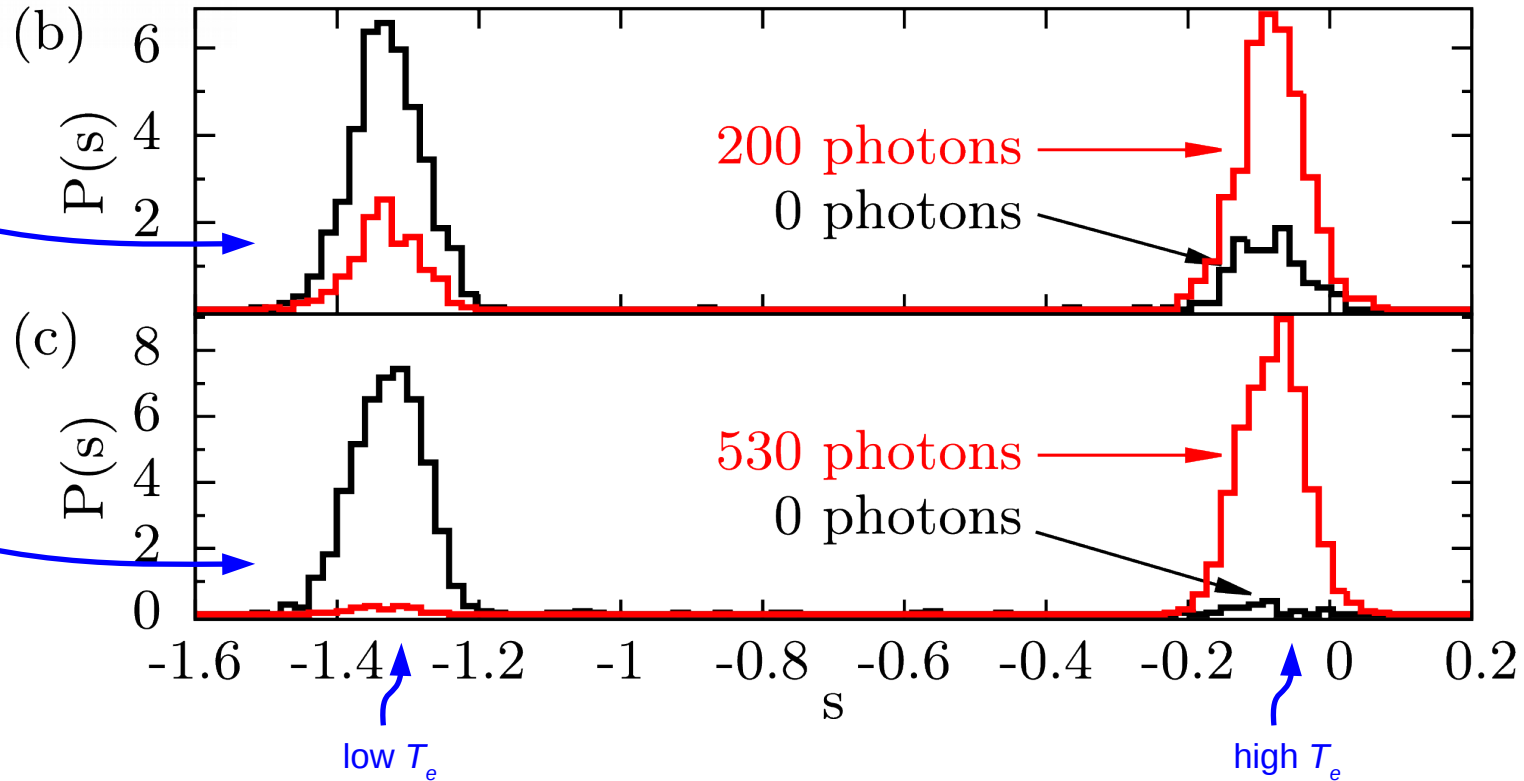
Threshold detection – histograms



$f_{\text{probe}} = 757 \text{ MHz}$
 $P_{\text{probe}} = -130 \text{ dBm}$

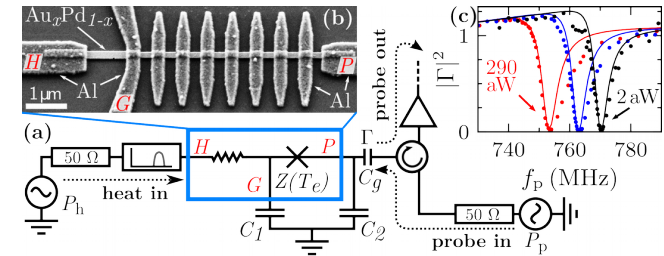


Fidelity = 0.56



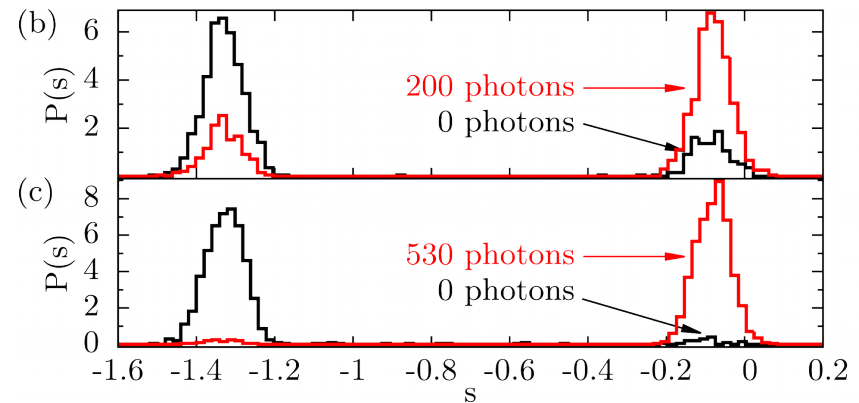
Fidelity = 0.94

Summary



Details in [Govenius et al., PRL 117, 030802 \(2016\)](#).

- detected $\sim 200 \times h \times 8.4 \text{ GHz} = 1.1 \text{ zJ}$ pulses
- using positive electrothermal feedback



The last slides on preliminary
noise equivalent power measurements
have been removed
from this online version.