

# Escape and retrapping experiments with Josephson $j$ junctions

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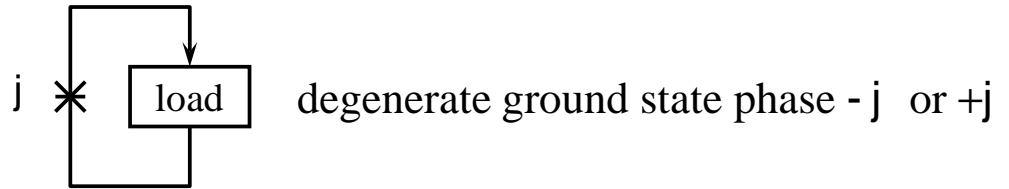
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**GIF**



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**DFG**

# j Josephson junction



## d-wave GB JJs (intrinsic $j$ JJ)

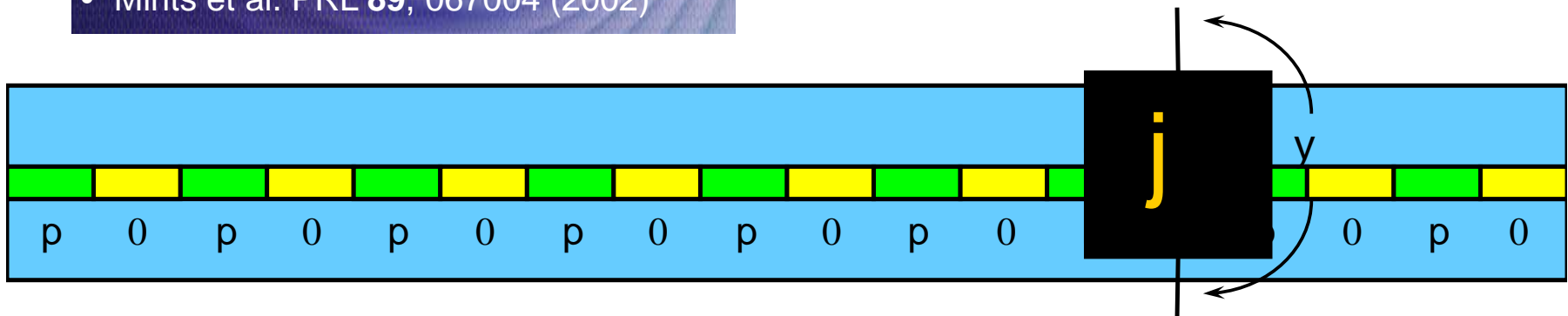
- Tanaka et al. PRB **56**, 892 (1997)
- Testa et al. APL **85**, 1202 (2004)
- Il'ichev et al. PRL **86**, 5369 (2001)

## $j$ JJ engineered from 0-p JJ:

- R. Mints et al. PRB **57**, R3221 (1998);
- A. Buzdin et al. PRB **67**, R220504 (2003).

## d-wave GB JJs (faceting $j$ JJ)

- Splintered vortices due to GB faceting:
- R. Mints et al. PRB **57**, R3221 (1998);
  - Mints et al. PRL **89**, 067004 (2002)

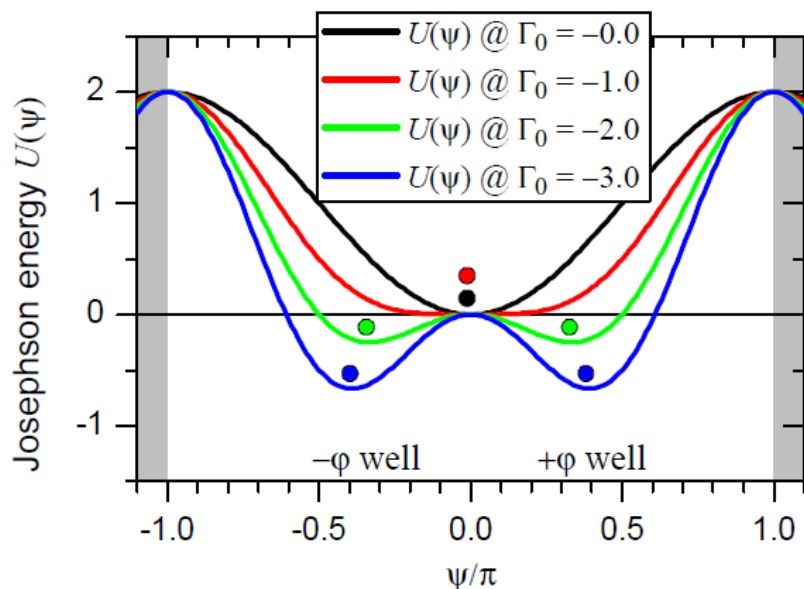


& Proposal: E. Goldobin et al., PRL **107**, 227001 (2011)  
& [http://www.pro-physik.de/details/news/3790631/Supraleiter\\_als\\_Phasenbatterie.htm](http://www.pro-physik.de/details/news/3790631/Supraleiter_als_Phasenbatterie.htm)

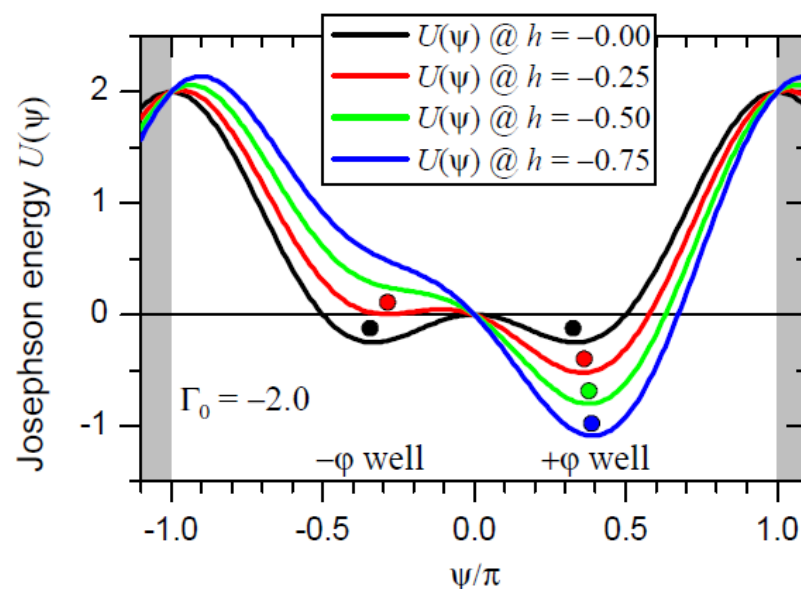
# j Josephson junction

$$U_J(\psi) = 1 - \cos(\psi) + \frac{\Gamma_0}{4} [1 - \cos(2\psi)] + \Gamma_h h \sin(\psi),$$

$$\varphi = \arccos(-1/\Gamma_0)$$



Bistable/two-level system



Ratchets & co.

& Proposal: E. Goldobin et al., PRL **107**, 227001 (2011)

& Experiment: H. Sickinger et al., PRL **109**, 107002 (2012)

& [http://www.pro-physik.de/details/news/3790631/Supraleiter\\_als\\_Phasenbatterie.htm](http://www.pro-physik.de/details/news/3790631/Supraleiter_als_Phasenbatterie.htm)

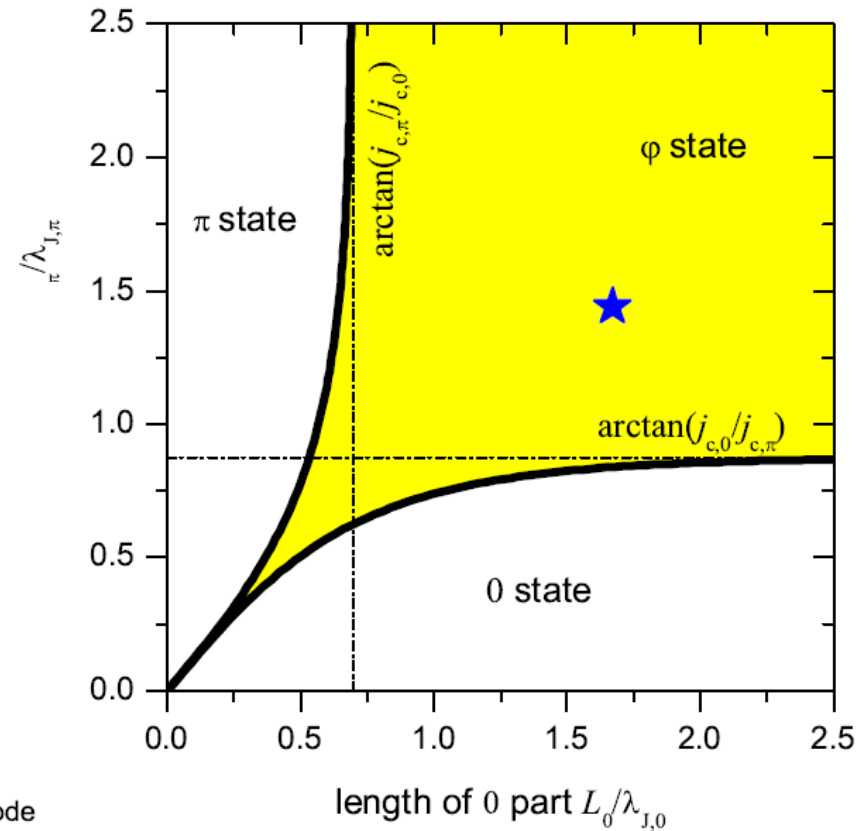
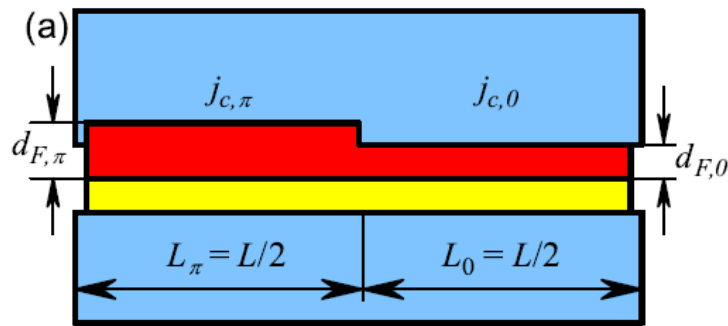
# Experiment: samples

SIFS 0- $\pi$  Josephson junction:

$L = 100+100$  nm,

$j_{c0} = 67.8 \text{ A/cm}^2$ ,  $j_{c\pi} = 47.4 \text{ A/cm}^2$ ,

$L_0 \sim 1.73 \lambda_{J,0}$ ,  $L_\pi \sim 1.45 \lambda_{J,\pi}$ , @300mK



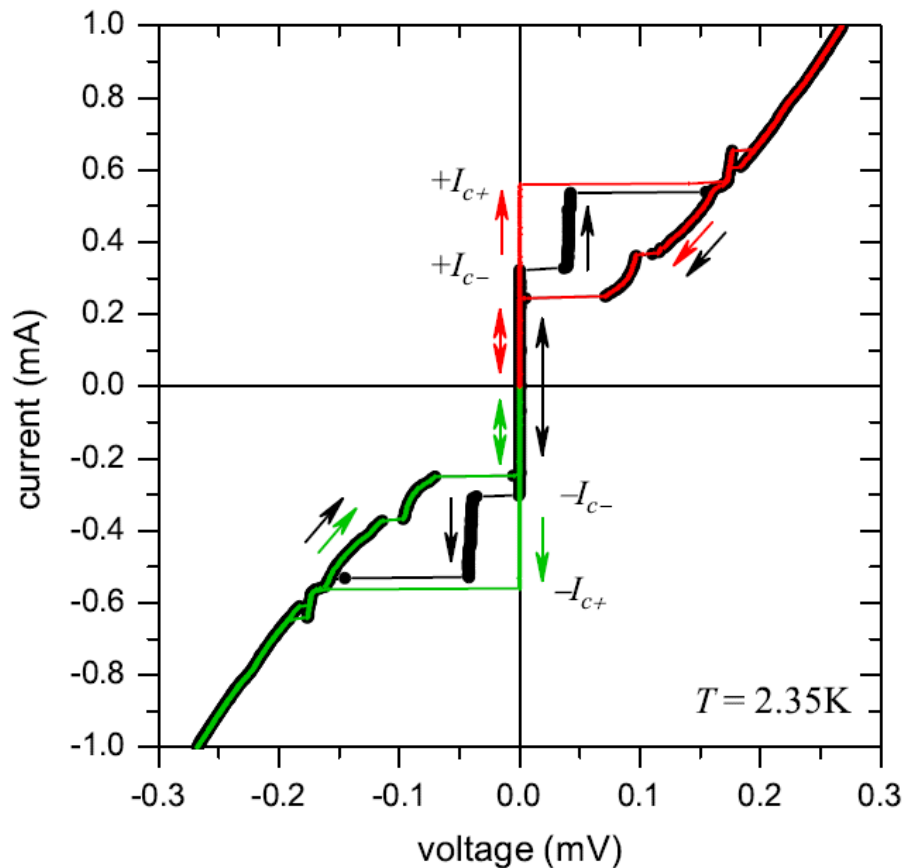
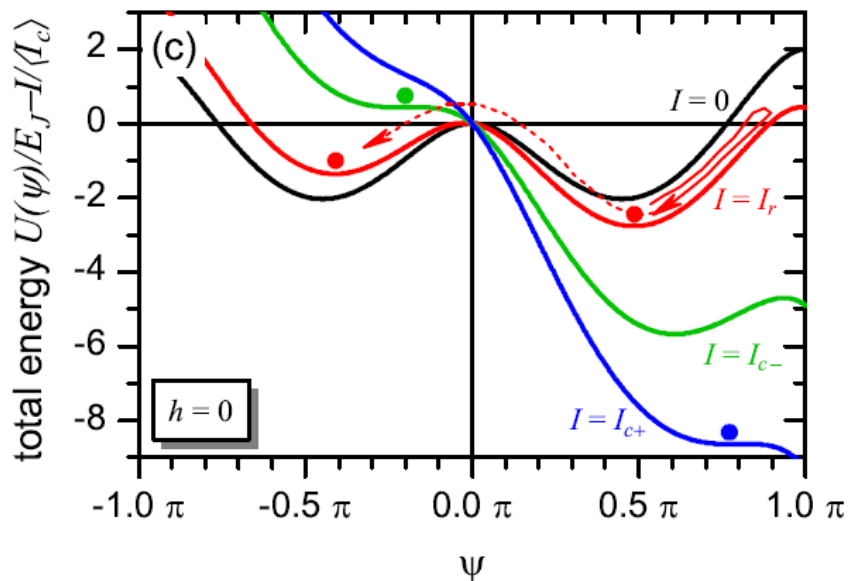
@  $T = 2.35$  K



# IVC: two critical currents

## Observation of $I_{c+}$ and $I_{c-}$

- $I_{c+}$  is always observed
- $I_{c-}$  only @  $0.3 \text{ K} < T < 3.5 \text{ K}$   
(low damping  $a$ )
- immediate retrapping in the  $+j$  well  
(high damping  $a$ )

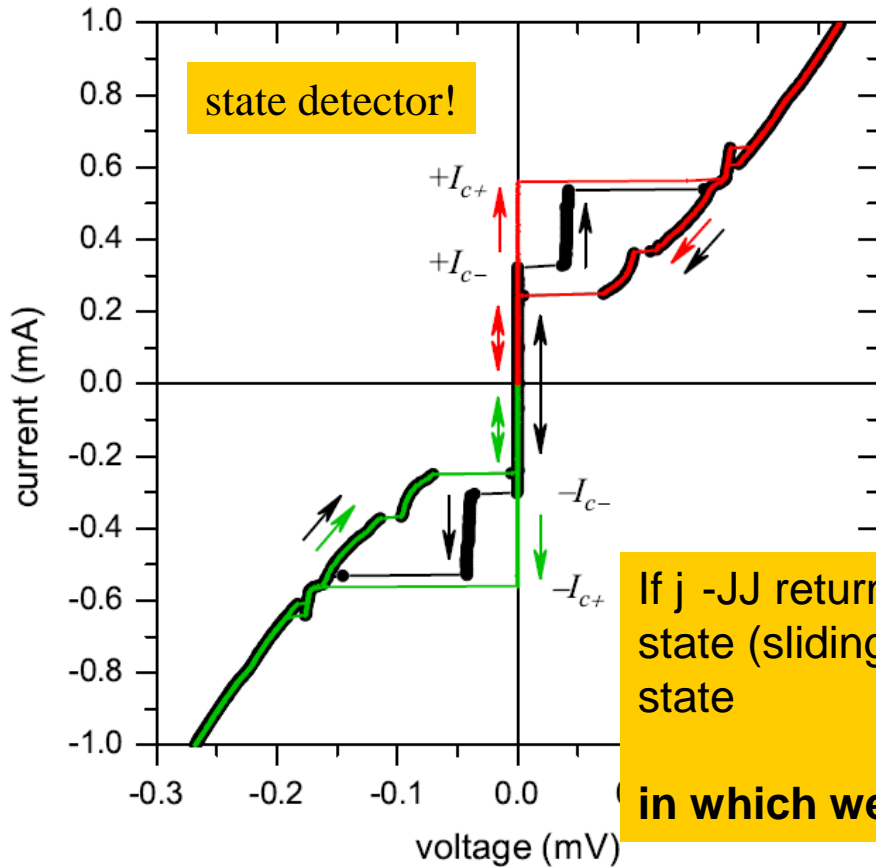


**state detector!**

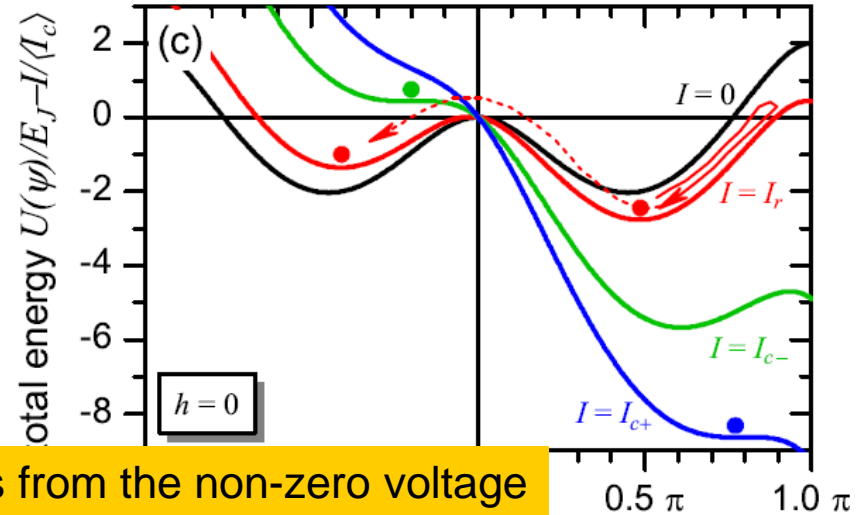
# Phase retrapping in $j$ JJ

# IVC and phase retrapping

*I*--*V* characteristic



$$U(\psi) = U_J(\psi) - \gamma\psi,$$

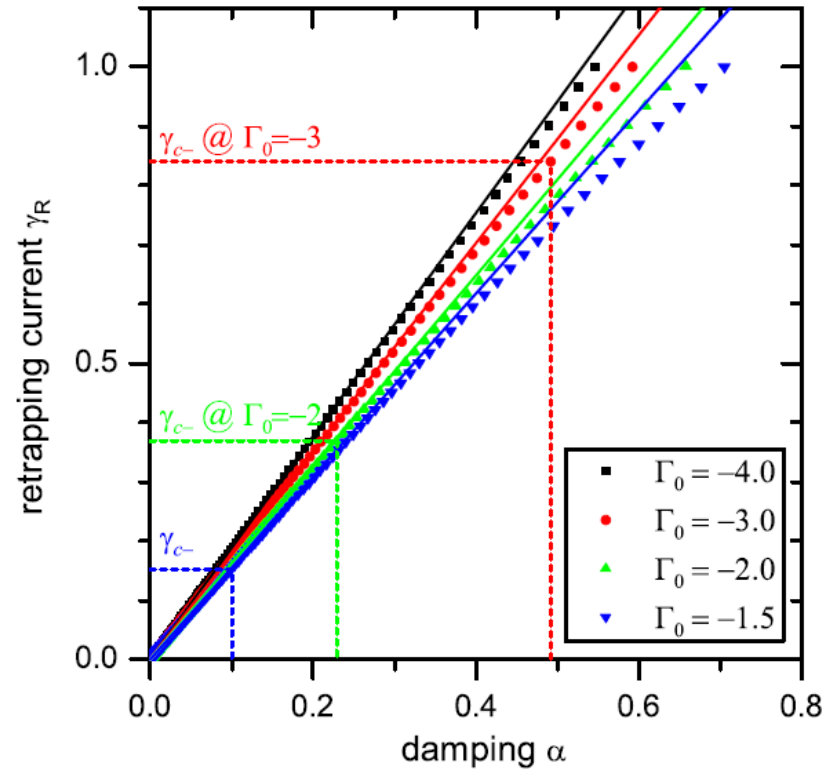
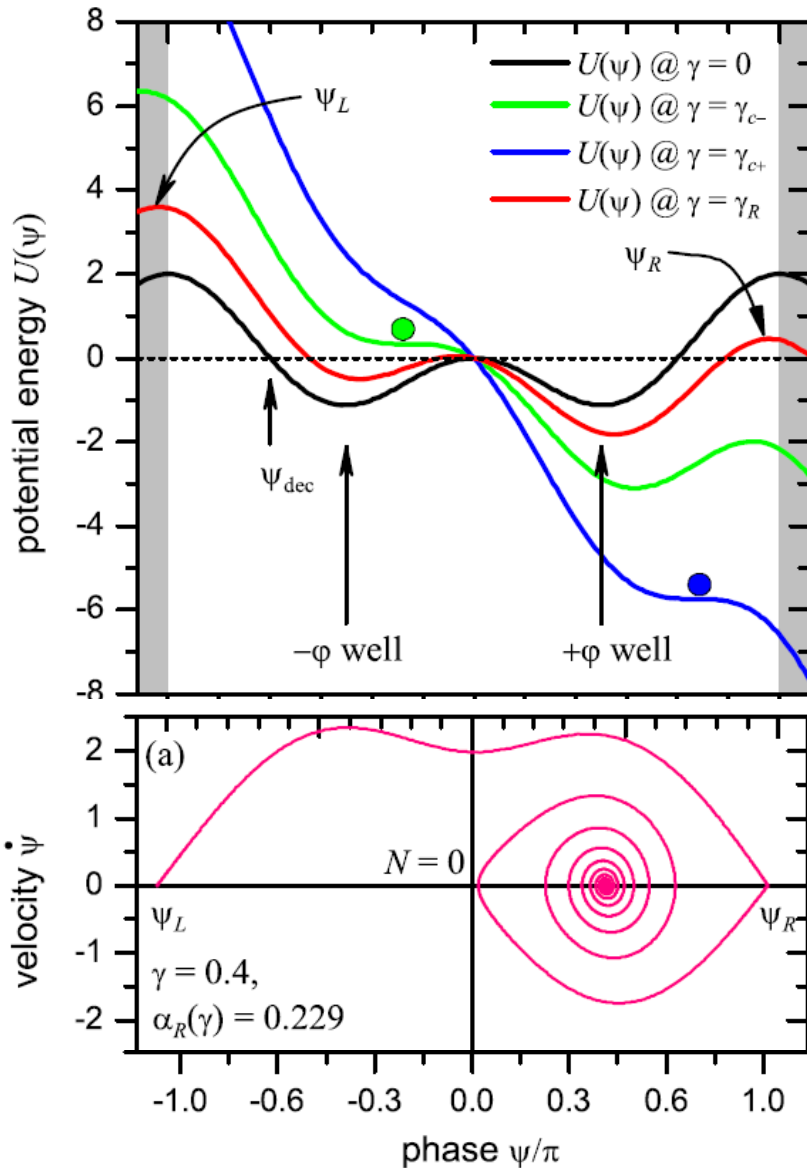


If *j* -*JJ* returns from the non-zero voltage state (sliding phase) to zero voltage state

in which well is the phase trapped?

$$\ddot{\psi} + \frac{\partial U_J}{\partial \psi} = \gamma - \alpha \dot{\psi},$$

# Phase Retrapping

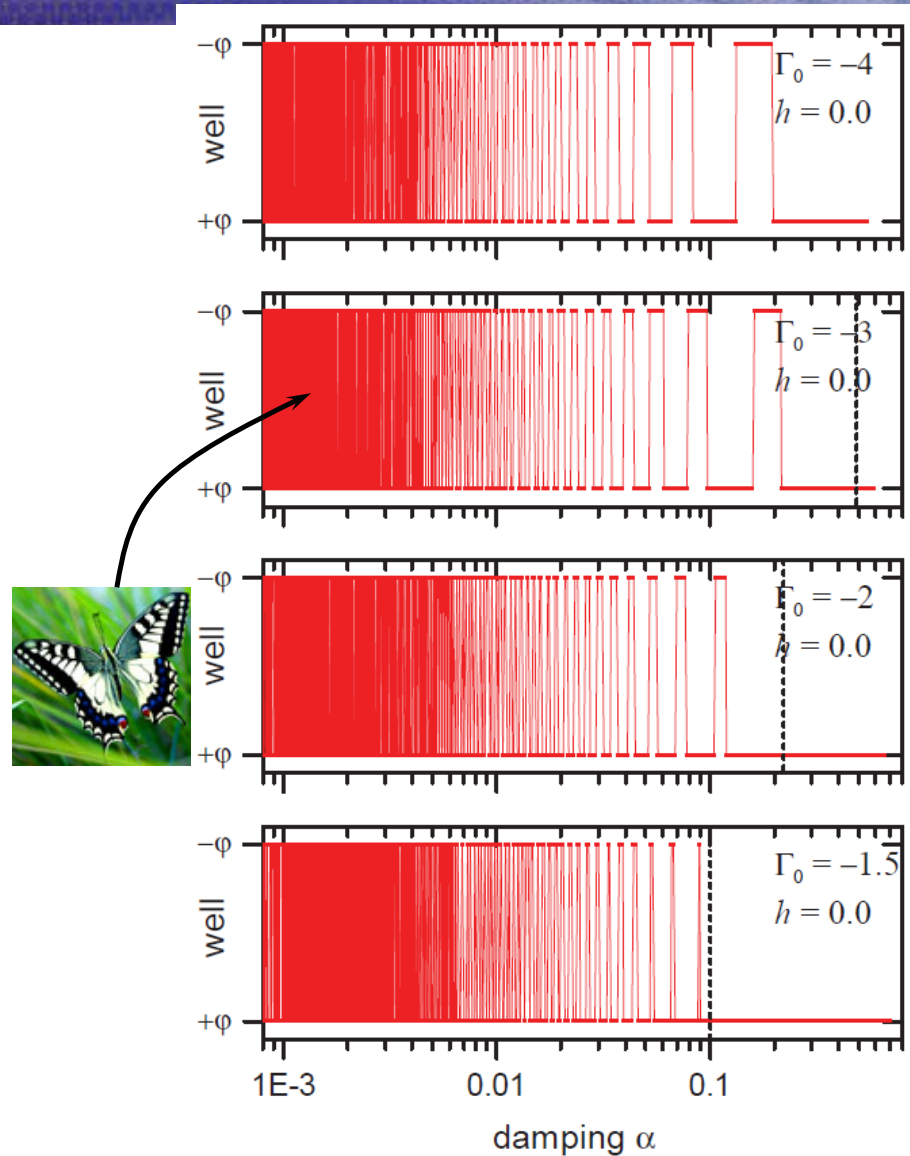
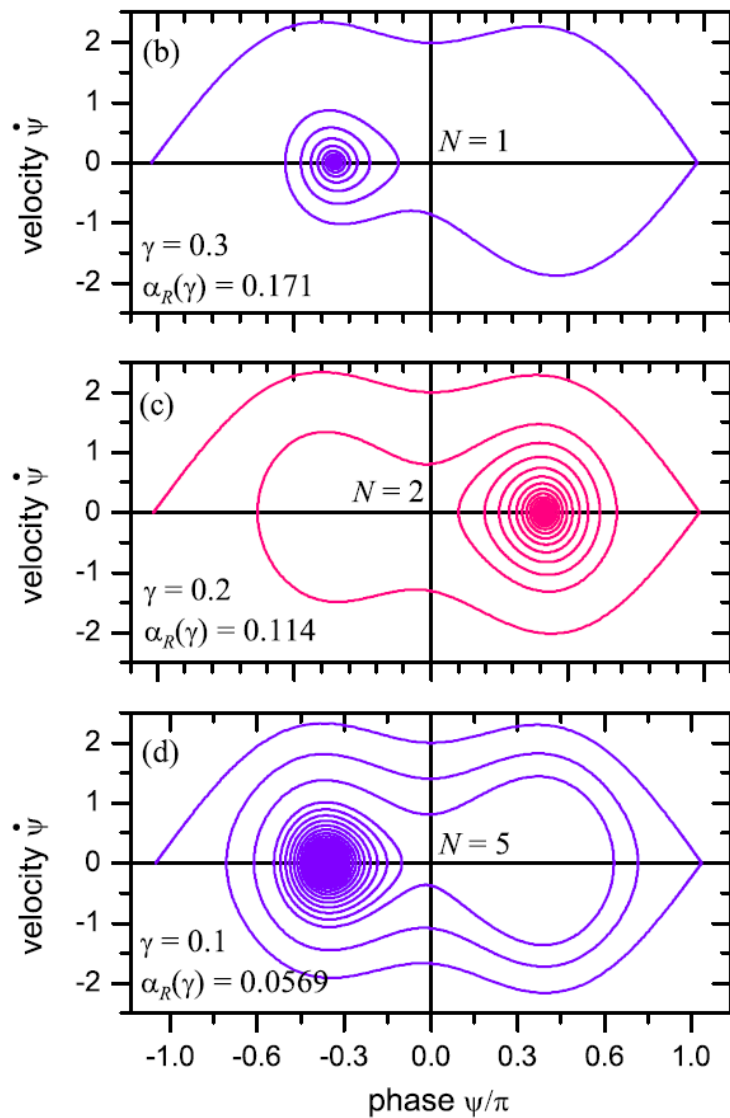


Perturbation theory ( $a \ll 1, g \ll 1$ ):

$$\gamma_R(\alpha) = \frac{I(\Gamma_0)}{2\pi} \alpha.$$

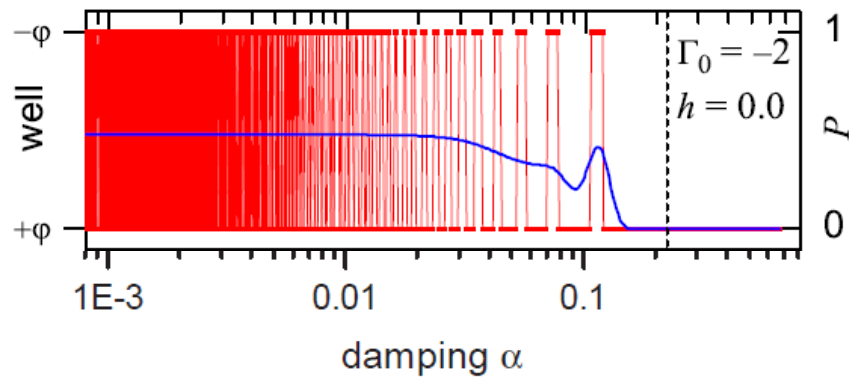


# Butterfly effect

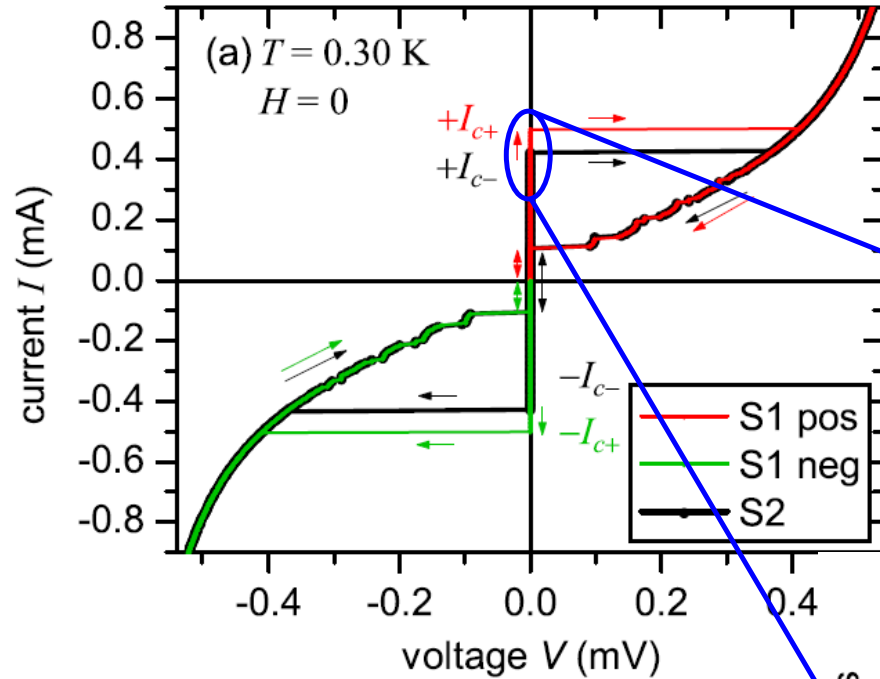


# Presence of noise

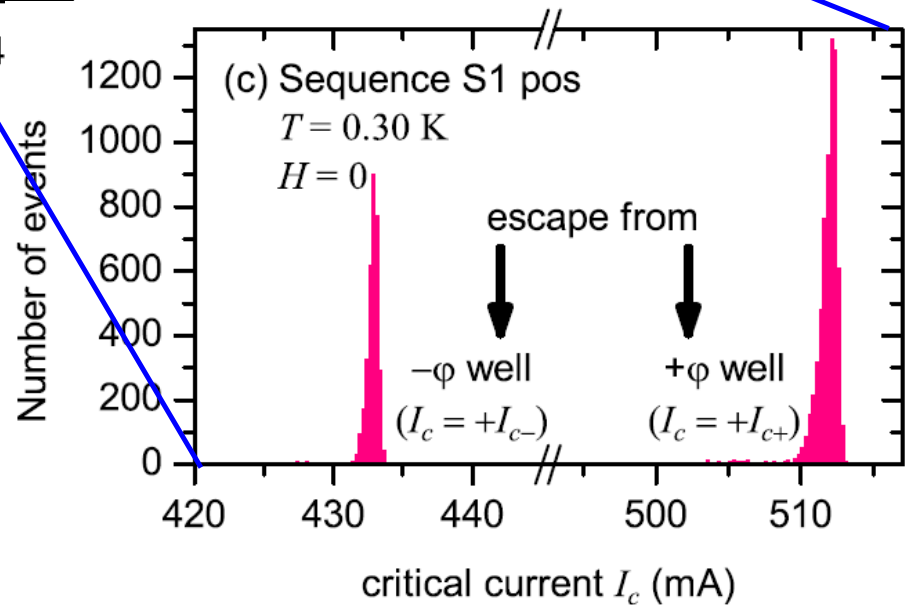
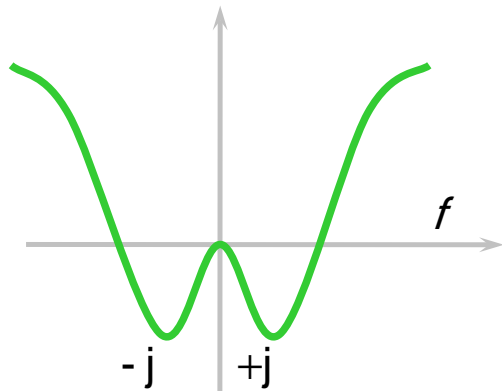
Simple model: low frequency Gaussian noise



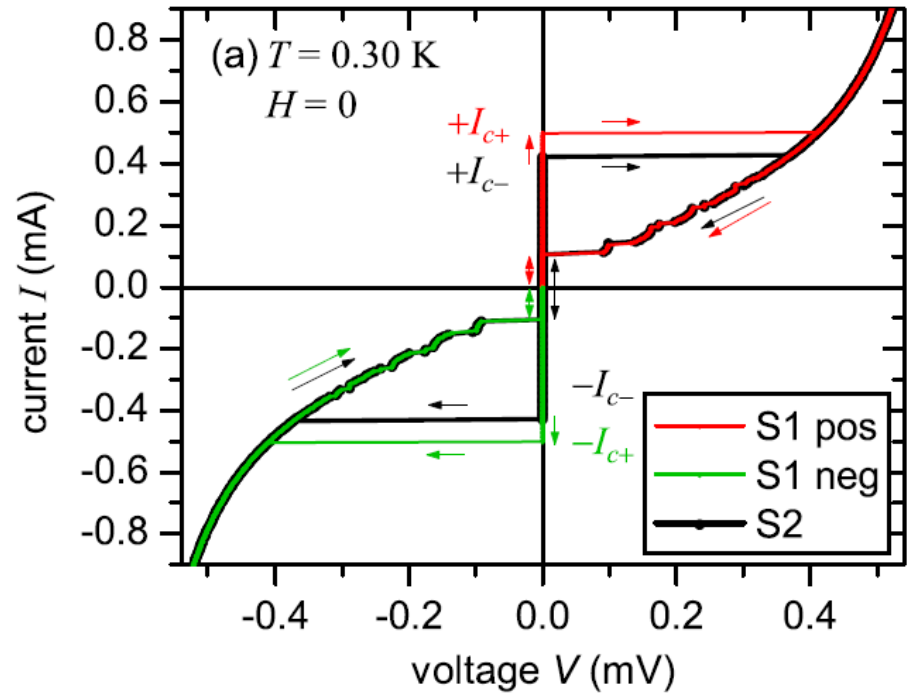
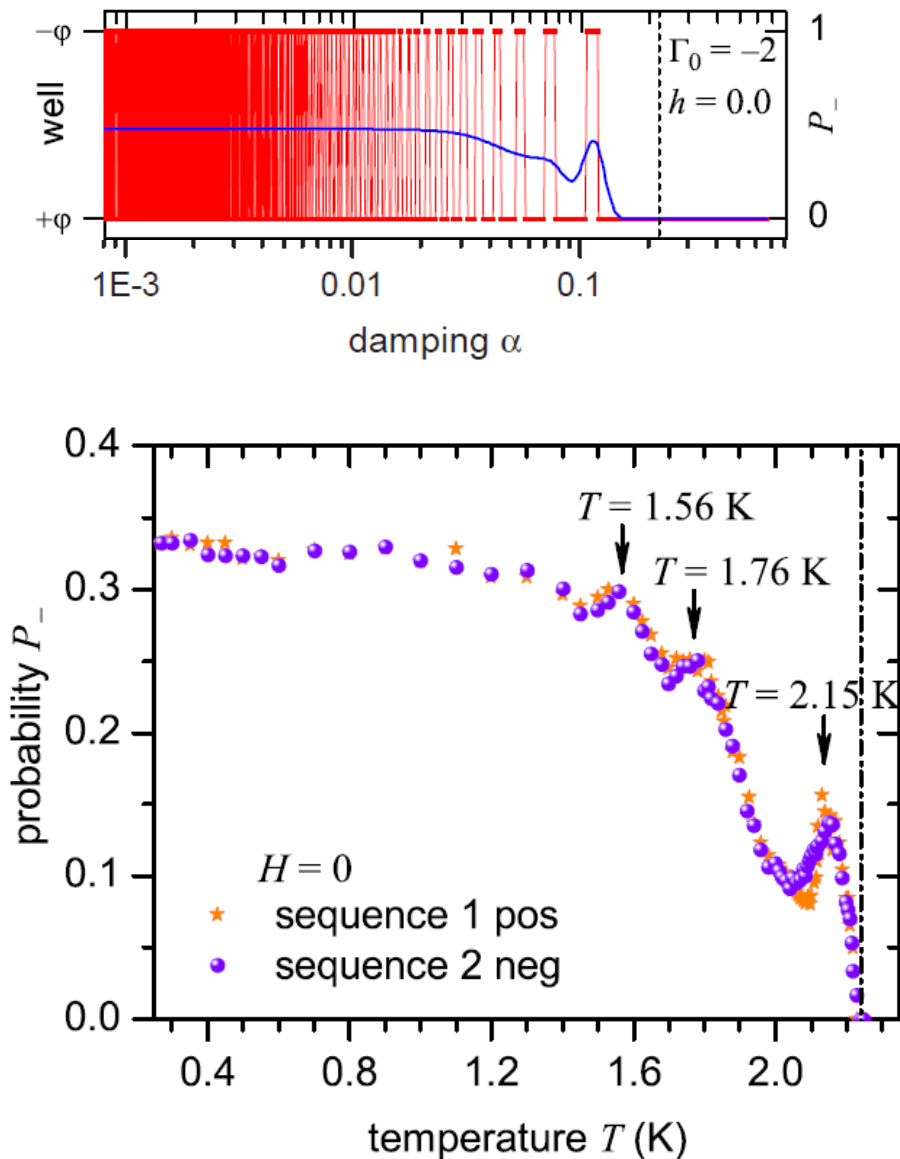
# Experiment: Retrapping + Escape



Nb-AlO-CuNi-Nb JJ:  
 $L = 100+100$  nm,  
 $j_{c0} = 67.8$  mA/cm<sup>2</sup>,  $j_{cp} = 47.4$  A/cm<sup>2</sup>,  
 $L_0 \sim 1.73 |J_{0,0}|$ ,  $L_p \sim 1.45 |J_{p,0}|$ , @0.3K



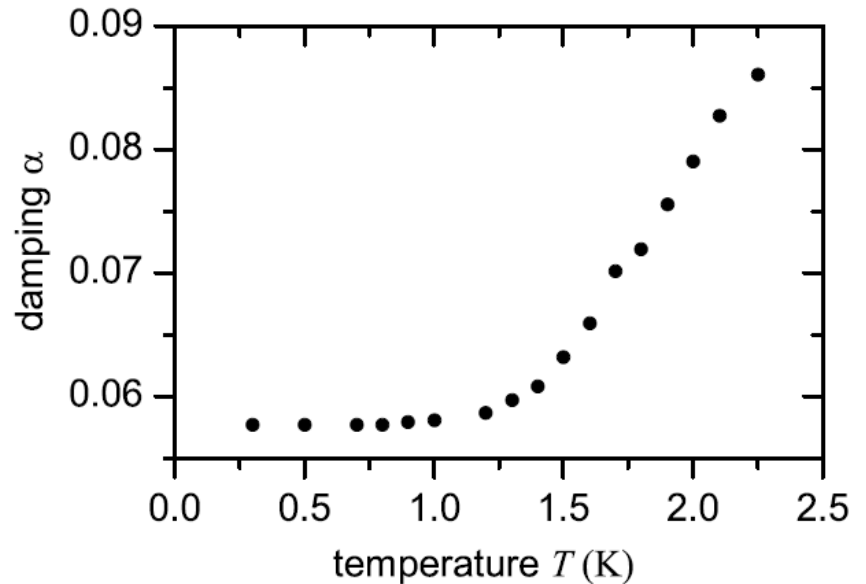
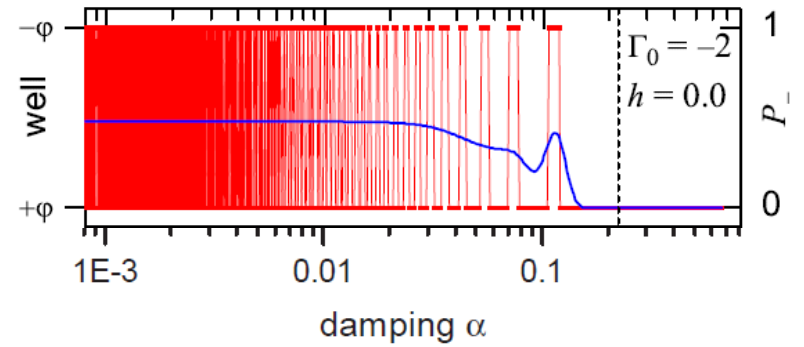
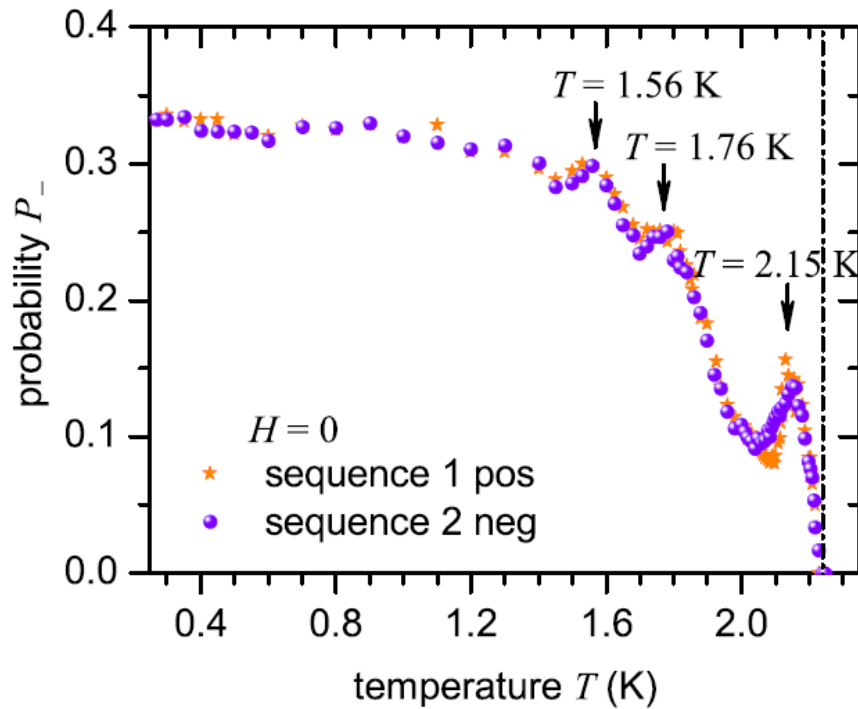
# Retrapping statistics vs. $T$



## Why saturation of $P_-$ is not at 50%?

- Asymmetric double well potential
- Saturation of damping  $a(T)$
- other nontrivial effects

# Retrapping statistics vs. $T$





# Summary

## Summary:

- è Introduction to  $j$ -JJs and their main properties
- è Phase retrapping experiments:
  - è Onset of the butterfly effect
  - è Saturation at 33% instead of 50%  
(due to saturation of the damping)

## Outlook:

- è **repeat the experiment with a low damping system (e.g. SIS JJ) to reach lower damping i.e. go deeper into the butterfly-effect region.**